DISCHARGE OF NON-REACTIVE FLUIDS FROM VESSELS

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Abstract – This paper presents simulations of discharges from pressure vessels that consistently account for non-ideal fluid behavior in all the required thermodynamic properties and individually considers all the chemical components present. The underlying assumption is that phase equilibrium occurs instantaneously inside the vessel and, thus, the dynamics of the fluid in the vessel comprises a sequence of equilibrium states. The formulation leads to a system of differential-algebraic equations in which the component mass balances and the energy balance are ordinary differential equations. The algebraic equations account for the phase equilibrium conditions inside the vessel and at the discharge point, and for sound speed calculations. The simulator allows detailed predictions of the condition inside the vessel and at the discharge point as a function of time, including the flow rate and composition of the discharge. The paper presents conceptual applications of the simulator to predict the effect of leaks from vessels containing mixtures of light gases and/or hydrocarbons and comparisons to experimental data.

Keywords: Relief, venting, tank, valve, equation of state.

INTRODUCTION

Discharges of hazardous chemicals can bring about serious consequences to populations living close to industrial units, in addition to financial losses. In some cases, the discharges are accidental, as in the case of leaks. In others, as in operations for pressure relief, they are intentional and aim to prevent further damage, such as the explosion of pressure vessels. In both cases, it is important to predict the flow and composition of the material discharged to the environment in order to plan measures of containment and remediation.

Due to the growing importance of this practical problem, several programs for the simulation of leaks and venting from pressure vessels exist (Woodward and Mudan, 1990; Bendiksen et al., 1991; Haque et al., 1992a, 1992b; Richardson and Saville, 1996; Mahgerefteh and Wong, 1999; Cumber, 2001; Witlox and Bowen, 2002; Renfro et al., 2014; D’Alessandro et al., 2015). In order to simplify the formulation and shorten their execution time, some of them use approximations, such as that of ideal gas behavior, that increase the uncertainty of their predictions. Other papers account for deviations from ideal gas behavior as, for example, those of Haque et al. (1992a, 1992b) and Richardson and Saville (1996), who used a proprietary computer package for physical properties called PREPROP, and of Mahgerefteh and Wong (1999), who used cubic equations of state. Another approximation occasionally used is that the chemical components can be lumped into a single pseudo-component; however, the composition of the vented fluid and of the fluid inside the vessel can vary significantly during a simulated period. These references focus on the so-called source term, which refers to the behavior of the fluid up to the point

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of its release from the vessel. The behavior of the fluid beyond the release point can also be rather complex, as exemplified by the work of Birch et al. (1987), who present correlations to predict how the velocity of the fluid decays as it flows into the atmosphere. Other examples are the work of Winters (2009) and Houf and Winters (2013), who model the flow of hydrogen into ambient air right after leaks from tanks that store liquid hydrogen at very low temperatures. An interesting aspect of these publications is the rigorous modeling of physical properties using the REFPROP (Lemmon et al., 2007) thermodynamics suite of flash algorithms.

Renfro et al. (2014) describe the features of the “Blowdown Utility” program for the simulation of discharges from horizontal or vertical vessels of several geometries. A non-equilibrium vessel model is adopted and the simulator allows the choice of several models for the evaluation of the physical properties of the fluid. Their approach allows the simulation of vessels that contain three fluid phases. However, the article provides no details about the mathematical formulation and an undisclosed expression is used to calculate the flow rate of the leaking fluid.

D’Alessandro et al. (2015) describe a simulator called VBsim (Vessel Blowdown Simulator) that uses global phase stability analysis and minimization of the Gibbs energy to find the conditions inside the vessel. VBsim uses the concept of partial phase equilibrium (Speranza and Terenzi, 2005), according to which the liquid and vapor phases have the same pressure, but not the same temperature, because of their different heat transfer coefficients, which are calculated by the program. In this approach, the liquid phase is in equilibrium with a “bubble” phase while the vapor phase is in equilibrium with a “droplet” phase. Different expressions are adopted for the flow through the vessel’s orifice, depending on whether the discharge is of a liquid or vapor phase. However, their approach seemingly disregards the possibility of phase change at the discharge point.

