Growth of the silverside *Atherinella brasiliensis* in a subtropical estuary with some insights concerning the weight-length relationship

**BARBARA M. DE CARVALHO**¹, **JOSÉ RICARDO S. BARRADAS**², **NELSON F. FONTOURA**³ and **HENRY L. SPACH**¹³

¹Programa de Pós-Graduação em Zoologia, Departamento de Zoologia, UFPR, Centro Politécnico, Caixa Postal 19020, Jardim das Américas, 81531-980 Curitiba, PR, Brazil
²Faculdade de Biociências, PUCRS, Av. Ipiranga, 6681, 90619-900 Porto Alegre, RS, Brazil
³Programa de Pós-Graduação de Sistema Costeiro e Oceânicos, UFPR, Av. Beira-Mar, s/n, Caixa Postal 61, Bal. Pontal do Sul, 83255-976 Pontal do Paraná, PR, Brazil

Manuscript received on November 10, 2016; accepted for publication on March 8, 2017

**ABSTRACT**

Specimens of Brazilian silverside (*Atherinella brasiliensis*, *n*=9672) with a length range of 1.5 to 14.2 cm were captured in the intertidal areas of the Estuarine Complex of Paranaguá, Brazil, between August 2010 and July 2011. The species’ weight-length relationship was represented by the equation $W=0.00533 L^{3.136}$ with a slightly positive allometry ($b>3$) and could be divided into two growth stanzas: $W = W_1 + W_2$; Stanza 1: $W_1 = SW_1 (0.005239 L^{3.152})$; Stanza 2: $W_2 = (1 – SW_1) (0.000699 L^{3.913})$; Switch-Function: $SW = \left[1 + e^{1.204 (L – 11.66)}\right]^{-1}$. The breakpoint between the first and second stanza (11.66 cm) matches published values for the estimated size at first maturity of adult females. Frequency distributions indicate that the species is present in the shallow areas of the Estuarine Complex of Paranaguá during all phases of its ontogenetic development, with the recruitment of juveniles taking place between October and November. Modal displacement was monitored throughout 12 months. The von Bertalanffy growth model and longevity was estimated as follow: asymptotic length ($L\infty$) of 17.5 cm, growth coefficient ($K$) of 0.89 (year$^{-1}$) and longevity ($A_{95}$) of 3.33 years. We present some considerations with regard to the general methodology for adjusting weight-length relationships.

**Key words**: Atherinopsidae, longevity, von Bertalanffy, weight-length relationship.

**INTRODUCTION**

Floor growth patterns are influenced by counteracting driving forces, such as food availability, environmental factors and species requirements during the fish life cycle, e.g. for reproduction, migration or territory defense. By investing energy to grow faster, fish can avoid high predation rates of smaller animals. On the other hand, a focus on early reproduction reduces expected final size, but increases the chance of an individual to pass its genes on to the next generation. Therefore, the success of a species and its life-history strategy results from interacting temporal and spatial driving forces. In this regard,
a specific growth pattern could be interpreted as an indirect result of the selected life strategy. For example, species with a wide geographical range are likely to have latitudinal growth patterns, with increasing final size and decreasing growth rates in higher latitudes (Taylor 1958, 1959, 1960, 1962, Pauly 1980, Fontoura and Agostinho 1996, Giacomini and Shuter 2013, Peck et al. 2013).

The family of Atherinopsidae comprises 13 genera and 104 species of marine, estuarine and freshwater fish, 14 of which occur in Brazil: *Atherina lessoni*, *Atherinella blackburni*, *A. brasiliensis*, *Odontesthes argentinensis*, *O. bicudo*, *O. bonariensis*, *O. incisa*, *O. humensis*, *O. eleae*, *O. perugiae*, *O. piquava*, *O. mirinensis*, *O. retropinnis* and *Pseudothyrina iheringi* (Froese and Pauly 2017).

