Finite element modelling of cornea mechanics: a review

Modelagem de elementos finitos da mecânica da córnea: uma revisão

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ABSTRACT
The cornea is a transparent tissue in front of the eye that refracts light and facilitates vision. A slight change in the geometry of the cornea remarkably affects the optical power. Because of this sensitivity, biomechanical study of the cornea can reveal much about its performance and function. In vivo and in vitro studies have been conducted to investigate the mechanics of the cornea and determine its characteristics. Numerical techniques such as the finite element method (FEM) have been extensively implemented as effective and noninvasive methods for analyzing corneal mechanics and possible disorders. This article reviews the use of FEM for assessing the mechanical behavior of the cornea. Different applications of FEM in corneal disease studies, surgical predictions, impact simulations, and clinical applications have been reviewed. Some suggestions for the future of this type of modeling in the area of corneal mechanics are also discussed.

Keywords: Finite element analysis, Cornea/physiology, Cornea/ultrastructure, Cornea/surgery, Biomechanics/methods, Models, biological

RESUMO
A córnea é um tecido transparente na parte frontal do olho, que refrata a luz e torna a visão possível. Uma ligeira alteração na geometria da córnea notavelmente afeta a sua potência óptica. Devido a essa sensibilidade, o estudo biomecânico da córnea pode revelar muito sobre o seu desempenho e funcionalidade. Estudos in vivo e in vitro foram realizados para investigar a mecânica da córnea e para determinar suas características. Técnicas numéricas como o método dos elementos finitos (FEM) foram amplamente implementadas como métodos eficazes e não invasivos de análise mecânica da córnea e seus possíveis transtornos. Este artigo analisa o uso de FEM para avaliar o comportamento mecânico da córnea. Diferentes aplicações da FEM no estudo de doenças da córnea, previsões cirúrgicas, simulações de impacto e aplicações clínicas foram revisadas. São discutidas algumas sugestões para o futuro deste tipo de modelagem na área de mecânica de córnea.

Descritores: Análise de elementos finitos; Córnea/fisiologia; Córnea/ultraestrutura; Córnea/cirurgia; Biomecânica/métodos; Modelos biológicos

INTRODUCTION
The cornea is the transparent, anterior part of the eye that refracts light onto the lens and is essential to vision. The curvature and thickness of the cornea play an important role in focusing the light to the lens; therefore, they are largely responsible for its optical powers.

In humans and many other mammals, the cornea consists of five layers: the epithelium, Bowman’s membrane, the stroma, Descemet’s membrane, and the endothelium. Of these, the middle layer, the stroma, accounts for 90% of the corneal thickness in humans and is the major layer contributing to the mechanical strength and stiffness of the cornea.

The stroma is a composite material comprising matrix embedded with a complex network of collagen fibrils. The matrix is a viscoelastic and nearly incompressible material. The collagen fibrils are bundled together to form fibers, which are stacked in parallel layers called lamellae. In the human cornea, the stroma consists of approximately 300 lamellae at the center and approximately 500 lamellae at the limbus. The fibers reinforce the tissue and give it mechanical strength along their orientation. The arrangement of collagen fibrils is important to determine the mechanical strength of the cornea. X-ray scatter intensity distribution data has indicated two preferred orientations at points called nodes. The nodes and elements create a network approximately two-thirds of the fibrils are preferentially oriented in the cornea, with the remaining third exhibiting a more or less random orientation. This arrangement of collagen fibrils results in anisotropy of the corneal material.

Biomechanical experiments on corneal tissue have been performed in both in vitro and in vivo studies. Recently, the use of computational models based on the finite element method has proven to be an effective way for studying corneal mechanics and related diseases. These models have been successful in predicting the pre- and postoperative response to eye surgery for myopia, hyperopia, astigmatism, and keratoconus.

The finite element method (FEM) is a numerical technique to obtain approximate solutions for partial differential equations involving physical, thermal, chemical, and other phenomena. Generally, these differential equations are impossible to solve analytically because of the complex geometries and properties of the materials. The approach for solving the equations is to simplify the form of the equation using simple interpolation functions and integrate the entire solution to obtain the final results. This method is very useful for solving problems involving complex material properties and irregular geometries.

To conduct a finite element analysis (FEA), a given body or system is divided into small units called elements, which are interconnected at points called nodes. The nodes and elements create a network...
referred to as a mesh. Each element is assigned specific material and structural properties and the body is analyzed under certain boundary conditions. These boundary conditions can include forces, displacements, and temperatures. The analyzed solution of each element is assembled together to give the global response of the system. The accuracy of this method, in general, depends upon the number of elements used for analysis. A larger number leads to a more precise solution. However, over-refinement of the mesh can lead to longer computational time and memory use in the computer. The element shape and type also play an important role in the accuracy of analysis.