This paper introduces a simulator for discharges from pressure vessels that accounts for deviations from ideal gas behavior in all the required thermodynamic properties and individually considers all the chemical components present. The formulation follows the so-called homogenous equilibrium assumption, according to which equilibrium is achieved instantaneously and, thus, the dynamics of the fluid in the vessel comprises a sequence of equilibrium states. The underlying mathematical problem is a system of differential-algebraic equations (DAE) in which the component mass balances and the energy balance are ordinary differential equations. The differential energy balance includes the internal energy of the fluid and of the vessel walls. The algebraic equations account for the phase equilibrium conditions inside the vessel and at the discharge point. Due to the size and complexity of the model, numerical solution is necessary.

At each time step during the integration of the ordinary differential equations of the model, the values of the internal energy and component amounts inside the vessel become known. Since the vessel’s volume is known and fixed, the state of the system can be found by maximizing the fluid’s entropy (Callen, 1985). To compute the discharge conditions, the assumption is that the region inside the vessel close to the discharge point acts as an adiabatic converging nozzle whose operation is isentropic. This leads to an unusual equilibrium problem with specification of fluid entropy and stagnation enthalpy (enthalpy plus kinetic energy). The model accounts for the possibility of non-choked and choked flow at the discharge point. In the latter, the fluid speed is equal to the local thermodynamic sound speed. Therefore, a procedure to compute the thermodynamic sound speed in systems with multiple phases is also part of the formulation.

The simulator allows predictions of the conditions inside the vessel and at the discharge point as a function of time, including the flow rate and composition of the discharge, which are crucial pieces of information when planning for emergencies and studying containment alternatives. The paper shows applications of the simulator to predict the effect of leaks from vessels containing light gases and hydrocarbon mixtures.

ASSUMPTIONS

A set of assumptions underlies the development of the mathematical model of leak and vent operations from pressure vessels. A central one is that the fluid inside the vessel is in thermodynamic equilibrium at all times, and that properties such as temperature, pressure, and chemical potential of each component are the same everywhere within the vessel. When the mass and the specific heat capacity of the vessel wall are considered in the simulation, it is assumed that the wall and fluid temperatures are equal at any time. It is also assumed that the volume of the vessel’s wall remains constant, that is, wall expansions or contractions because of temperature changes are neglected. In the absence of chemical reactions, as is the case considered here, this means that determining the state of the fluid within the vessel requires a phase equilibrium computation.

Another key assumption is related to finding the leak or vent flow rate, for which it is necessary to model the region in the vessel near the orifice. As usual in similar simulations, the assumption is that this region is a hypothetical converging nozzle that operates adiabatically and reversibly. As such, the flow in the converging nozzle is taken as isentropic. During leaks from vessels that contain condensed phases, the violent boiling caused by depressurization can swell the liquid phase, i.e., its level may rise because of bubble formation within the liquid. This effect is neglected, under the assumption that there is instantaneous disengagement of the phases present.
With these assumptions, the mathematical model consists of a set of differential-algebraic equations (DAE). The mass and energy balances are ordinary differential equations (ODE). The algebraic equations allow the determination of the state of the fluid inside the vessel and at the exit point at each time step of the numerical ODE integration.

Furthermore, to determine the leak or vent flow rate, it is necessary to find several fluid properties at the fluid’s exit point from the vessel, namely, its temperature, pressure, number of phases with their amounts and compositions, and thermodynamic sound speed. The sound speed is relevant because it is the maximum achievable fluid speed at the exit of a converging nozzle. Flows at sonic speed are referred to as choked and the pressure at the exit point is larger than the backpressure, which is the pressure away from the vessel. Flows below sonic speed are referred to as non-choked and the exit pressure is equal to the backpressure.

