On the use of Titration Calorimetry to Study the Association of Surfactants in Aqueous Solutions

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A técnica de titulação calorimétrica isotérmica vem sendo cada vez mais usada na investigação de processos de associação envolvendo surfatantes. Este fato pode ser associado com o desenvolvimento de novos equipamentos mais sensíveis e de mais fácil operação, alíado à vantagem de possibilitar a determinação simultânea dos principais parâmetros termodinâmicos associados a estes processos. Entretanto, uma parte significativa destes novos usuários ainda não está familiarizada com vários aspectos relacionados ao uso desta técnica calorimétrica. Por isto, este artigo de revisão pretende discutir o planejamento e execução de experimentos com o objetivo de investigar associação de surfatantes em água e na presença de polímeros, eletricamente carregados ou não, bem como discutir a determinação dos parâmetros termodinâmicos a partir das curvas de titulação. Alguns exemplos da literatura são discutidos para ilustrar estas aplicações em diferentes sistemas.

Keywords: titration calorimetry, surfactant association, surfactants, polymer solutions, thermodynamics

1. Introduction

Nowadays, accurate and easy-to-operate titration calorimeters are commercially available with the advantage that they can be used to study the association of amphiphilic substances in solution. This can be self-association to determine c.m.c. and enthalpies of micelle formation, aggregation in the presence of polymers or interaction with other amphiphilic aggregates such as vesicles and so on. Usually, results of other types of measurements are needed to gain insight into the complex systems under study. This means that persons that carry out the calorimetric experiments, or who wish to do so and have had no special training in the method may feel uncertain about how to plan the experiments and evaluate the results. In this article we review the main design features of common instruments, the principles of operation and how to plan and evaluate the experiments. We do not give any general treatment of basic thermodynamics of solutions but refer to textbooks on general physical chemistry. A more extensive treatise is given in reference 1. The chapter by Desnoyers et al.2 deals with thermodynamics related to calorimetric measurements on surfactant systems.

2. Principal Design Features

Titration calorimetric experiments are carried out at constant temperature so the method is commonly named isothermal titration calorimetry, abbreviated as ITC. The calorimeters usually have a high sensitivity so small heat
effects are measured with good accuracy. The volume of the reaction vessels is usually 1 to 4 mL but larger or smaller vessels can be used. Measurements can be made using small amounts of dilute solutions, which means that limited amounts of substances are required. Sensitive calorimeters are normally arranged as twins and function as differential instruments. In the following, we will use the word microcalorimeter for various high-sensitivity solution calorimeters. One calorimetric vessel contains the reaction system and the second reference vessel is an inactive dummy that, preferably, has heat capacity and heat conduction properties similar to the reaction vessel. The titrant solution is added from a high-precision syringe outside the calorimeter.

Sensitive commercial calorimeters have one of two principally different designs: adiabatic calorimeters or heat conduction calorimeters. MicroCal’s (Northampton, MA, USA) and CSC’s (TA Instruments) titration microcalorimeters are in principle adiabatic calorimeters. The MicroCal instrument has coin-shaped cells permanently mounted on either side of a special thermoelectric device, which measures the temperature difference between the two cells. The cells contain electrical heaters and the temperature is allowed to slowly increase during an experiment by heating the reference cell by a small constant power. The temperature difference between the sample and reference cell is monitored and the proportional power fed to the sample cell is adjusted to keep the temperature of the two cells the same (power compensation calorimeter). The heat generated or taken up in the process is proportional to the integral of the differential power. This instrument has a small time constant, that is, it reaches thermal equilibrium fast. The totally filled cells in the present versions of the instrument have a volume of about 1.3 mL and are permanently mounted. The calorimeter, and its use, is described in reference 3. The reactant solution R produces (or taken up) during an experiment is too large, over about 0.2 mW. This means that if we choose to use an injection rate of 0.5 µL s\(^{-1}\) when we study a process that gives an enthalpy change of 20 kJ mol\(^{-1}\) of injected R\(_2\), the concentration of R\(_2\) in the syringe cannot exceed 0.02 mol L\(^{-1}\). The CSC isothermal titration calorimeter has 1 mL fixed conical cells and a fast response time.\(^{4}\)