*Atherinella brasiliensis* has the widest geographic distribution of all American Atherinopsidae, ranging from Venezuela (10° N) to southern Brazil (32° S) (Brian and Dyer 2006). *Atherinella brasiliensis* is common in estuarine areas, but also occurs in coastal waters (Hostim-Silva et al. 1995, Pessanha and Araújo 2001, Neves et al. 2006, Fávaro et al. 2007). The species has generalist and opportunistic feeding habits (Chaves and Vendel 2008, Contente et al. 2010). Estimated length at first maturity varies from 7.6 to 9.1 cm of total length. Intense reproduction activities take place between October and January (Bervian and Fontoura 1997, Fávaro et al. 2003), involving the deposition of adherent benthic eggs and direct larval development (Del Rio et al. 2005). A compilation of published information concerning growth and mortality of the species along the Brazilian coast is presented in Table I. The weight-length relationship is characterized by positive allometric growth. Concerning parameters of the von Bertalanffy growth curve, asymptotic lengths are estimated between 11.3 and 17 cm and the growth constant ranging between 0.82-0.89 (year\(^{-1}\)); resulting in longevity estimates of slightly more than three years (Paiva-Filho and Giannini 1990, Haimovici and Velasco 2000, Pessanha and Araújo 2001, Giarrizzo et al. 2006, Macieira and Joyeux 2008, Mazzei et al. 2011, Freire et al. 2012, Costa et al. 2013, Franco et al. 2013).

In the present study we describe the weight-length relationship and growth patterns of *A. brasiliensis* within the Estuarine Complex of Paranaguá (Paraná, Brazil), aiming to identify possible latitudinal trends of the species along the Brazilian coast. Also, some considerations with regard to the general methodology for adjusting weight-length relationships are presented.

**MATERIALS AND METHODS**

Specimens were collected once a month between August 2010 and July 2011 at 17 sites along the north-south axis in intertidal areas (~1 m, neap tide) of the Estuarine Complex of Paranaguá, Brazil (Fig. 1, 25° 15’ - 25° 35’ S and 48° 20’ - 48° 45’ W) through a 30 m coastal trawling with a beach seine net (15 m long; 2 m high; 2.5 mm mesh) (IBAMA 10.876). After collection, specimens were cooled, identified to species (Menezes and Figueiredo 2000), measured for total length (Lt; 0.01 cm) and weighed (P; 0.01 g).

Weight-length relationship was adjusted by using a power equation (Froese 2006): \( W = aL^b \), where \( W \) is the weight (g), \( L \) is the total length (cm), \( a \) is the coefficient of proportionality, and \( b \) is the coefficient of allometry. To avoid the bias of log-transformation (Smith 1993), function adjustment was made with untransformed data by using the Solver tool of Microsoft Excel 10.0 (non linear GRG). To identify trends concerning polyphasic growth (Bervian et al. 2006) the data set was grouped into size intervals (log scale, 0.0339 increment), where each size class was represented by mean length and mean weight of all selected individuals. This procedure had two main objectives: (1) to cluster several animals...
within a single information point, aiming to reduce the natural variability that can hide subtle trends, and (2) by using narrower size classes for small and abundant juveniles, and by increasing the size interval (on a log scale) for larger fishes to account for their lower abundance in samples, thus minimizing (but not eliminating) bias from the unbalanced sampling design. To handle intrinsic heteroscedasticity of the weight-length relationship data, a power function was adjusted to the weight standard deviation of each size class: 

\[ W_{sd} = a_{sd} \cdot L_{c}^{bsd}, \]

where \( W_{sd} \) is the weight standard deviation for each size class, \( L_{c} \) is average total length of each size class, and \( a_{sd} \) and \( b_{sd} \) are empirical coefficients. Once a general trend concerning the heteroscedastic pattern was identified, this trend was used to keep a homoscedastic residual: 

\[ R_h = \frac{(W - West)}{(a_{sd} \cdot L_{c}^{bsd})}, \]

where \( R_h \) is the homoscedastic residual, \( W \) is the measured weight of each individual and \( West \) is the estimated weight of the weight-length function. Complementary procedures for polyphasic adjustment can be found in Bervian et al. (2006), Fontoura et al. (2010) and Oliveira et al. (2011). Detailed scripts for polyphasic fitting by using R statistical platform could be found in J.R. Barradas (unpublished data; http://repositorio.pucrs.br/dspace/bitstream/10923/8518/3/TES_JOSE_RICARDO_DE_SOUZA_BARRADAS_COMPLETO.pdf).

The species life cycle was interpreted by grouping specimens into length-frequency intervals (every other month) to improve visibility concerning the general pattern of modal displacement. Age groups were estimated by taking into account the time gap between each sample and the climax of the annual reproductive period (October in the Bay of Paranaguá; Fávaro et al. 2003). The age of each specimen was assessed according to its age group. Superimposed age groups were artificially divided within the crossing edge of both tails.