**FORMULATION**

The formulation follows the recent work of Kanes et al. (2016). We consider storage vessels with no material input during the simulated time. The number of output streams is arbitrary and user-defined. The possibility of simulating the simultaneous discharge through more than one output stream is useful in situations such as the aperture of a relief valve followed by the opening of a bursting disk. We consider vertical cylindrical vessels; if the phase volumes are known, it is simple to compute the level of the interfaces. By knowing these levels and the shape and position of the orifices, it is possible to determine the leaking phase at any given moment. This may change during the simulation. For example, at the beginning of a simulation, the liquid phase may leak but, as its level decreases, vapor may leave the vessel through the same orifice in later stages of the process. In this paper, we assume that the orifice sizes remain constant during the simulated time.

The first step of the solution procedure is to determine the initial condition of the fluid in the vessel. This is accomplished by solving a flash calculation whose specifications are the fluid temperature, internal volume of the vessel, and amount of each component (Espósito et al., 2000). By minimizing the system’s Helmholtz energy and using global phase stability analysis (Michelsen, 1982), this calculation determines the number of phases present, their volumes, amounts, compositions, and internal energies at the beginning of the simulated process. When the effect of the vessel wall is included in the simulation, determining the initial condition includes the evaluation of the wall’s internal energy, given its mass and specific heat capacity at constant volume.

With the initial state determined, it is possible to start the dynamic simulation of the fluid in the vessel, which requires the solution of a set of differential equations. The differential mass balance of each component \(i\), written on a molar basis, is:

\[
\frac{dn_i}{dt} = \sum_{m=1}^{n_{out}} n_{im}^{out}
\]

In Eq. (1), \(t\) represents time, \(n_i\) is the number of moles of component \(i\) in the vessel, and \(n_{im}^{out}\) is the molar flow rate of component \(i\) in stream \(m\), which is one of the \(n_{out}\) streams that exit the vessel. The energy balance takes the form:

\[
\frac{dU}{dt} = -\sum_{m=1}^{n_{out}} n_{m}^{out} \left( h_{m}^{out} + M_{m}^{out} \left( \frac{u_{m}^{out}}{2} \right)^2 \right) + \dot{Q}
\]

In Eq. (2), \(U\) is the internal energy of the vessel wall (when it is considered) and of the fluid in the vessel, \(\dot{Q}\) is the heat transfer to the fluid in the vessel, and \(h_{m}^{out}\), \(M_{m}^{out}\), and \(u_{m}^{out}\) are the molar enthalpy, molar mass, and average fluid speed at exit point \(m\), respectively. It is necessary to apply a numerical method to integrate the ODE set comprised by Eqs. (1) and (2). In this work, the Bulirsch-Stoer method is used, as implemented by Press et al. (1992). This is a conventional ODE integrator, not an integrator for differential algebraic equations (DAE). There has been no attempt to use a DAE integrator because reliable numerical convergence of phase equilibrium equations (algebraic) often requires highly specialized algorithms. The adopted strategy has been to solve the algebraic equations every time the ODE integrator needs to evaluate the right hand side of the differential mass and energy balances, which are represented by Eqs. (1) and (2), respectively. To compute them, it is necessary to determine the flow rate, composition, average fluid speed, and enthalpy of each stream \(m\) that exits the vessel. All these algebraic calculations consider the possibility of single or multiple phases in the vessel and at the exit point.

The first step to accomplish this is to determine the state of fluid in the vessel. This requires solving a flash problem whose specifications are the current values of internal energy and component amounts, as provided by the ODE integrator, and the vessel’s internal volume, which is constant. Determining the equilibrium condition for this set of specifications requires maximizing the system’s entropy (Callen, 1985). A flash algorithm developed specifically for this situation (Castier, 2009) is used. This
algorithm is extended in this work to account for cases that include the mass and heat capacity of the vessel wall, which is considered as a solid phase that exchanges heat, but neither mass nor volume, with the fluid phases present. The outcomes of this calculation are the fluid and wall temperature and fluid pressure, number of phases present, their densities and volumes, amount of each component in each phase, and the molar enthalpy and entropy of each phase, among other thermodynamic properties. With the calculated phase volumes (and mass densities, to establish their relative positions), it is possible to find the location of the interfaces for a given vessel geometry (vertical cylinder, in this work). The position of each exit point \( m \) is then checked against the interface locations to decide whether each discharge is from a liquid or vapor phase, or both when an orifice is exposed to both phases simultaneously, as discussed by Kanes et al. (2016).

