Formation Flight Control of Multi-UAV System with Communication Constraints

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ABSTRACT: Three dimensional formation control problem of multi-UAV system with communication constraints of non-uniform time delays and jointly-connected topologies is investigated. No explicit leader exists in the formation team, and therefore, a consensus-based distributed formation control protocol which requires only the local neighbor-to-neighbor information between the UAVs is proposed for the system. The stability analysis of the proposed formation control protocol is also performed. The research suggests that, when the time delay, communication topology, and control protocol satisfy the stability condition, the formation control protocol will guide the multi-UAV system to asymptotically converge to the desired velocity and shape the expected formation team, respectively. Numerical simulations verify the effectiveness of the formation control system.

KEYWORDS: Three dimensional formation control, Jointly-connected topologies, Multi-UAV system, Non-uniform time delays, Consensus protocol.

INTRODUCTION

Recently, with the development of computer control, sensors, communication network etc., many researches on the formation flight control have been performed. This is because various missions can be successfully completed by the formation flight, such as battlefield reconnaissance, multi-target attacking, environment monitoring and earthquake rescue and so on. Multi-UAV coordinated formation control has overwhelming superiority in high efficiency in performing tasks, low cost of fuel, strong robustness and more flexibility compared with single UAV (Ren and Beard 2008; Cao et al. 2012). Therefore, multi-UAV formation flight control has become a hot topic in UAV field.

In earlier years, typical approaches for formation control could be roughly categorized as leader-follower, behavioral, virtual leader/virtual structure. Most of the formation flight researches are performed based on the leader-follower approach, where some UAVs are designed as leaders while others are designed as followers (Ren 2007; Giulietti et al. 2000). In this approach, the leaders track the predefined trajectory, and the followers track the nearest leaders according to given schemes. It is easy to analyze and implement the leader-follower controller. However, the leader is a single point for the formation, and therefore this approach is not robust with respect to the leader failure.

In recent years, the problem of multi-UAV cooperative formation flight control based on consensus protocol has drawn substantial research effort from many studies (Kuriki and Namerikawa 2013; Menon 1989; Ren 2006; Seo et al. 2012). Ren (2007) extended a consensus protocol, which is introduced for systems modelled by second-order dynamics, to tackle multi-UAV formation control problems by appropriately choosing information states on which consensus is reached. Seo (2009)
proposed a consensus-based formation flight control protocol and proved that the multi-UAV system can form and maintain a geometric formation flight with the network topology switching between a directed strongly-connected topology and a topology with a spanning tree. Dong et al. (2014) investigated the time-varying formation control problem by applying a consensus-based formation control protocol, and necessary and sufficient conditions are obtained for the stability of the system which contains a spanning tree in the fixed topology. Then a quadrotor formation platform was introduced to validate the theoretical results. However, most of the researches about consensus-based cooperative formation flight control are mainly focused on two systems: one is a fixed communication topology without time delays; the other is a switching communication topology without time delays as well. There are few results available to treat the formation control system with jointly-connected topologies and time delay. But, in reality, the time delay usually exists due to transmission rate and network congestion, and the communication topology of the multi-UAV system will be changed owing to communication jamming, complex terrain, limitation of communication distance etc. Therefore, it is of great significance in both theory and application to investigate cooperative formation flight control by considering time delay and changing topology.

The main contributions of the paper can be summarized as follows. First, to design a new formation flight control protocol considering two key-problems: one is the diverse and asymmetric time delays, and the other is the dynamically changing topologies. The topologies discussed here may not connect all the time but the union of the topologies is connected in each period of time. Second, the analysis of the complex topologies is turned to a simple research of connected component in each period of time according to the stability analysis, and a sufficient condition for the stability is obtained based on Lyapunov theory. The multi-UAV system can shape and maintain the expected formation with desired velocity, when it satisfies the sufficient condition.

MODEL OF THE MULTI-UAV SYSTEM

This paper considers a group system consisting of \( n \) autonomous UAVs, and the point-mass model is used to describe the motion of the UAV formation flying. The related variables are defined with respect to the inertial coordinate system and are shown in Fig. 1 (Wang and Xin 2012).