Size-at-age was described by the von Bertalanffy (1938) growth curve:

\[ L_t = L_{\infty} \cdot [1 - e^{-K \cdot (t-t_0)}], \]

where: \( L_t \) is total length (cm) at age \( t \) (years), \( L_{\infty} \) is the asymptotic length, \( K \) is the instantaneous
growth rate, and \( t_0 \) is a time-correcting factor related to the size at birth or eclosion. Model adjustment (SPSS 17.0; nonlinear routine; Levenberg-Marquardt algorithm) was performed by using the length to age relationship of all captured individuals comprising a time series of the first identified age-group in November/2010; which was followed to July/2011. As there were no captures after July/2011, animals that belonged to this age group (1+) but were captured between August-November/2010, were used to emulate the growth pattern of this cohort. Longevity, estimated as the time a fish takes to reach 95% of \( L_\infty \), was calculated as follows: \( A_{95} = -2.96/K \), in which \( K \) is the instantaneous growth rate of the von Bertalanffy growth model (Taylor 1958, 1959, 1960, 1962).

Using the available growth and mortality parameters of \( A. \) brasiliensis along the Brazilian coast, linear regressions were applied to identify latitudinal patterns as described in the literature (Taylor 1958, 1959, 1960, 1962, Pauly 1980, Fontoura and Agostinho 1996, Giacomini and Shuter 2013, Peck et al. 2013).

RESULTS

Captured specimens of \( A. \) brasiliensis (n=9672) ranged from 1.5 to 14.2 cm (total length, mean=4.5 cm; SD=2.5 cm), and from 0.02 g to 23.09 g (total weight, mean=0.03g; SD=1.0 g).
Figure 2a shows the weight-length relationship (W=0.00558 L^{3.113}) for the complete data set (gray dots), as well as the average weight by average length by size class (black dots). Weight standard deviation by size class shows a typical power function pattern (Wsd = 0.00280 L^{2.198}; Fig. 2b), which was used to correct the heteroscedastic pattern to obtain a homoscedastic residual distribution.

Residual distribution from a regular weight-length relationship is presented in Fig. 2c. Although no pattern was detected when analyzing the entire data set (gray dots), a clear trend was apparent for the average weight to average length by size class (black dots) which can be described as an empirical polynomial function (R = 0.0026x^4 - 0.0825x^3 + 0.895x^2 - 3.903x + 5.753; R^2=0.589), with notable anomaly regarding animals longer than 10 cm.

By applying a polyphasic model according to Bervian et al. (2006) the growth of A. brasiliensis could be divided into two stanzas (Fig 3a):

- **Switch-Function:** SW = \[1 + e^{1.204(x - 11.66)}\]^{-1}
- **Stanza 1:** \(W_1 = SW \cdot (0.005239 L^{3.152})\)
- **Stanza 2:** \(W_2 = (1 - SW) \cdot (0.000699 L^{3.913})\)

\(W = W_1 + W_2\)

After adjusting the polyphasic model, no residual pattern could be identified (Fig. 3b; R^2=0.00002), indicating that the polyphasic growth model accounted for all of the potentially explained weight variance.

Figure 4 shows the size distribution of A. brasiliensis in the Estuarine Complex of Paranaguá (grouped bimonthly to increase data consistency). The first sampling period (Aug-Sep/2010) was characterized by a modal group in which most individuals were larger than 7 cm (mean Lt = 9.5 ± 1.86 cm), the smallest mature female reported by Bervian and Fontoura (1997), and comprise basically an adult age-group. In the Oct-Nov sample, newborn juveniles with a size range of 2-3 cm appeared and were present throughout the year, although with decreasing abundance, indicating a long recruitment period with increased intensity in October/November. Trend lines are presented in Fig. 4 to suggest modal displacement within the annual cycle.

Figure 5 graphs the length of all collected specimens (open dots), month by month for the entire year, with individual age assessed by the length frequency distribution. It also presents the median total length of specimens of the same age (black squares) and the predicted growth curve following von Bertalanfly’s model. Estimated growth parameters are presented in Table II. Longevity (A_{95}) was estimated to be 3.3 years.

Latitudinal patterns in relation to growth and mortality parameters were evaluated by using linear regression, but with no identifiable trends (P>0.05).
As observed in the present study, most existing analyses of growth patterns of *A. brasiliensis* (Table I) indicate a positive allometric growth, except for the analyses by Macieira and Joyeux (2008), and Costa et al. (2013). As a general trend, a positive allometric growth can be expected for most fish species (Froese 2006, Froese et al. 2014). Animals of all sizes were captured throughout the year, suggesting that the species completes its ontogenetic development in the shallow waters of the study area. The occurrence of all ontogenetic phases of *A. brasiliensis* in intertidal zones was also observed by Favero and Dias (2015).