The next step is to model what happens inside the vessel next to each exit point \( m \). The assumptions are that each of these regions behaves as a converging nozzle that operates adiabatically and isentropically and that changes to the nozzle’s input conditions have instantaneous effect on the exit conditions, i.e., mass and energy accumulations in the nozzle are neglected. An additional assumption is that the average fluid speed at the nozzle’s entrance is negligible compared to its value at the exit point. These assumptions lead to the following two algebraic equations, written on a molar basis:

\[
\begin{align*}
    h_{m}^{dch} &= h_{m}^{\text{out}} + M_{m}^{\text{out}} \left( \frac{u_{m}^{\text{out}}}{2} \right)^{2} \\
    s_{m}^{dch} &= s_{m}^{\text{out}}
\end{align*}
\]

(3)

(4)

where the superscript \( dch \) denotes properties of the discharged material inside the vessel, at the entrance of the hypothetical nozzle. It should be noted that the fluid may have one or more phases at an exit point, but this is not known beforehand. In fact, determining the state of a fluid with specifications of fluid composition, entropy, and stagnation enthalpy constitutes an unusual phase equilibrium problem. A new algorithm for this situation has been the focus of recent work (Castier et al., 2016). An important feature of this algorithm is that it begins with the assumption that the pressure at the exit point is equal to the specified value of the backpressure. If it turns out that the flow is supersonic under these considerations, the solution is invalid because the sound speed is the upper limit for flow speed at the exit of an adiabatic converging nozzle. When this happens, the problem is solved again relaxing the pressure specification and considering that the flow is sonic. Thus, the sound speed calculations play an important role on the overall computation path. Very importantly, they are occasionally necessary for systems with more than one phase, if flashing conditions occur at the exit point. Few algorithms exist to this end. A recent procedure for the calculation of thermodynamic sound speed in systems with any number of fluid phases (Castier, 2011) is used in this work. For multiphase systems, this procedure involves the solution of a system of linear equations formulated with the use of derivatives of several thermodynamic properties, phase equilibrium conditions, and conservation equations for volume, entropy, and mole number of each component. Regardless of being sonic or subsonic, the flow rate at the exit point is obtained using:

\[
    n_{m}^{\text{out}} = A_{m}^{\text{out}} \frac{u_{m}^{\text{out}}}{v_{m}^{\text{out}}}
\]

(5)

where \( A_{m}^{\text{out}} \) and \( v_{m}^{\text{out}} \) are the exit area and molar volume at point \( m \), respectively.

In summary, three flash algorithms are necessary as part of these simulations:

- A TVN flash establishes the initial state of the fluid in the vessel for given volume, initial temperature, and initial amounts of each component.
- A UVN flash determines the state of the fluid in the vessel during the dynamic simulation. Its specifications are the current values of \( U \) and \( N \) obtained from the numerical integration of the differential equations and the internal vessel volume, which is constant throughout the simulated period.
- A HSN flash determines the state of the fluid at the leak point, which is assumed to be the exit of a hypothetical converging nozzle. Its specifications are the stagnation enthalpy of the fluid that enters the nozzle, its entropy, and component amounts.

In this work, the Peng-Robinson equation of state (Peng and Robinson, 1976) is used to compute the thermodynamic properties, including the fugacity coefficients, residual internal energy, residual enthalpy, residual entropy, and thermodynamic sound speed, as well as their derivatives, as required by the phase equilibrium calculations. In this sense, the same thermodynamic model is used to evaluate all the thermodynamic properties of the fluid. The critical properties, acentric factor, and coefficients of a 3rd degree polynomial correlation in temperature for the molar ideal gas heat capacities are taken from Reid et al. (1987). Despite the specific modeling choices, it should be noted that the formulation is general and not limited to using the Peng-Robinson equation of state, whose recommended application is for calculations involving hydrocarbon mixtures.
RESULTS

This section shows simulation results of cases in which light gases or hydrocarbons are vented from vertical cylindrical vessels. The possible occurrence of chemical reactions is neglected in all cases.