The prototypal heat conduction microcalorimeter, also called heat-leak, heat-flow or heat-flux calorimeter, developed by Suurkuusk and Wadsö, is described in reference 5. In a heat conduction microcalorimeter, heat released (or taken up) in the reaction vessel flows to (or from) a surrounding heat sink, usually an aluminum block. Thermopile plates positioned between the sample container and the heat sink register the heat flow. The temperature difference between the vessel and the heat sink, which is the driving force for the heat flow, will generate an electrical potential over the thermopile that is recorded. Semiconducting thermopiles, often called thermocouple plates, are used as sensors. They have a relatively large thermal conductance and the temperature difference between the calorimeter vessel and the surrounding heat sink is usually small, of the order of 1 mK. The time constant for heat conduction calorimeters is usually fairly large, typically between 100 to 1000 s. This means that for fast processes the time needed to reach thermal equilibrium is much longer than the time needed for the reaction to go to completion. Even if the reaction is fast, a titration calorimetric experiment with, say, 10 consecutive injection steps may require several hours. However, the time needed can be reduced by an order of magnitude without loss of accuracy by using a dynamic correction method. Sample injections are made at 5 to 7 min interval without waiting for the signal to return to the baseline.\(^{6}\)

After the experiment, the curve is deconvoluted using the Tian equation\(^{6}\) with a value for the time constant determined from electrical calibration experiments.

Heat conduction calorimetric systems are marketed by TA Instruments (previously by Thermometric, Järfalla, Sweden and by CSC Lindon, Utah, USA). Reaction vessels in the TAM calorimeters (Suurkuusk-Wadsö design) are usually 1 to 4 mL in volume but may be up 20 mL in some equipment. Usually, they are replaceable for easy cleaning and filling. An appropriate amount of solution containing reactant R\(_1\) (or pure solvent) is placed in the reaction vessel. The vessels are only partially filled leaving a gas phase above the liquid. Solution of reactant R\(_1\) in the same solvent as reactant R\(_2\) (or pure R\(_2\)) is added from the external syringe through a stainless steel capillary. During the titration the total volume increases and the solution of reactant R\(_1\) is diluted while the total amount of R\(_1\) is unchanged. The enthalpic effect from this dilution is usually insignificant but is easily checked by separate dilution
experiments injecting the solvent into the calorimetric liquid. This system has a large measuring range from 0.1 µW to 10 mW.

In titration calorimetric experiments the titrant solution is usually added stepwise in small portions in order to have good control of the concentration of the reactants and to achieve the best accuracy in the measurements. Typical injection volumes range from 1 to 15 µL although larger injection volumes are possible for some equipment. When using small injection volumes of concentrated solutions or pure liquids, the problem of diffusion of the titrant solution in contact with the solution in the calorimeter vessel should be considered. When using larger injection volumes, the injection rate must be low enough to allow thermal equilibration of the titrant solution before it reaches the calorimetric vessel.

Particularly when working with systems giving small heat effects it is advisable to make frequent blank experiments of titration of water into water (or solvent into solvent) to detect spurious heat effects. Most common disturbances arise from pressure-volume work due to blockage in the outlet from the calorimetric cell. Only small restrictions in the outlet can cause significant heat effects as measured in a highly sensitive calorimeter.

The titration microcalorimeters were developed and used primarily for studies of biochemical systems, particularly, protein-ligand binding processes and for the hydration of small hydrophobic solutes. This means that the stirring in the calorimeter vessel has been optimized for dilute aqueous solutions. When designing the stirrers and adjusting the stirring speed, the aim has been to minimize the heat of friction from stirring and the mechanical wear of dissolved proteins by keeping the stirring speed as low as possible. The advice in the manuals for the commercial calorimeters applies to such conditions. But even small changes in viscosity of the calorimetric solution can have a detrimental effect on the stirring efficiency. Problems can arise when studying, for instance, polymer solutions or when solvents other than water are used.

In the disc-shaped vessel of the MicroCal calorimeter, the tip of the injection needle is modified to act as a stirrer and the syringe rotates to achieve stirring. The stirring blades cannot extend further into the sample than the width of the cell and a large fraction of the liquid may be out of reach. Experiments using different stirring speeds may indicate if the stirring is sufficient for the system studied.