The focus of this article will be the use of FEA for mechanical analysis of the cornea. We will review how this method has been applied to examine the cornea under different loads such as intraocular pressure (IOP), impact from a foreign object, or incisions. The method can also be used to examine how the shape is affected by changes in material properties, such as those occurring during keratococcus. It is worth mentioning briefly, though, that the method can be applied to a wide variety of problems. It has been used to study thermal, electrical, and other physical responses as well as ionic transport. Shafahi and Vafai (17) used a thermal finite element model of the eye to study its response to thermal disturbances. Papaioannou and Samaras (18) used a rabbit eye model to simulate the temperature distribution and velocity field generated under exposure to millimeter wave radiation. Jo and Aksan (19) performed a simulation of conductive keratoplasty, a thermal treatment for hyperopia and presbyopia, to predict thermal damage to the corneal tissue. Mandel et al. (20) used a three-dimensional corneal model exposed to an electrical field to evaluate the electrical properties of the endothelial layer. Guimera et al. (21) also developed a noninvasive FEM to predict the electrical properties of the endothelium and study variations in epithelial permeability. Li and Pinsky (22) created a multiphase mathematical model describing the transport of ionic solution and ionic species in human corneal tissue. We refer the reader to those papers and references therein for further details on these topics of study.

Section 2 discusses the modeling assumptions made in many finite element models of the cornea. The purpose of this section is to give modelers an understanding of the different assumptions that have been used, so that they may choose an appropriate model for their application of interest. Section 3 discusses different applications in corneal mechanics. Finite elements have been used to model the response to corneal surgery, disease, and treatments such as collagen cross-linking (CXL); trauma; and basic research applications. Section 4 summarizes the work and gives some suggestions on the future of such modeling in the practice of ophthalmology and eye research.

**Modeling basics**

The structural model of the cornea can be approached by creating a continuum model or shell model. Continuum models explicitly model the geometry of the cornea in three dimensions, although two-dimensional (2D) approximations are sometimes used. Shell-based models use the theory of thin shell behavior to decrease the geometrical complexity. The modeled geometry is a surface, with the thickness of the shell as a defined parameter. Tensile and bending loads on the shell create deformations in the shell in accordance with shell theory. While this approach decreases geometrical complexity and increases efficiency of the formulation, it is difficult to extend to complex constitutive models. Anderson et al. (23) proposed a corneal model by using shell analysis to develop a nonlinear finite element model to study the mechanical behavior of the cornea. Howland et al. (24), Pinsky and Datye (25), Li and Tighe (26), and Elsheikh and Wang (27) also based their models on this method.

**Geometry**

The structure of the human cornea has a nonuniform curvature with variable thickness throughout (28). It is thinner at the center and thickens towards the edges. Dubbelman et al. (29) recorded the corneal geometry for the internal and external surfaces of the human cornea using Scheimpflug photography. Roy et al. (30) used magnetic resonance imaging to determine the geometric profile of the eye.

Some early models of the cornea, e.g. (29), use a 2D axisymmetric approximation of the cornea. This models the geometry as a surface of revolution and is efficient compared with three-dimensional models (3D). However, it cannot capture the subtle variations in the geometry of the cornea from a surface of revolution, prevalent anisotropies in the material, or any loads that occur off-center, such as an impact or incision. Figure 1 illustrates common shell elements and 3D elements used for FEA of the cornea.

Pandolfi and Holzapfel (2) used the corneal geometry data published by Dubbelman et al. (28) to create biconic interior and exterior surfaces for a 3D corneal model. Pandolfi and Manganiello (31) used an ellipsoidal shape to define the anterior and posterior corneal surfaces. Nguyen et al. (32) and Nguyen and Boyce (33) also approximated the corneal surface to be ellipsoidal according to digital image correlation (DIC) measurements of the corneal surface profile. Buzad (34) and Howland et al. (35) used axisymmetry to create their corneal models.

Salimi et al. (36) meshed the corneal model into triangular shell elements. For 3D models, hexahedral elements are more commonly used (37), although tetrahedral elements may also be used. Linear tetrahedrals and standard trilinear hexahedrals are known to perform poorly for nearly incompressible materials such as soft tissues. Trilinear hexahedral elements can be modified using techniques such as selective reduced integration (38); alternatively, higher order elements may be employed. Figure 2 shows an example of an FE mesh of the cornea.