Discharge of nitrogen or methane

This conceptual case compares the discharge of pure nitrogen or pure methane. The vessel is adiabatic and has a volume of 1.00 m$^3$, with height of 2.00 m and diameter of 0.798 m. A $25.0 \times 10^{-6}$ m$^2$ orifice located 1.00 m above the bottom of the vessel is used (with unity coefficient of discharge). The initial temperature of the fluid in the vessel's interior is 400 K. The vessel load consists of 80.0 moles of nitrogen or methane and the thermal inertia of the vessel walls is neglected. Figure 1 shows how the pressure inside the vessel drops as function of time until it becomes equal to the backpressure, which is specified to be equal to 0.10132 MPa. It is noticeable that the discharge of nitrogen takes longer, which is an outcome associated to the fluid speed at the exit point.

Figure 2 displays the corresponding temperature profile during the simulated period. Methane has larger molar heat capacity than nitrogen and its temperature drop is accordingly smaller.

Figure 3 shows the fluid and sound speeds at the point of discharge. For each compound, these speeds overlap in the beginning of the simulated time, until 38.7 s for methane and 40.5 s for nitrogen, meaning that the exit flow is sonic, i.e., choked. The plot also shows that the discharge speed of pure methane is faster than that of pure nitrogen, justifying the fact that the pressure in the methane vessel becomes equal to the backpressure before this happens in the nitrogen vessel (Fig. 1).

Therefore, these results illustrate how two pure light compounds behave differently during a leak, even though there is only one phase inside the vessel and at the exit point for both of them throughout the simulated period.

Figure 4 shows the effect of increasing the orifice area to $100.0 \times 10^{-6}$ m$^2$, i.e., quadrupling its area compared to the previous situations. As expected, the times needed to equalize the vessel pressure and the backpressure are one-fourth of the times reported in Fig. 1.

Discharge of nitrogen: comparison with Véchot’s (2006) data

Véchot (2006) measured temperature and pressure during the discharge of nitrogen from a $0.0107$ m$^3$ vessel initially at 0.3612 MPa and 293.67 K through an orifice whose area is equal to $1.131 \times 10^{-6}$ m$^2$. To match these specifications, the initial amount of nitrogen in the simulation is equal to 1.586 moles of nitrogen.

For an adiabatic vessel of negligible heat capacity compared to the heat capacity of the fluid it contains, the
fluid temperature would decrease from the beginning until
the end of the experiment. The experimental data show
that there is a minimum in temperature equal to 274.73
K at 58 s. The nitrogen temperature increases after that,
indicating that there is heat transfer to the fluid in the
vessel, either from outside the system or from the vessel’s
construction material. As Véchot (2006) did not report the
mass and material of construction of the vessel, this effect
was simulated by imposing a constant heat transfer rate to
the fluid (equal to 41 J/s) so that the simulated temperature
exhibits the same minimum value, which occurs at 28.9 s of
simulated time. The ratio of the simulated and experimental
times for the minimum in temperature, equal to 0.50, was
interpreted as a practical coefficient of discharge for this
venting process, which is lower than the typical value of
0.61 for discharges through orifices.

Figures 5 and 6 display the pressure and temperature
profiles. There is only one phase within the vessel during the
simulated period. The experimental data are plotted against
the measured time. The calculated data are plotted against
a rescaled time equal to the simulated time divided by the
coefficient of discharge of 0.50. The plots end at 58 s, when
the minimum in temperature occurs. The experimental
and calculated results are in acceptable agreement during
this period. Beyond it, the disagreement between the two
results increases, especially for temperature, because of the
adopted approximation of constant heat transfer rate.