The model assumes that the aircraft thrust is directed along the velocity vector and that the aircraft always performs coordinated maneuvers. It is also assumed that the Earth is flat, and the fuel expenditure is negligible, i.e. the center of mass is time-invariant (Xu 2009). Under these assumptions, the motion equations of the \( i \)th UAV can be described as follows:

\[
\begin{bmatrix}
\dot{x}_i \\
\dot{y}_i \\
\dot{h}_i \\
\dot{v}_i \\
\dot{\gamma}_i \\
\dot{\chi}_i \\
\dot{\phi}_i \\
\dot{L}_i
\end{bmatrix} = \begin{bmatrix}
v_i \cos \gamma_i \cos \chi_i \\
v_i \cos \gamma_i \sin \chi_i \\
v_i \sin \gamma_i \\
(T_i - D_i)m_i - g \sin \gamma_i \\
(g/v_i)(n_i \cos \phi_i - \cos \gamma_i) \\
L_i \sin \phi_i / (m_i v_i \cos \gamma_i)
\end{bmatrix}
\]

where: \( i = 1, 2, ..., n \) is the index of multiple UAVs under consideration. For UAV \( i \), \( x_i \) is the down-range; \( y_i \) is the cross range; \( h_i \) is the altitude; \( v_i \) is the ground speed; \( \gamma_i \) is the flight path angle; \( \chi_i \) is the heading angle; \( T_i \) is the engine thrust; \( D_i \) is the drag; \( m_i \) is the mass; \( g \) is the acceleration due to gravity; \( \phi_i \) is the banking angle; \( L_i \) is the vehicle lift.

The control variables in the UAVs are the g-load \( n_i = L_i / g m_i \), controlled by the elevator, the banking angle \( \phi_i \), controlled by the combination of rudder and ailerons, and the engine thrust \( T_i \), controlled by the throttle. Throughout the formation control process, the control variables will be constrained to remain within their respective limits.

Define \( R^{m \times n} \) as a \( m \times n \) real matrix set, \( \xi_i = [x_i, y_i, h_i]^T \in R^3 \), and \( u_i = [u_{xi}, u_{yi}, u_{hi}]^T \in R^3 \). Differentiating \( \dot{x}_i, \dot{y}_i, \dot{h}_i \) with respect to time twice and substituting \( x_i, y_i, h_i \) one has the transformed dynamic models of the \( i \)th UAV as follows:

\[
\dddot{\xi}_i = u_i
\]

where: \( \xi_i \) is the position of UAV \( i \); \( u_i \) is a new control variable,
and the relationship between $u_i$ and the actual control variable $U_i$ is given by the expressions (Xu 2009):

$$
\phi = \tan^{-1}\left(\frac{u_i \cos \theta_i - u_i \sin \theta_i}{\cos \gamma_i (u_i + g) - \sin \gamma_i (u_i \cos \theta_i + u_i \sin \theta_i)}\right)
$$

(3)

$$
\tau_i = \frac{\cos \gamma_i (u_i) - \sin \gamma_i (u_i \cos \theta_i + u_i \sin \theta_i)}{g \cos \phi}
$$

(4)

$$
T_i = \left[\sin \gamma_i (u_i + g) + \cos \gamma_i (u_i \cos \theta_i + u_i \sin \theta_i)\right] m_i + D_i
$$

(5)

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**FORMATION CONTROL PROTOCOL DESIGN OF THE MULTI-UAV SYSTEM**

The multi-UAV system and its behavior are described in graph theory. It is supposed that the multi-UAV system under consideration consists of $n$ UAVs and $G(\Gamma, E, A)$ is an undirected graph of the multi-UAV system, where $\Gamma = \{s_1, s_2, ..., s_n\}$ is the set of nodes, $\ell = \{1, 2, 3, ..., \ell\}$ is the set of number of nodes, and $E = \{(s_i, s_j) \in \Gamma \times \Gamma, i \neq j\}$ is the set of edges. At each time, each UAV updates its current state based upon the information received from its neighbors. Undirected graphs are used to model communication topologies. Each UAV is regarded as a node. Each edge $(s_i, s_j)$ corresponds to an available information link between UAV $s_i$ and UAV $s_j$. A communication topology is formed when the UAVs begin to communicate to each other at any time. In reality, the communication topology usually switches due to link failure brought by communication blocking, external disturbance, hardware failure etc. To describe the variable topologies, a piecewise constant switching function $\sigma(t)$ is defined, where $N(t)$ denotes the total number of all possible communication undirected graphs. The communication graph at time $t$ is denoted by $G_\sigma$ and the corresponding Laplacian, by $L_\sigma$. This paper investigates the design of the control protocol of the multi-UAV system under jointly-connected communication graph.