**Boundary conditions**

The viscous fluid filled inside the anterior chamber of the eye exerts pressure known as IOP on the cornea. Under physiological conditions, the IOP inflates the cornea and gives it shape. A model developed for the cornea using the entire eyeball allows appropriate realistic displacement at the limbus. Uchio et al. (39) and Amini and Barocas (40) modeled the entire eye globe for the analysis. However, the whole eye model may not be efficient because it is highly time consuming and not economical for development and analysis.

![Figure 1. Common shell and solid elements used for finite element analysis (FEA) of the cornea. A) Triangle and B) quadrilateral are common shell elements. Each shell element node has 5 degrees of freedom (DOF): 3 translational and 2 rotations (approximately 2 orthogonal axes on the shell surface). C) Tetrahedral and D) hexahedral are common 3D elements. Each element node has 3 translational DOF.](image-url)
Alastrue et al.\textsuperscript{(10)} analyzed the corneal model with the limbus constrained against displacement. Anderson et al.\textsuperscript{(23)} compared the deformation pattern of the entire eye model to the rigid cornea-limbus boundary. They proposed an approximate boundary condition, with roller support at the edges inclined at 40° with respect to the horizontal axis, to represent the cornea-limbus behavior. The results obtained from their boundary assumption were similar to the results obtained for the whole eye. Other studies\textsuperscript{(11,13,14,19)} adopted similar boundary conditions for their corneal models. Roy et al.\textsuperscript{(14)} created the whole eye model and compared the displacement results with those for the corneal model with fixed sclera to show that the corneoscleral limbus plays an important part in predicting the response to refractive surgery. Pandolfi and Holzapfel\textsuperscript{(2)} proposed a corneal model allowing rotation at the limbus and restricting displacement at the edges. Rotation at the limbus plays a role in changing the curvature of the cornea. Figure 3 illustrates these boundary conditions.

Figure 2. An example of a finite element (FE) mesh of the cornea using hexahedral elements.

Figure 3. Schematic of boundary conditions at the limbus used by researchers. A) The cornea is constrained against displacement and rotation, as proposed in\textsuperscript{(10)} B) The cornea is fixed against displacement, but may rotate at the edges, as in\textsuperscript{(17,18)} C) Springs normal to the cross-section. Researchers in\textsuperscript{(13,19)} investigated boundary conditions (a), (b), and (c). D) The cornea is allowed to expand along a given surface, as in\textsuperscript{(26,27,41)} Forty degrees from horizontal is taken as a typical angle.

Figure 4. An example of vertical displacement mapping of a mouse cornea subjected to intraocular pressure (IOP) obtained from finite element (FE) simulations is shown in the cross-section. The wireframe on the bottom is the undeformed mesh, and vertical displacement colored by magnitude is shown on top. The corneal displacement, but not rotation, is restricted along the limbus.

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an FEM to find a set of optimal parameters for a given model to be used in the FE simulation. Such methods are important for determining the physical properties of actual corneas.

Nguyen and Boyce(31) presented an inverse FEM to estimate bovine corneal material properties using an in vitro inflation experiment and investigate the influence of variations in these properties on the bovine inflation response. They determined a set of anisotropic material properties, minimizing the error between simulation results and experimental measurements of the surface displacement field.

**Summary of finite element modeling choices**

Different choices in finite element models of the cornea can change the results. 2D or shell models are efficient, but they may not be able to accurately capture the complex material behavior of some applications. While modeling the entire eye may avoid approximate boundary conditions at the limbus, the computational time increases significantly. However, modeling the changes in IOP during an impact may be difficult without a full model of the eye.

Material models are also increasingly accurate and, at the same time, computationally more expensive. While linear models are very efficient, they may be inaccurate over large changes in deformation. Isotropic models may not accurately capture the behavior of the complex material in the stroma, but they may be adequate for problems that only require a rough idea of the displacements. The depth of knowledge of the properties of corneal tissue is improving. In applications with rapid load, the viscoelastic and dynamic properties of the cornea may be important. For other analyses, such as those of the long-term results of surgery, a quasistatic model is acceptable. It is important to select a model that can simulate an application with the necessary accuracy. However, a model with too much detail may computationally become very expensive.

**APPLICATIONS**

FEA is a useful tool for studying corneal mechanical behavior and the mechanisms underlying its functions. FEA has been widely used for modeling surgical effects on the cornea and for studying corneal diseases and eye trauma. In this section, different applications of FEA in simulation of corneal surgery, disorder, and impact, among others, are discussed.