Discharge of nitrogen: comparison with Haque et al.’s
(1992b) data

Haque et al. (1992b) measured the gas temperature,
wall temperature, and pressure during the discharge of
nitrogen, initially at 15.0 MPa and 290 K, from a vessel
of undisclosed construction and insulating (if any)
materials. Haque et al. (1992b) report the following vessel
dimensions: height of 1.524 m, internal diameter of 0.273
m, wall thickness of 0.025 m, with a circular orifice whose
diameter is 0.00635 m, positioned at the top of the vessel.
Using these dimensions and assuming that the vessel is
of stainless steel 316, whose density was taken as equal
to 7950 kg/m³ (British Stainless Steel Association, 2016),
the vessel’s mass was estimated to be equal to 316.1 kg.
To match the problem specifications, the initial amount of
nitrogen in the simulation is equal to 557.3 moles, which
corresponds to 15.60 kg. Thus, under these assumptions,
the initial mass of nitrogen is just 4.7% of the total mass of
the system. The vessel is considered as adiabatic and the
internal energy of the solid is considered in the simulation,
with the specific heat capacity of steel at constant volume
calculated using the following third degree polynomial in
temperature (in Kelvin):

\[
C_v \left( \frac{J}{\text{kg} \cdot K} \right) = 174.59 + 1.3837T - 1.7172 \times 10^{-3}T^2 + 7.6188 \times 10^{-7}T^3
\]  

This expression fits experimental data (British Stainless
Steel Association, 2016) between 293.15 K to 1143.15 K
with an absolute average relative deviation of 0.30%.

Figures 7 displays the experimental pressure data as
obtained from the graphical results of Haque et al. (1992b)
and plotted against time until the end of the experiment, at
100 s. It also shows the calculated results plotted against
a rescaled time, which is the simulation time divided by

![Figure 4. Pressure in vessels loaded with either pure nitrogen or
pure methane: effect of larger orifice.](image-url)

![Figure 5. Pressure in a vessel loaded with nitrogen: comparison of
experimental (Véchot, 2006) and calculated values.](image-url)
a coefficient of discharge of 0.70, in such a way that the final rescaled time at the end of the run is also equal to 100 seconds. At this condition, the simulated pressure inside the vessel becomes equal to the atmospheric pressure. The model overestimates the pressure at 10 s and 20 s, but there is good agreement between the experimental and calculated pressures at later times.

Concerning temperature, the experimental data of Haque et al. (1992b) show that the fluid temperature passes through a minimum, of about 190 K, and then increases, reaching a temperature of about 220 K at the end of the experiment. A possible explanation for this behavior is heat transfer from the vessel walls to the fluid, countering the temperature drop caused by depressurization. The experimental value of the wall temperature drops throughout the experiment, reaching a final value of about 285 K. As the model assumes a single temperature for the whole system, it cannot predict different temperatures for the fluid and for the wall. The simulated temperature results show a steady decrease in temperature from the initial temperature of 290 K to a final temperature of 279.6 K. This shows that the thermal inertia of the vessel wall, whose mass is about 20 times the mass of nitrogen, dominates the model’s temperature prediction. Thus, the temperature from the simulation is between the experimental fluid and wall temperatures, but closer to the latter because of the large heat capacity of the vessel wall.

**Discharge of nitrogen+methane mixture from heated vessel**

This conceptual case considers the discharge of an equimolar mixture of nitrogen and methane from a vessel of the same size and shape as that of case 4.1, with the binary interaction parameter of the Peng-Robinson EOS set to 0.1 (Firoozabadi, 1999). The vessel initially contains 40 moles of each compound at the temperature of 400 K. There is heat transfer to the fluid in the vessel at a rate of 1000 J/s. The vessel is initially closed and a relief valve (25.0x10−6 m², located 1.0 m above the bottom) opens when the pressure reaches 0.35 MPa. A bursting disk (100.0x10−6 m², located 1.5 m above the bottom) opens when the pressure reaches 0.40 MPa. Unity coefficient of discharge were used for the relief valve and bursting disk.