The state-space form of the dynamics of the $i^{th}$ UAV is obtained from Eq. 2, as follows:

$$
\begin{align*}
\dot{\xi}_i(t) &= \zeta_i(t) \\
\dot{\zeta}_i(t) &= u_i(t)
\end{align*}
$$

(6)

where: $\xi_i(t) \in \mathbb{R}^3$ is the position state; $\zeta_i(t) \in \mathbb{R}^3$ is the velocity state; $u_i(t) \in \mathbb{R}^3$ is the control input.

We say that the control protocol $u_i(t)$ solves the formation control problem if the states of UAVs satisfy $\lim_{t \to \infty} [\xi_i(t) - \xi_j(t)] = \tau_{ij}$ and $\lim_{t \to \infty} [\zeta_i(t) - \zeta_j(t)] = \frac{\zeta_i(t) - \zeta_j(t)}{r_{ij}}$, where $\tau_{ij}$ is the expect distance between UAV $i$ and UAV $j$ in formation and $\zeta_i(t) \in \mathbb{R}$ is the expected velocity, i.e. the multi-UAV system can shape and maintain an expected formation with a desired velocity under the control protocol $u_i(t)$.

In this paper, a formation flight control protocol for the multi-UAV system is designed, and the two key-problems of non-uniform time delays and jointly-connected topologies are considered. To solve this problem, a linear control protocol for the $i^{th}$ UAV is firstly presented, as follows:

$$
\begin{align*}
u_i(t) &= \sum_{j \in N(i)} a_{ij}(t) \left[k_1(\xi_j(t) - \xi_i(t)) - \zeta_i(t) - \tau_{ij}(t) \right] + \\
&+ \sum_{m=1}^M a_{ij}(t) \left[k_2 \left[\zeta_j(t) - \zeta_i(t) - \tau_{ij}(t) \right] - r_{ij} \right]
\end{align*}
$$

(7)

where: $a_{ij}(t)$ is the adjacency weight of the communication graph $G_\sigma$; $N_i(t)$ is the neighbor set of the $i^{th}$ UAV; $k_1, k_2 > 0$, and $k_3 = k_4 k_5$; $\tau_m(t)$ is the time-varying self-delay of the $i^{th}$ UAV that may be caused by measurement or computation, and $\tau_{ij}(t)$ is the time-varying delay for the $i^{th}$ UAV to get the state information of the $j^{th}$ UAV.

Here, it is not required that $\tau_{ij}(t) = \tau_{ji}(t)$. It is supposed that there are altogether $M$ different time delays, denoted by $\tau_m(t) \in \mathbb{R}^M(t)$, $m = 1, 2, ..., M$, satisfying the following assumptions 1 and 2.

**Assumption 1**: the time-varying delays $\tau_m(t)$, $m = 1, 2, ..., M$, are satisfied $0 \leq \tau_m(t) \leq h_m$ and $\dot{\tau}_m(t) \leq d_m < 1$ for specified constants $h_m > 0$ and $d_m > 0$.

A model transformation is made to analyze the close-loop control performance of the multi-UAV system. Therefore, the concept of formation center is introduced, which is a formation centroid of the multi-UAV system. A formation of “regular pentagon” is considered as an example for convenient and easy understanding of the formation problem, as shown in Fig. 2, where $O$ is the origin of Cartesian coordinates, $O_i$ is the formation center, $\xi_i(t)$ and $\dot{\xi}_i(t)$ are positions of UAV $i$, in plane coordinate system, respectively, and $\dot{\xi}_i(t)$ is the formation center. The distance between UAV $j$ and the formation center are $r_j$ and $\dot{r}_j$, respectively.