**Surgery**

The curvature of the internal and external surfaces of the cornea significantly affect its refractive power. Refractive eye surgery can improve the visual acuity in patients with common refractive maladies such as astigmatism, hyperopia, and myopia. In several surgical techniques, the dioptric power of the cornea is improved by removing thin layers of biological tissues and adjusting the curvature of the cornea using excimer lasers(13). Laser-assisted in-situ keratomileusis (LASIK), photorefractive keratectomy (PRK), and intrastromal photo-refractive keratectomy (ISPRK) are the 3 main types of refractive surgeries on the periphery of the cornea, such as keratoconic keratoplasty (CK) and intracorneal rings (ICR), have recently attracted more interest. These surgeries are primarily performed on hyperopic eyes that require steepening rather than flattening of the corneal surface(38).

FEA has potential usefulness as a simulation tool for refractive surgery planning using accurate in vivo corneal material properties and geometry data(14). FEA has been extensively used to model deformation of the cornea for corneal surgery simulation and predict mechanical and refractive effects of surgery(24).

Pandolfi et al.(14) implemented an FEM in astigmatic and myopic corneas to evaluate the mechanical and refractive outcomes of laser refractive surgery. They computed the change in the curvature and thickness of the human cornea exposed to laser ablation and evaluated the corrected dioptric power in individual patients.

Roy et al.(14) proposed an FE model of the whole eye to give insight into refractive surgery planning. They later presented an inverse FEM to determine the undeformed state of the cornea(36). They also developed a 3D, patient-specific, corneoscleral FEM model to estimate the surgical impact on corneal shape variations and changes in corneal elastic properties.

Niroomandi et al.(43) presented a novel numerical technique for actual surgery simulation using an extended FEM (X-FEM). The X-FEM enhances standard FE by defining additional degrees of freedom, in this case, for fracture opening (those interested in further theory of the X-FEM can refer to the work of Belytschko et al.(52), among others). In their model, fracture opening induced by the incision placed during refractive surgery was reproduced using the X-FEM method. Their presented FEM was able to simulate the complex constitutive model of the cornea and reproduce the discontinuities of the scalpel incision for actual surgery simulations.

Nomograms in ophthalmology are sets of tables of corrected values or graphics used to plan the surgical procedure, particularly incisional surgeries for astigmatism and similar diseases(49). Nomograms can manage the incision effect by revising the cut parameters such as depth, length, and optical zone in incisional surgery. Cristóbal et al.(40) proposed an FE model of a limbal incision to predict patient-specific optical power that can be induced during surgery. The nomogram outcomes were compared to simulation results, and, in some cases, the nomograms were revised accordingly.

CXL is a subablative thermal treatment wherein thin electrodes are inserted into the stroma to apply radiofrequency (RF) heating. The heat causes the peripheral corneal tissue to shrink. Jo et al.(10) developed a 3D FE model, including the cornea, aqueous humor, and RF electrodes, to investigate the resultant thermal damage during RF heating in the CK procedure. Fraldi et al.(20) also presented a viscoelastic FEA to study the mechanical response of the hyperopic cornea to CK and assess the postsurgical stability of the applied refractive correction. Hameed et al.(25) created a 3D FE model to simulate the ISPRK technique for correcting myopic corneas and predicting treatment outcomes. The simulation outcomes were compared with the results from an earlier 2D FE model developed by Bryant et al.(62) for the same purpose. The model outputs were more strongly correlated with the clinical data when the 3D model was used than when the 2-D model was used.

**Corneal diseases**

Finite element analysis has been widely used to study biomechanical interactions in corneal maladies (e.g. keratoconus) and better understand the etiology and treatment of the diseases. FEM can be used to investigate the effects of variations in corneal material properties on vision power in patients with corneal diseases.

Keratoconus is a degenerative corneal disease characterized by irregular thinning and bulging of the corneal structure and progressive topographic irregularities in the cornea. This shape distortion leads to an optical aberation that can be corrected with the use of hard contact lenses or glasses in mild cases or corneal transplantation in more severe cases(15). CXL is a new method for treating keratoconus. In this technique, the epithelium is usually removed from the central zone of the cornea, and riboflavin is absorbed into the stroma(16). Under ultraviolet (UV) radiation, the riboflavin creates additional cross-linking in the collagen fibrils, stiffening the cornea.

Gefen et al.(12) presented a 3D linear anisotropic FE model of normal and keratoconic corneas to investigate the mechanical behavior and optical performance. The results of analysis revealed that IOP had a considerable influence on the optical power of the keratoconic cornea, while having little effect on the refractive power of the normal cornea. Roy et al.(18) presented a 3D patient-specific FE model of the whole eye to study keratoconus progression. The model was able to demonstrate a patient-specific procedure for investigating
the locally decreased corneal elastic properties during keratoconus development.