An in-depth review (Froese 2006) on the weight-length relationship of fish, and a meta-analysis using Bayesian statistics (Froese et al. 2014) identified general trends of the weight-length relationship according to body shape. As a general approach they suggested to use Log_{10} transformed data to linearize the power function of the weight-length relationship.

Both papers, together with the review of Le Cren (1951), are landmarks in the weight-length literature, describing research history, clarifying
**Figure 5** - *Atherinella brasiliensis* in the Estuarine Complex of Paranaguá, Brazil. Growth curve according to the von Bertalanffy growth model.

\[
L_t = 17.45 \left(1-e^{-0.890(t+0.060)}\right)
\]

**Figure 6** - Bias resulting from adjusting a power function from log-transformed data: a) an artificial data series using the simple power function: \(Y = 1 \cdot X^1\), with homoscedastic variability (\(Y\pm1\)). The trend line represents the fitted model after log-transformation. b) Same data series of Fig. 5a on a log scale. The trend line represents linear regression.
concepts, suggesting approaches, and, importantly proposing general trends concerning fish biology.

Nevertheless, the problems associated with log-transformations to cope with power functions has been pointed out by Smith (1993), and are highlighted in Figure 6. For Fig. 6a, an artificial data series was created using the simple power function: $Y = 1. X^1$. We also introduced homoscedastic variability ($Y \pm 1$) to simulate “real” world data. If a power function is adjusted using standard statistical packages (log-transformation routines), the result is far from $a=1$ and $b=1$. In this case, $a$ was underestimated to 0.899 and $b$ overestimated to 1.05, i.e. a pure isometric data set was estimated as with positive allometry.

Fig. 6b explains the reason for these biases. When values are compressed, lower values undergo less compression than higher values. This is problematic in two ways. Any regression is a balance around a theoretical axis centered between average $Y$ and $X$ values. By compressing $X$ values, the center of balance is downgraded to smaller $X$ values, decreasing the number of individuals below $X$ average. But the major problem is related to the compression of $Y$ values. For each set of values, the $Y$ values above the trend line will be more compressed than $Y$ values below the trend line, and this is especially true for small animals. This unbalanced treatment of $Y$ values will lower the trend line for small animals, underestimating presumed weight, and increase the weight of large animals, overestimating their presumed weight.

As a mathematical “trap”, the trend line rotates counter-clockwise, decreasing the proportionality coefficient ($a$) and increasing the allometric coefficient ($b$). This second problem occurs especially with small samples and large weight variability.

Of course, these biases are amplified in the present simulation due to artificially increased variability for small animals. Fortunately, with real fish data, this is less of a problem since absolute variability of small animals is usually narrow (see Fig. 7). Here, we used variability that was more similar to real data (heterocedastic; $Y \pm Y/10$). In this case, $\log_{10}$ transformation brings the data to a homoscedastic pattern, although with an unbalanced compression of $Y$ values above and below the adjusted trend line. In this simulation, however, the estimated allometry ($b$ value) is correctly estimated as 1.0, although with some distortion concerning proportionality (0.9967 instead of 1.0), but with no practical implication.

By using the entire data set of *A. brasiliensis* and by fitting a regular weight-length relationship with non-linear adjustment, our estimate for $b$ was 3.136, and was very similar when log-transformed data ($b=3.139$) were used, with no practical difference regarding proportionality. If the general recommendations of Froese (2006) are followed with good quality data, bias should be minimal.

Thus, although we argue that nonlinear algorithms are, in theory, better tools for the adjustment of weight-length relationships, the application of linear regression to log-transformed data is sufficient for general use. In particular, the allometry coefficient appears not to be severely compromised by data transformation and the general patterns described by Froese et al. (2014) are probably very close to real patterns.

With regard to the polyphasic weight-length relationship, our intention was to supply information that can elucidate details of the species’ life-history instead of simply describing a useful tool for fishery management. The objective is not the weight-length relationship itself, but to use weight-length information to examine the species’ biology.