Figure 8 displays the pressure as a function of time. The pressure initially increases because the vessel is closed and there is heat transfer to the fluid. When the pressure reaches 0.35 MPa, the relief valve opens. The effect appears as a change of slope in this pressure-time diagram. However, because of the small cross sectional area of the relief valve, the pressure keeps increasing after its opening. When the pressure reaches 0.40 MPa, the bursting disk opens. With a much larger cross sectional area, its opening causes a sharp pressure drop, bringing the vessel pressure quickly down to the backpressure value.
Figure 9 shows the fluid temperature during the simulated period. The opening of the relief valve has little effect on the temperature but, when the bursting disk opens, it drops sharply.

Figure 10 is a plot of the total molar amount within the vessel as a function of time. The amount is initially constant and equal to 80 moles because the vessel is closed; it then undergoes a small decrease while the valve relief is open but the bursting disk is closed, and finally decreases rapidly when both are open.

Figure 11 shows the fluid and sound speeds. The relief valve opens at about 293 s of simulated time. Between this time and the time the bursting disk opens, at about 795 s, the flow is sonic and of increasing velocity. Shortly after the opening of the bursting disk, at about 815 s, the flow becomes subsonic. It should be noted that the flow and sound speeds in the relief valve and in the bursting disk, when both are open, are identical. This happens because there is only one phase within the vessel at all times and, therefore, the properties of the fluid vented through both devices are equal.

Discharge of a two-phase n-hexane+n-octane mixture

This conceptual case simulates the discharge of an equimolar mixture of n-hexane+n-octane from an adiabatic vessel whose volume is 0.7894 m³, with height of 1.00 m and diameter of 1.00 m. The binary interaction parameter of the Peng-Robinson EOS was set to zero, as usual for hydrocarbon mixtures (Reid et al., 1987). The orifice has an area of 12.57×10⁻⁶ m², centered 0.50 m above the vessel’s bottom. The initial temperature of the fluid in its interior is 400 K. The load consists of 100 moles of each component and the coefficient of discharge is equal to 1. This section presents results of two cases with different initial fluid temperatures, equal to 450 K and 460 K. In both of them, the fluid has two phases inside the vessel at the beginning of the simulated period. However, the liquid level is low and the leak is from the vapor phase at all times.

Figures 12 and 13 show the evolution of pressure and temperature in the vessel as a function of the simulated time. For the initial temperature of 450 K, the fluid in the vessel has two phases throughout the simulated period. However, for the initial temperature of 460 K, the fluid has two phases up to only about 670 s, when the liquid phase disappears from the vessel. In Fig. 13, the liquid phase disappearance coincides with the change in slope that occurs at about 670 s in the curve that represents the system evolution from the initial temperature of 460 K.

Figure 14 shows the temperature at the exit point for the two simulated cases. From Figs. 13 and 14, it is clear that the temperature at the exit point is smaller than in the vessel at any given time. For example, at the beginning of the simulation, the temperature at the exit point is about 10 K smaller than the temperature inside the vessel. The curve
for the initial vessel temperature of 450 K (solid line in Fig. 14) has a change of slope at about 960 s, which coincides with the transition from sonic to subsonic flow at the exit point. The curve for the initial vessel temperature of 460 K (dotted line in Fig. 14) exhibits two changes of slope. The first of them occurs at about 670 s and is a consequence of the liquid phase disappearance from the vessel. The second one occurs at about 980 s, when the exit flow becomes subsonic.

Figure 15 displays the instantaneous leak flow rates of n-hexane and n-octane as a function of time for the initial fluid temperature of 450 K. Because the leak is from the vapor phase, the exit flow rate of n-hexane is larger than that of n-octane at the beginning of the simulation; thus, n-hexane depletes faster. At about 940 s, the flow rates of the two components become equal. After that, until the end of the simulated time, the flow rate of n-octane is larger.

This case illustrates the simulator’s ability of dealing with the change to the number of phases present in the vessel and its effect on the properties of the exiting stream.