An efficient turbine stirrer is needed to achieve satisfactory mixing in the cylindrical 4 mL vessel used with the TAM heat conduction calorimeter. It is important that the stirrer induces a vertical movement in the liquid. Horizontal stirring resulting in liquid layers is easy to achieve but will not give a homogenous solution. We have found it very valuable to perform bench experiments using transparent plastic vessels to check stirring efficiency. The flow pattern in the solution to be studied can then be examined by injecting a colored solution. One should keep in mind that the viscosity may change significantly during a titration experiment. This is most likely to happen when surfactant solution is added to a polymer solution where the interaction between polymer chains may be changed by the added surfactant. A change in viscosity will give a change of the baseline as the heat of friction from stirring will change. This baseline shift may need to be considered when calculating the peak area.

Usually, microcalorimeters are calibrated electrically, which is convenient and highly accurate if the electrical heater is properly placed. However, in order to check the overall performance of the system, including the auxiliary equipment, we recommend the use of a suitable test reaction. The dissolution of propan-1-ol in water is a convenient reaction for this purpose. However, the heat effect is too large for many of the instruments. The dilution of (aqueous) 10.00 mass % propanol is an alternative that gives smaller heat effects. For the more sensitive calorimeters, even the dilution of 10.00 mass % propanol may give heat effects too large to be convenient and dilution of 1.00 mass % propanol (or another dilute concentration) may be used instead. The dilution enthalpy and, accordingly, the heat effect (at 25 °C) is calculated using the virial interaction coefficients reported in reference 8.

3. Use of Titration Calorimetry to Study Micelle Formation, Uncharged Polymer-Surfactant Interaction and Polyelectrolyte-Surfactant Interaction

3.1. Micelle formation of surfactants in water

The critical micelle concentration, c.m.c., and enthalpy of micelle formation, \( \Delta H_{\text{mic}} \), can be determined from titration calorimetric experiments. From measurements at varying temperatures, the heat capacity change, \( \Delta C_p,\text{mic} \), is derived. In a typical experiment, small aliquots of concentrated surfactant solution, the titrant solution, are injected into the reaction vessel initially containing pure solvent. The injection volumes are usually in the range of 5 to 15 µL and the volume of the solvent is in the range of 0.9 to 3 mL. The concentration, \( C_\text{T} \), of the titrant solution should be high, at least 20 times the c.m.c. so that the monomer concentration can be disregarded, see below. In the first few injections giving final concentrations below the c.m.c., the micelles will break up to give monomers:
N \, S_{S}(C_{o}) + \text{solvent} = S(c) \tag{1}
\Delta H(1) = \Delta H_{\text{obs}}(\text{initial})

N \, S_{S}(C_{o}) + \text{solvent} = N \, S_{S}(c) \tag{2}
\Delta H(2) = \Delta H_{\text{m}}(c)

N \, S_{S}(c) = S(c) \tag{3}
\Delta H(3) = \Delta H_{\text{demic}} = - \Delta H_{\text{mic}}

(1) = (2) + (3)
\Delta H(1) = \Delta H(2) + \Delta H(3)

When the final concentration in the vessel reaches the c.m.c. region, only part of the injected micelles will break up and, at higher final concentrations, the added micelles are only diluted, as follows:

N \, S_{S}(C_{o}) + \text{solvent} = N \, S_{S}(c) \tag{4}
\Delta H(4) = \Delta H_{\text{mic}}(c) = \Delta H_{\text{obs}}(\text{final})

Process (1) minus process (4) gives

N \, S_{S}(c) = S(c) \tag{5}
\Delta H(5) = \Delta H(1) - \Delta H(4) = \Delta H(2) + \Delta H(3) - \Delta H(4)
\Delta H(5) = \Delta H_{\text{mic}}(c) + \Delta H_{\text{demic}} - \Delta H_{\text{mic}}(c)

This means that

\Delta H_{\text{obs}}(\text{initial}) - \Delta H_{\text{obs}}(\text{final}) = \Delta H_{\text{demic}} + \{\Delta H_{\text{m}}(c) - \Delta H_{\text{m}}(c)\} \tag{6}

The difference between \Delta H_{\text{obs}}(\text{final}) extrapolated forward to the c.m.c and \Delta H_{\text{obs}}(\text{final}) extrapolated back to the c.m.c. will give a value of \Delta H_{\text{demic}} valid at the c.m.c.\(^{10}\) The dilution enthalpies within the bracket will refer to the same total concentration, that is the c.m.c., and as the concentration of micelles is low, the difference will be small and is ignored. The error introduced by this assumption is negligible compared to the uncertainty introduced in the extrapolation of measured \Delta H_{\text{mic}}(c) back to the c.m.c., see below. It is important to note that \Delta H_{\text{obs}} from consecutive additions of small amounts of concentrated amphiphile solution are differential enthalpy changes that, in case the additions are small, can be regarded as approximations of partial molar enthalpies of dilution.