Consequently, the control protocol (Eq. 7) can be transformed into:

$$
\begin{align*}
u_i(t) &= \dot{\zeta}_i + \sum_{j \in N(i)} a_{ij}(t) \left[k_1(\dot{\xi}_j(t) - \dot{\xi}_i(t)) - \zeta_i(t) - \tau_{ij}(t) \right] + \\
&+ \sum_{m=1}^M a_{ij}(t) \left[k_2 \left[\zeta_j(t) - \zeta_i(t) - \tau_{ij}(t) \right] - r_{ij} \right]
\end{align*}
$$

(8)
where: \( r_{ji} = r_j - r_i \).

\[ u_i(t) = \sum_{\gamma \in \mathcal{K}(i)} e_{\gamma}(t) \left[ k_{\gamma} \left( \xi_i(t) - \tau_{\gamma}(t) \right) - \xi_i(t) \right] + \frac{2}{k_{\gamma}} \left[ \bar{\xi}_i(t) - \xi_i(t) \right] = \xi_i(t) \] (9)

It is denoted:

\[ \dot{\xi}_i(t) = 2 \bar{\xi}_i(t)/k_{\gamma} + \xi_i(t); \quad \alpha(t) = [\bar{\xi}_i(t), \xi_i(t), \ldots , \xi_i(t), \xi_i(t)]^T \]

\[ B = \begin{bmatrix} -k_{\gamma}/2 & k_{\gamma}/2 \\ k_{\gamma}/2 & -k_{\gamma}/2 \end{bmatrix}; \quad Q = \begin{bmatrix} 0 & 0 \\ 0 & 2/k_{\gamma} \end{bmatrix} \] (10)

Under the protocol (Eq. 9), the closed-loop dynamics of the multi-UAV system is:

\[ \dot{e}(t) = (I_n \otimes B) e(t) - \sum_{m=1}^{d_{\alpha}} (I_{om} \otimes Q) e(t - \tau_{am}) \] (11)

where: \( I_n \) is the \( n \)-dimensional unit matrix; \( \otimes \) denotes the Kronecker product; \( I_{om} \in \mathbb{R}^{m \times n} \); \( I_{om} \otimes Q \) is the coefficient matrix of the variable \( e(t - \tau_{am}) \) for \( m = 1, 2, \ldots , M \). It is clear that \( L_{\alpha} = \sum_{m=1}^{d_{\alpha}} I_{om} \) and \( I_{\alpha} = L_{\alpha} \).

Evidently, if \( \lim_{t \to t_{am}} e(t) = 0 \), then \( \lim_{t \to t_{am}} \bar{\xi}_i(t) = 0 \) and \( \lim_{t \to t_{am}} \xi_i(t) = 0 \), i.e. \( \lim_{t \to t_{am}} \xi_i(t) - \tau_{am} = 0 \). And \( \lim_{t \to t_{am}} \xi_i(t) = \xi_i \), that is, the multi-UAV system can shape and maintain the expected formation with a desired velocity under the formation control protocol. In the following, we prove that the multi-UAV system can realize \( \lim_{t \to +\infty} e(t) = 0 \) under the protocol (Eq. 7).

**STABILITY ANALYSIS OF FORMATION FLIGHT CLOSE-LOOP CONTROL SYSTEM**

**Definition of switching topology and related lemmas**

Some preliminary definitions and results need to be presented before the stability analysis. The concept of switching topology is introduced first. It is considered an infinite sequence of non-empty, bounded, and contiguous time intervals \([t_k, t_{k+1})\), \( k = 0, 1, \ldots \), with \( t_0 = 0 \) and \( t_{k+1} - t_k \leq T_1 \) for some constant \( T_1 > 0 \). It is supposed that, in each interval \([t_k, t_{k+1})\), there is a sequence of non-overlapping subintervals

\[ [t_{k_0}, t_{k_1}), \ldots , [t_{k_{m-1}}, t_{k_m}) \]

(12)

satisfying \( t_{k_{m-1}} - t_{k_m} \geq T_2, 0 \leq b \leq m \), for some integer \( m \geq 0 \) and a given constant \( T_2 > 0 \) such that the communication topology \( G_{\sigma} \) switches at \( t_{kb} \) and it does not change during each subinterval \([t_{kb}, t_{kb+1})\).

**Assumption 2:** the collection of graphs in each interval \([t_k, t_{k+1})\) is jointly-connected.

With the switching topologies defined above, it is supposed that the time-invariant communication graph \( G_{\sigma} \) in the subinterval \([t_{kb}, t_{kb+1})\) has \( d_{\sigma} \) (\( d_{\sigma} \geq 1 \)) connected components with the corresponding sets of nodes denoted by \( \psi_{k_1}^{\sigma}, \psi_{k_2}^{\sigma}, \ldots , \psi_{k_{d_{\sigma}}}^{\sigma} \). Then there exists a permutation matrix \( P_{\sigma} \in \mathbb{R}^{n \times n} \) such that \( P_{\sigma}^T L_{\sigma} P_{\sigma} = \text{diag}(L_{om1}^2, L_{om2}^2, \ldots , L_{omd_{\sigma}}^2) \),