Carvalho et al. presented a FEM of a keratoconic cornea to predict the biomechanical behavior and evolution of the cornea in keratoconus. Using shell elements, they investigated how variations in IOP and material properties of the cornea (i.e., decrease in rigidity of the cornea) can lead to a localized increase in corneal curvature. Foster et al. examined the stiffening effect of CXL in corneal tissue, fitting the material parameters to experiments on corneal strips.

**IMPACT AND TRAUMA**

Ocular trauma can cause long-term vision disorders and can be expensive to treat. FEM is a useful tool for simulating ocular trauma. It may offer possible solutions for decreasing eye impact injuries and designing protective tools against globe trauma. The impact of different projectiles on the eye has been simulated using FEA to investigate the injury potential.

Stitzel et al. offered a nonlinear FEM of the human eye to predict eye rupture injuries caused by high-speed blunt impact. The numerical model was verified with experiments to predict the injury due to different types of impacting projectiles and loading conditions.

Weaver et al. implemented a numerical model of eye impact that considered a variety of blunt projectiles and loading conditions and was based on many experimental impact tests. They investigated the effects of different projectile mass, size, material properties, and velocity on the response of the eye to impact. The study results gave insights for predicting eye rupture in various loading conditions and designing eye safety equipment.

Gray et al. studied the impact of paintballs on the cornea, with the aim of designing safer paintballs. To this end, they implemented a numerical model of the human eye, orbit, and paintball into the CTH computer code (a 3D, finite-volume, and large deformation numerical hydrocode developed by Sandia National Laboratory) to study the physical mechanisms causing impact eye injuries. By varying material properties, they concluded that paintballs with less mass can be safer for the eye.

Uchio et al. also presented a 3D FEA supercomputer simulation of traumatic impacts on the eyeball. They investigated the threshold of impact eye injuries caused by bodies of different sizes and velocities.

**OTHER APPLICATIONS**

FEM can be used as a potential noninvasive tool in clinical applications for investigating the biomechanical behavior of the cornea and obtaining characteristic measurements of the tissue. FEM may be a critical method for assessing corneal mechanical and electrical properties and for obtaining IOP measurements.

Applanation tonometry is among the most widely used contact tonometry techniques for IOP measurement. FEM has been used to examine applanation tonometry for measuring IOP. Ghaboussi et al. developed a computationally efficient numerical method to accurately measure IOP in the cornea using a modified applanation tonometer. They used the combination of a neural network and genetic algorithm to fit clinical applanation tonometry outcomes (force and displacement history data) to the outcomes achieved from the FE model.

As the heart beats, IOP behind the cornea changes; the vibration characteristics of the eye also vary with IOP. Salimi et al. developed a coupled fluid-structure FEM of the eye and investigated the dynamic response of the eye to changing IOPs. They validated the vibrational characteristics from the simulation model with experimental modal analysis (EMA) of a water-filled spherical shell.

Rhee et al. developed a nonlinear, anisotropic FE model of the mouse cornea to study the formation of spiral patterns on the epithelium. They compared the obtained numerical curves of maximum shear strain with actual spiral patterns observed on X-ray images of mouse cornea. The presented work helped in providing insight into the possible development of the cornea.

**CONCLUSIONS**

FEA is a powerful numerical technique for finding approximate solutions to partial differential equations in complex structures. FEA may be used to simulate a wide range of biological structures and body organs. In this work, the different applications of FEA in studying mechanical behavior of the cornea were reviewed. This review included information about a wide variety of applications, ranging from surgery to disease and impact simulation.

On the basis of the articles reviewed, FEA has been used to develop a better understanding of the mechanics of the cornea in a variety of settings. It can be a noninvasive, predictive method for assessing corneal function and properties and studying related diseases. The FEM models can be used in clinical applications to investigate corneal malfunctions and present possible treatments. FEA can predict the pre- and postoperative responses of the cornea to refractive surgeries and may be used as a patient-specific simulation tool in clinical applications for surgical planning.

In the future, FE models may become important tools for planning treatments. Initially, the models will be used to improve procedural parameters such as incision locations and depths. However, it will soon be possible to provide patient-specific corneal models that can be used to plan individual surgeries and predict outcomes, such as optimal treatment times and concentrations for CXL.

Obtaining the parameters for the stiffness of individual corneas, particularly in vivo, remains a challenge. A combination of investigations of excited corneas and simple tests of in vivo corneas will provide reasonable data to approximate patient-specific corneal properties. Ongoing investigations on the complex mechanical properties of the cornea will continue to create more realistic and accurate models for all these applications.

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