Figure 1. A change of temperature from 25 to 35 °C will give rise to water at 15 °C and 25 °C. Data taken from reference 37.

Before discussing further how to calculate \Delta H_{\text{mic}} as well as the c.m.c. we must define what we mean by the c.m.c. The concept of a critical micellization concentration is not well defined but has its most precise interpretation within the (pseudo)phase separation model. The definition of c.m.c. within the framework of other models is less clear.\(^{12,13}\) The book by Evans and Wennerström \(^{11}\) is recommended for study as it gives an authoritative but accessible discussion of various models for micelle formation.

The plot in Figure 2a shows how the fraction \(f_{\text{mic}} = \frac{d \{N[S_{S}]\}}{dc_{r}}\) that forms micelles varies with the total surfactant concentration, \(c_{r}\), when an incremental amount of amphiphile is added, for various values of the aggregation number N.\(^{14}\) The amphiphile concentration is normalized to the c.m.c. The curve for \(N = 20\) represents the behavior at true phase separation. For \(N = 100\), the break is sharp and within a very small concentration range \(f_{\text{mic}}\) will shift from 0 (= no micelles form) to 1 (= all added amphiphile gives micelles). For \(N = 20\), the rise in \(f_{\text{mic}}\) is still fairly steep but the bend in the curve is fairly wide and at twice the c.m.c. a significant fraction of added amphiphile stays as monomer. The smaller N is, the wider the range...
where \( f_{\text{mic}} \) has values between 0 and 1. For \( N = 10 \), \( f_{\text{mic}} \) has still not reached 0.95 at five times the c.m.c., that is 5% of added amphiphile dissolves as monomers.

\[
\Delta H_{\text{obs}} = (1 - f_{\text{mic}}) \Delta H_{\text{dil}} + \Delta H_{\text{mic}}
\]  

(7)

In the beginning all added micelles break up to monomers and \( f_{\text{mic}} \) is zero. In the c.m.c. region a fraction \( (1 - f_{\text{mic}}) \) will change into monomers while a fraction \( f_{\text{mic}} \) will remain in micellar form. The steepness of the titration curve (normalized to the c.m.c.) is an indication of the cooperativity of the aggregation process, \textit{i.e.} of the aggregation number \( N \). The curve for \( \text{C}_{8}\text{EO}_{4} \) closely resembles the curve in Figure 2a for \( N = 20 \). In Figure 2a, the c.m.c. is defined as the concentration where 1% of surfactant is in micellar form. The concentration at the crossing point in Figure 2b between extrapolated initial and linear ascent lines will be close to the c.m.c. defined in this way. It will be the concentration where the start of formation of micelles is detected. However, the c.m.c can be defined and derived in other ways from calorimetric titration curves. The inflection point in the titration curve can be chosen as a measure of the c.m.c.\textsuperscript{16} This will be close to the recommendation in reference 13 that “A good measure of this concentration (c.m.c.) is where an added monomer is as likely to enter a micelle as to remain in solution” that is at \( f_{\text{mic}} = 0.5 \). The concentration at the intersection of the pre- and post-micellar tangents in the curve of the cumulative enthalpy changes, that is the integral enthalpies of dilution, has also been denoted the c.m.c.\textsuperscript{17} We recommend that the c.m.c is determined as the concentration at the inflection point in the calorimetric titration curves.

For large \( N \), say above 50, and accordingly low c.m.c., values of c.m.c. defined in either way will be very close and the difference insignificant compared to experimental uncertainties. For such systems, the (pseudo) phase separation model usually suffices for a (basic) thermodynamic description. In this model the c.m.c is simply the saturation concentration of surfactant in monomer form.

However, for smaller \( N \) different ways to define the c.m.c. will give numerical values that differ significantly compared to experimental uncertainties. For \( \text{C}_{8}\text{EO}_{4} \) as shown in Figure 2b, the difference will be of the order of 1 mmol kg\(^{-1} \), that is, significantly larger than the experimental uncertainty. Thus, care should be taken when reporting to describe how values of c.m.c have been derived.