\[ P_{\sigma}^T L_{om\sigma} P_{\sigma} = \text{diag}(L_{om1}, L_{om2}, \ldots , L_{omd_{\sigma}}) \] (13)

and

\[ e^T(t)(P_{\sigma} \otimes I_{\beta}) = [e_{\sigma}^1, e_{\sigma}^2, \ldots , e_{\sigma}^{d_{\alpha}}] \]

where each block matrix \( L_{\sigma}^m \in \mathbb{R}^{d_{\sigma} \times d_{\sigma}} \) is the Laplacian of the corresponding connected component, \( L_{om} \in \mathbb{R}^{d_{\alpha} \times d_{\alpha}} \) and \( L_{\sigma} = \sum_{m=1}^{d_{\alpha}} L_{om} \). Then, in each subinterval \([t_{kb}, t_{kb+1})\), the system (Eq.11) can be decomposed into the following \( d_{\alpha} \) subsystems:

\[ \dot{e}_{\sigma}(t) = (I_{\sigma} \otimes B) e_{\sigma}(t) - \sum_{m=1}^{d_{\alpha}} (L_{om} \otimes Q) e_{\sigma}(t - \tau_{am}) \]

(15)

where: \( e_{\sigma}(t) = [e_{\sigma}^1(t), \ldots , e_{\sigma}^{d_{\alpha}}(t)] \in \mathbb{R}^{d_{\alpha}} \).

Lemma 1 (Lin and Jia 2010): consider the matrix \( C_{\alpha} = n I_n - 11^T \) (1 represents \([1, 1, \ldots , 1]^T \) with compatible dimensions).
then there exists an orthogonal matrix $U_n \in \mathbb{R}^{n \times n}$ such that
$$U_n^T D U_n = \text{diag}\{nI_{n-1}, 0\}$$
and the last column of $U_n$ is $1/\sqrt{n}$.

Given a matrix $D \in \mathbb{R}^{n \times n}$ such that $1^T D = 0$ and $D 1 = 0$, then
$$U_n^T D U_n = \text{diag}\{(U_n^T D U_n)^T, 0\},$$
where $\mathcal{U}_n$ denotes the first $n-1$ columns of $U_n$.

Lemma 2 (Lin and Jia 2011): for any real differentiable vector function $x(t) \in \mathbb{R}^n$, any differentiable scalar function $\tau(t) \in [0, h]$, and any constant matrix $0 < H = H^T \in \mathbb{R}^{n \times n}$, the following inequality can be obtained:
$$\frac{1}{h} [x(t) - x(t - \tau(t))]^T H [x(t) - x(t - \tau(t))] \leq \int_{t - \tau(t)}^{t} \tilde{V}(s) H(s) ds, \quad t \geq 0$$

where $h > 0$ is a specified scalar value.

**Sufficient conditions for the multi-UAV close-loop control system**

Theorem 1: Consider a multi-UAV system with non-uniform time delays and switching topologies, for each subinterval $[t_{k-1}, t_k)$, if there is a common constant $\gamma > 0$ and $F^i \in \mathbb{R}^{(f_i \times f_i)}$, $i = 1, 2, ..., d$, such that
$$F_i^T \Xi_i F_i < 0$$

then $\lim \xi_i(t) - \xi_j(t) = r_{ij}$ and $\lim \zeta_i(t) = \zeta^*$, that is, the multi-UAV system can finally shape an expected formation with the desired velocity $F^i = \text{diag}\{U^i_{f_{i1}}, I_{2Mf_{i2}}\}$ and $U^i_{f_{i2}}$ is defined as in Lemma 1, where
$$\Xi^i = \begin{bmatrix} \Xi_{11} & \Xi_{12} \\ \Xi_{21} & \Xi_{22} \end{bmatrix}.$$
From the analysis above, system (Eq. 11) is stable (Gu et al. 2003), i.e. \( \lim_{t \to +\infty} V(t) = 0 \), thus \( \lim_{t \to +\infty} \epsilon(t) = 0 \); consequently, \( \lim_{t \to +\infty} \xi(t) = \xi \), and \( \lim_{t \to +\infty} \zeta(t) = \zeta \), that is, the multi-UAV system can shape and maintain the expected formation with an desired velocity under the formation control protocol (Eq. 7).