For *A. brasiliensis* the weight-length relationship can be divided in two stanzas. The first stanza, with $b=3.152$, describes the weight-length relationship of animals up to 11.66 cm. Above this size, the $b$ value increases to 3.152. The transition from the first to the second stanza is achieved by
a switch function at a relatively slow rate (1.204) with no strong disruption of the growth pattern. The side effect is that the proportionality and allometry coefficients of the second stanza are mathematical artifacts, resulting from the “tail” of the first stanza (Fig. 3a).

Although this general methodology is an interesting tool to describe the growth pattern for each specific stanza, as in Bervian et al. (2006), Fontoura et al. (2010) and Oliveira et al. (2011), it sets the potential trap of achieving a good statistical result with little biological meaning. But the benefit of this approach does not lie in the stanzas themselves, but in identifying the breakpoint between stanzas, that could indicate an interesting shift in the species’ life-cycle. Concerning *A. brasiliensis*, the breakpoint (11.6) is the size estimated by Fávaro et al. (2003) for 100% of the females at sexual maturity in the Paranaguá estuary. While this information is already available, the key point here is to identify whether the reproductive cycle is imprinted in the growth patterns of fish (Bervian et al. 2006, Fontoura et al. 2010, Oliveira et al. 2011).

The adjusted von Berfalanffy growth model ($L_\infty = 17.45$; $K = 0.89$; Paraguá; $25^\circ S$) was

---

**Figure 7** - Bias resulting from adjusting a power function from log-transformed data: **a)** an artificial data series using the simple power function: $Y = 1 \cdot X^1$, with heteroscedastic variability ($Y \pm Y/10$). The trend line represents the fitted model after log-transformation. **b)** Same data series of Fig. 6a on a log scale. The trend line represents linear regression.
similar to estimated models published by Bervian and Fontoura (2007; Females: L<sub>∞</sub>=17.0; K=0.825; Males: L<sub>∞</sub>=16.0; K=0.884; Tramandaí; 29°S) and the FishBase life history tool (L<sub>∞</sub>=17.0; K=0.83). On the other hand, Pessanha and Araújo (2001; Sepetiba Bay, 23°S) estimated a larger growth constant (K=0.93) but a smaller asymptotic length (L<sub>∞</sub> = 11.26), resulting in a reduced growth pattern (Fig. 8).

Although a smaller total size is expected for lower latitudes as described by Taylor (1958, 1959, 1960, 1962), latitudinal differences did not explain the identified pattern. The length-frequency data of Pessanha and Araújo (2001) indicates that very few animals were captured with total length > 10 cm (the largest animal was 13.8 cm). Also, there is a difference in sampling methods: the present work and Bervian and Fontoura (2007) used a 15 m long beach seine net, while Pessanha and Araújo (2001) used a 10 m long seine net. Although the escape capacity of larger animals is unknown, the lack of larger animals in Sepetiba bay may be due to sampling bias, since animals up to 16 cm length have been reported for the same latitude (Costa et al. 2013).

An estimated life span of 3.3 years is very similar to the one proposed by Bervian and Fontoura (2007; Males; A<sub>95</sub>=3.4; Females; A<sub>95</sub>=3.6) and that of the FishBase Life history tool (3.4 years). Nevertheless, very few individuals in a size compatible with a two year old fish (≈14 cm) and none with size in size predicted for three year old fish (≈16 cm) were captured, although animals of this size have been reported in literature (Table I). Especially, no animal was captured with lengths larger than 12 cm after April, suggesting that a displacement of large animals to deeper waters may be happening.

Considering that ten different estimates of the weight-length relationship of <i>A. brasiliensis</i> are available (Table I), we also intended to test the hypothesis of a latitudinal trend concerning proportionality and allometry coefficients, as expected for maximum length (Taylor 1958, 1959, 1960, 1962). Nevertheless, no trend was identified,
possibly due to a nonexisting trend or to poor data quality.

Finally, growth studies of fish species are still needed, since growth parameters for most species are unknown. Also, a meta-analytical approach is highly recommended to summarize growth patterns in relation to environmental gradients (Taylor 1958, 1959, 1960, 1962, Pauly 1980), body shape (Froese et al. 2014) and phylogenetic driving forces (Rodrigues et al. 2014).

ACKNOWLEDGMENTS

The authors would like to thank Coordenação de Aperfeiçoamento de Pessoal de Nível Superior (CAPES) for the scholarship awarded to Barbara Maichak de Carvalho and José Ricardo de S. Barradas (M.Sc and PhD scholarships) and Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq) for the scholarship awarded to Nelson Ferreira Fontoura (research scholarship).

REFERENCES