The variable \( f_{\text{mic}} \) in Figure 2a was calculated from the mass action law model for micelle formation, also named the closed-association model in reference 13.

\[
N S = S_a K_N = [S_a]/[S]^N
\]

(8)

This model gives a good description of basic features of micelle formation of nonionic amphiphiles such as \( \text{C}_{8}\text{EO}_{4} \). In dilute solution of nonionic surfactants, the activities of the solute species can be approximated with concentrations. From fits of this model to calorimetric titration curves, values of c.m.c, \( \Delta H_{\text{mic}} \) and aggregation number \( N \) can be
The shape of the calorimetric titration curve will depend on the aggregation number \( N \), the size distribution of the micelles and on the purity of the sample. The curves are S-shaped but, as Figure 2 shows, they do not need to be symmetric. This figure depicts micelle formation of a pure homologue of a nonionic amphiphile \((C_3\text{EO}_4)\) with an aggregation number of just above 20. If the sample contains impurities of other homologues or other impurities this will influence the aggregation process and change the shape of the calorimetric titration curve. Triton-X100 has a low c.m.c., 0.27 mmol kg\(^{-1}\), but the micellization range is large and does not reflect the large aggregation number \((N > 100)\) due to the presence of homologues with varying ethylene oxide contents.\(^{15}\)

Micelle formation of ionic surfactants is more complicated. It can be described as an equilibrium between charged surfactant ions \( S^-\) and counterions \( B^+\) and micelles \( S_N^+\):

\[
N \ S^− + (N − P)B^+ = S_N^{−−P}
\]

\[K_N = ([S^{−−P}] / ([S^−] [B^+]^N))^{−P}\]

For large aggregation numbers, say above 50, and accordingly fairly low c.m.c., the titration curves will resemble \( f_{\text{mic}} \) in Figure 2a, with a sharp rise at a certain concentration in the same way as for nonionic amphiphiles.

While the monomer concentration of nonionic amphiphiles above the c.m.c will be fairly constant, the monomer concentration for ionic amphiphiles decreases above the c.m.c. This is because the product \([S^−][B^+]\) remains constant above the c.m.c but as the concentration of unbound \( B^+ \) increases with increasing total amphiphile concentration, \( [S^−] \) decreases, leading to an increase in micelle concentration.\(^{19}\) The quantitative description of the micelle formation process is difficult using the mass action law model.\(^{15}\) The most comprehensive treatment has been made by Woolley and Burchfield\(^{20,21}\) in their extensive study of the thermodynamic properties of alkyltrimethylammonium bromides. Archer has studied how values of \( \Delta H_{\text{mic}} \) obtained from various models are influenced by various assumptions about, for instance, aggregation number, counterion binding and ion interaction parameters.\(^{22}\) His comparison illustrates that similar models but slightly different assumptions can give large differences between derived values. A more direct method with fewer adjustable parameters is based on the treatment of the electrostatic interactions using the Poisson–Boltzmann equation.\(^{11,13,23-25}\)

### 3.1.1. How to derive \( \Delta H_{\text{mic}} \)

We start with nonionic amphiphiles. Relation (6) shows that if we extrapolate the (differential) dilution enthalpies below and above the c.m.c. to the c.m.c., the difference is:

\[
\Delta H_{\text{obs}}(\text{initial at c.m.c.}) − \Delta H_{\text{obs}}(\text{final at c.m.c.}) = \Delta H_{\text{demic}} = − \Delta H_{\text{mic}} \quad (11)
\]

This value is the enthalpy of formation of micelles at the c.m.c. from monomers at the same concentration. At the c.m.c., the concentration of micelles will be small so the (differential) dilution enthalpies just below and above the c.m.c. will be nearly the same. Note that \( \Delta H_{\text{mic}} \) is independent of the titrant concentration. It should be kept in mind that \( \Delta H_{\text{mic}} \) is a differential enthalpy change.