Discharge of methane+ethane+propane: comparison with Haque et al.’s (1992b) data

This case considers experiment S9 of Haque et al. (1992b), which used a vertical vessel with torispherical ends and the following dimensions: tangent-to-tangent distance of 2.250 m, internal diameter of 1.130 m, wall thickness of 0.059 m, with a circular orifice whose diameter is 0.010 m, positioned at the top of the vessel. Such a vessel has an internal volume of 2.50 m³. As torispherical geometry is unavailable in the current version of our simulator, a vertical cylindrical vessel of the same volume and diameter is assumed, and its corresponding length is 2.49 m. It was also assumed that the vessel is made of stainless steel 316 with mass equal to 5515.2 kg. The vessel is initially charged with a mixture of methane, ethane, and propane, whose mole fractions are equal to 0.855, 0.045, and 0.100, respectively. The initial temperature and total amount in the vessel were taken equal to 303 K and 15060 moles, which give an initial pressure of 120 bar and a mass of 256.6 kg of fluid initially inside the vessel. Therefore, the initial mass of fluid is just 4.4% of the total mass of the system. As in case 4.3, the vessel is considered as adiabatic and the internal energy of the solid is considered in the simulation, with the heat capacity of steel at constant volume given by Eq. (6). The binary interaction parameters of the Peng-Robinson EOS are set equal to zero, which is typical for hydrocarbon mixtures (Reid et al., 1987). The existence of a single vapor phase throughout the simulated period is predicted. Figure 16 compares the experimental (Haque et al., 1992b) pressure with the calculated pressure, the latter plotted against rescaled time, which is the simulation time divided by a coefficient of discharge of 0.57, such that the rescaled time at the end of the run is equal to 1200 seconds.
Despite the similar trends, the calculated pressure is higher than the experimental pressure. According to Haque et al. (1992b), the final experimental temperature of the wall in contact with the gas is about 290 K. They also report the formation of a small volume of liquid phase in the vessel and the final temperature of the solid wall in contact with it is about 250 K. As the simulator adopts a homogeneous equilibrium model, the calculated temperatures of the fluid and of the vessel wall are equal, initially 303 K, and 284.6 K at the end of the simulation, which is somewhat smaller than the final experimental temperature of the wall in contact with the gas (290 K).

CONCLUSIONS

This work presented the results of a simulator based on the homogenous equilibrium assumption for discharges from pressure vessels that contain non-reactive mixtures. The particular feature of this simulator is that it evaluates all the thermodynamic properties using the same equation of state, including phase equilibrium conditions, calorimetric properties, and derivative properties, such as the sound speed. The Peng-Robinson equation of state was used, but the formulation is general and it is possible to adopt other thermodynamic models.

The conceptual and sensitivity analyses reported here demonstrate that the simulator predicts meaningful trends for the complex phenomena that take place during discharge operations. The simulated results generally agree with the experimental fluid discharge data when a coefficient of discharge is used. Future work on this simulator will focus on: (a) the effect of liquid swelling caused by bubbles due to non-instantaneous phase disengagement during leaks of condensable fluids; (b) expanding the availability of heat transfer models available; (c) studying the venting dynamics of vessels with several runaway reactions.

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NOMENCLATURE

\( A^\text{out}_m \) orifice area at exit point \( m \)

\( c_v \) specific heat capacity at constant volume

\( h^\text{ch} \) molar enthalpy of the discharged fluid at the entrance of the hypothetical nozzle

\( h^\text{out}_m \) molar enthalpy at exit point \( m \)

\( M^\text{out}_m \) molar mass at exit point \( m \)

\( n_i \) number of moles of component \( i \) in the vessel

\( n^\text{out}_m \) molar flow rate of component \( i \) in stream \( m \)

\( n^\text{out}S \) number of streams that exit the vessel

\( \dot{Q} \) heat transfer to the fluid in the vessel

\( s^\text{ch} \) molar entropy of the discharged fluid at the entrance of the hypothetical nozzle
$S_{out}^m$  molar entropy at exit point $m$

t  time

$u_{out}^m$  fluid speed at exit point $m$

$U$  internal energy of the fluid and of the vessel wall

$V_{out}^m$  fluid molar volume at exit point $m$

REFERENCES