MULTI-UAV CONTROL SYSTEM SIMULATION

Numerical simulations will be given to verify the designed control protocol and illustrate the theoretical results obtained in the previous section. In this paper, the drag in the UAV model (Eq. 1) is calculated by (Xu 2009):

\[
D_i = 0.5 \rho (v_i - v_n)^2 S_i C_{D0} + 2 k k_n n_i W_i^2 / \left( \rho (v_i - v_n)^2 S_i \right) \quad (19)
\]

where: the wing area \( S_i = 37.16 \text{ m}^2 \); the zero lift drag coefficient \( C_{D0} = 0.02 \); the load factor effectiveness \( k_n = 1 \); the induced drag coefficient \( k = 0.1 \); the gravitational coefficient \( g = 9.81 \text{ kg/m}^2 \); the atmospheric density \( r = 1.2207 \text{ kg/m}^3 \); the weight of the UAV \( W_i = m_i g = 14,515 \text{ N} \). The gust model is \( v_{wi} = v_{wi,n} + v_{wi,t} \) and varies according to the altitude \( h \). In the simulated gust, the normal wind shear \( v_{wi,n} = 0.215 U \log_{10}(h) \), where \( U = 22.7 \text{ m/s} \) is the mean wind speed at an altitude of 5,000 m. The turbulence part of the wind gust \( v_{wi,t} \) has a Gaussian distribution with a zero mean and a standard derivation of 0.09 \( U \).

The six UAVs system will complete the task of formation climbing, level flight, and gliding. The communication topology graph of the UAVs and the expected formation structure are shown in Figs. 3 and 4, respectively.

The communication topology in Fig. 3 switches every 0.1 s in the sequence of \( G_1, G_{II}, G_{III}, G_1 \). All graphs in this figure are not connected, and the weight of each edge is 1.0, but the union of the graphs is jointly-connected. It is supposed that there are altogether three different time delays, denoted by \( \tau_1(t), \tau_2(t), \text{ and } \tau_3(t) \): \( \tau_1(t) = \tau_3(t) = \tau_4(t) = \tau_5(t) = \tau_6(t) = \tau_2(t) \); and \( \tau_2(t) = \tau_3(t) = \tau_4(t) = \tau_5(t) = \tau_6(t) = \tau_1(t) = \tau_2(t) \). The time delays satisfy \( 0 \leq \tau_1(t) \leq 0.01, 0 \leq \tau_2(t) \leq 0.02, 0 \leq \tau_3(t) \leq 0.03 \). It is supposed that all initial conditions of position, velocity, and flight path angle are randomly set. The desired \( v_1 = (50 + 10 \sin(0.08 t)) \text{ m/s} \) and \( \chi = 45^\circ \). It is solved that (Eq. 16) is feasible for \( k_1 = 0.6, k_2 = 1.1, k_3 = 0.66 \).

The trajectories of position, velocity, flight path angle, heading angle, and the formed formation are shown in Figs. 5 to 11.

It is clear that the multi-UAV system can complete the maneuver formation flight task with the expected velocity and heading angle as well as maintain the desired formation during the flight.
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Figure 6. Top view of UAVs’ formation flying.

Figure 7. Time histories of the height.

Figure 8. Time histories of the velocity.

Figure 9. Time histories of the distance between the UAVs.

Figure 10. Time histories of the heading angle.

Figure 11. Time histories of the flight path angle.
CONCLUSION

Three-dimensional formation flight control problems are investigated, considering the constraints of jointly-connected topologies and non-uniform time delays, where each UAV has a self-delay, and all delays are independent of each other. A consensus-based formation control protocol is designed, and the stability problem of the multi-UAV formation control system is turned into the problem that looks for a feasible solution by solving the linear matrix inequality. In reality, it is only necessary to study the connected components with different topology structures, making it possible to simplify the analysis of the whole topology structures. Numerical examples are included to illustrate the obtained results in addition. If the communication topology is jointly-connected and the non-uniform time delays satisfy the designing requirements, then the multi-UAV system can shape the desired formation and also maintain the expected velocity, heading angle, and expected flight path angle.

The problems of collision avoidance constraint and the size of the UAVs are not considered here. These challenging and meaningful problems will be presented in future studies.

REFERENCES