### 3.1.2. Pre-micellar region

Usually, the observed dilution enthalpies in the pre-micellar region are not constant but show an endothermic slope with increasing concentration. In the case of \( C_3\text{EO}_4 \) the slope was 80 dm\(^3\) kJ mol\(^{-2}\) and did not vary with temperature in the range 10 to 40 °C.\(^{15}\) Charged amphiphile ions show the same behavior. For SDS\(^{14}\) the slope in the pre-micellar region was found to be 124 dm\(^3\) kJ mol\(^{-2}\) and 102 dm\(^3\) kJ mol\(^{-2}\) for lithium perfluorononanate\(^{26}\) and again not varying with temperature. The slope increases with the length of alkyl chains and the increase in hydrophobicity. This nonideality in the pre-micellar region is ascribed to pairwise interaction between the hydrophobic chains.\(^{27,28}\) Usually, \( \Delta H_{\text{obs}} \) varies linearly with concentration and the short extrapolation to the c.m.c. does not introduce any significant uncertainty in \( \Delta H_{\text{mic}} \).

As micelles cannot exist in an infinitely dilute solution it is not meaningful to attempt to derive a “standard \( \Delta H_{\text{mic}} \) ” by extrapolating the dilution enthalpies in the pre-micellar region to zero concentration.

### 3.1.3. Post-micellar region

For nonionic surfactants with large aggregation numbers, \( N > 50 \), and accordingly low c.m.c., \( \Delta H_{\text{obs}} \) is expected not to vary significantly above the c.m.c. as there will be no further break up of micelles and, at a low total amphiphile concentration just above the c.m.c., dilution effects will be small. Extrapolation of \( \Delta H_{\text{obs}} \) back to the c.m.c will not introduce any significant uncertainty. At concentrations well above the c.m.c. secondary changes such as micellar growth may take place that may give measurable enthalpy effects.

In systems with lower aggregation numbers the situation is different. Figure 2b shows differential enthalpies of dilution of \( C_3\text{EO}_4 \) as a function of molality at 25 °C. As...
seen in the figure, there is a significant slope in $\Delta H_{\text{obs}}$ above the c.m.c. However, this slope is not due to dilution effects but to a continued break up of micelles. Still, at four times the c.m.c. a small but significant fraction of added micelles break up to monomers. Therefore, we must conclude that values of the enthalpy of micelle formation: 

$$\Delta H_{\text{mic}} = \Delta H_{\text{obs}} \text{ (final at c(\alpha=0))} - \Delta H_{\text{obs}} \text{ (initial at c.m.c.)}$$

(12)

The difference between the observed dilution enthalpy at this concentration, $\Delta H_{\text{obs}} \text{ (final at c(\alpha=0))}$, and the initial dilution enthalpy extrapolated to the c.m.c., $\Delta H_{\text{obs}} \text{ (initial at c.m.c.)}$, will give the correct value for the enthalpy of micelle formation:

$$\Delta H_{\text{mic}} = \Delta H_{\text{obs}} \text{ (final at c(\alpha=0))} - \Delta H_{\text{obs}} \text{ (initial at c.m.c.)}$$

(12)

The value of $\Delta H_{\text{mic}} = -5.1 \text{ kJ mol}^{-1}$ is ca. 10% smaller than $\Delta H_{\text{op}}$. (In case c.m.c is defined as the concentration at the inflection point, the difference between $\Delta H_{\text{op}}$ and true $\Delta H_{\text{mic}}$ will be about the same.)

Without a detailed analysis using a theoretical model based on the Poisson-Boltzmann equation or a more advanced treatment or an elaborated mass-action law model, it is not possible to evaluate the contribution from the additional micelle formation in the post-micellar region. Therefore, we must conclude that values of the enthalpy of micelle formation derived from extrapolation of post-micellar dilution enthalpies will give values of $\Delta H_{\text{op}}$ that must be considered estimates of $\Delta H_{\text{mic}}$. This discussion applies to micelle formation in pure water. In solutions with extra salt the variation of $\Delta H_{\text{obs}}$ with amphiphile concentration is much smaller as the presence of extra electrolyte will reduce dilution effects and suppress the decrease in monomer concentration. While titration curves show significant slopes above the c.m.c., values of $\Delta H_{\text{obs}}$ become constant close to the c.m.c in 0.1 mol dm$^{-3}$ NaCl solution. (The presence of extra salt also lowers the c.m.c and changes $\Delta H_{\text{mic}}$.)

For ionic amphiphiles with low aggregation numbers, say N of 10 to 15 or lower, it will not be possible to derive reliable estimates of $\Delta H_{\text{mic}}$ directly from the titration.
curves. At the c.m.c. the demicellization reaction is not complete but will continue well above the c.m.c and it is not possible to determine where demicellization ends, cf. Figure 2. The micelle formation process needs to be modeled using a model based on the Poisson-Boltzmann equation or a mass-action law model in order to allow the determination of a reasonable value of \( \Delta H_{\text{mic}} \). The addition of extra salt will promote the aggregation and reduce dilution effects but it will change the aggregation properties from those in water.

It is also necessary to consider the concentration of monomers in the titrant solution. If \( \Delta H_{\text{mic}} \) is calculated from the total concentration of surfactant and a significant fraction of the surfactant is in the form of monomers, the value will be in error. From what was said above, it is clear that it is not straightforward to calculate the monomer concentration, particularly not for ionic amphiphiles. In 0.08 mol dm\(^{-3}\) SDS, that is 10 times the c.m.c., the monomer concentration is still of the order of 0.004 mol dm\(^{-3}\), that is, about 5% of SDS is in monomer form. Neglect of the presence of monomers will give an error of 5% in the derived value of \( \Delta H_{\text{mic}} \). If instead the monomer concentration is assumed to equal the c.m.c, the error will be about 10%. Thus, it is necessary to use a high concentration of surfactant in the titrant solution, above 20 times the c.m.c, in order to derive reliable values of \( \Delta H_{\text{mic}} \), unless the monomer concentration is calculated and corrected for.

In summary, enthalpies of micelle formation, \( \Delta H_{\text{mic}} \), can be derived from calorimetric titration curves of consecutive additions of small amounts of micellar solution. The observed differential enthalpy changes before and after the c.m.c are extrapolated to the c.m.c and the difference equals \( \Delta H_{\text{mic}} \), provided the aggregation number is large, say above 50. This will give reliable \( \Delta H_{\text{mic}} \) values for nonionic amphiphiles. For ionic amphiphiles values of \( \Delta H_{\text{mic}} \) derived in this way may contain contributions from additional formation of micelles above the c.m.c.

For amphiphiles with lower aggregation numbers, extrapolation of \( \Delta H_{\text{mic}} \) from just above the c.m.c. back to c.m.c. can give erroneous values of \( \Delta H_{\text{mic}} \) due to an incomplete aggregation reaction. In the case of nonionic amphiphiles the aggregation can be modeled with sufficient accuracy by the mass action law model assuming a constant aggregation number \( N \) and approximating activities with concentrations. For ionic amphiphiles the change in monomer concentration above the c.m.c needs to be modeled using a mass action law model or a Poisson-Boltzmann approach. When reporting results, it is important to describe how values of c.m.c. and \( \Delta H_{\text{mic}} \) were derived. When using values from the literature it is important to find out what they represent, that is, how they were derived.

### 3.2. Surfactants and polymers

Systems containing surfactants and water-soluble polymers are of great interest both for their widespread applications and for their inherently interesting properties. Such systems have long been subject to intensive research and an introduction to and overview of the field can be found in references 33 and 34. The use of titration calorimetry is more recent but as commercial titration microcalorimeters are now available, the method has become more attractive for studies of surfactant-polymer systems. In the following, we will discuss some practical considerations when using titration calorimetry to study such systems. We will start to discuss systems containing nonionic water-soluble polymers, first linear homopolymers, then hydrophobically modified polymers, followed by self-aggregating block copolymers. Then we will discuss studies of surfactant interaction with charged polymers, that is, with polyelectrolytes.

#### 3.2.1. Surfactants and homopolymers

The most studied surfactant–polymer system is SDS and poly(ethylene oxide), PEO, and that applies also to calorimetry.\(^{15-38}\) When SDS is added to a PEO solution, the self-association of SDS is facilitated by the presence of the polymer and cooperative aggregation starts at a critical aggregation concentration, c.a.c, that is lower than the c.m.c. A typical titration curve from addition of concentrated (10 mass %) SDS to a dilute PEO solution at 25 °C is shown in Figure 4a. The molar mass of PEO was 1.5 × 10\(^6\) g mol\(^{-1}\) and the concentration 0.23 mol repeat unit kg\(^{-1}\) (0.1 mass %). At this temperature \( \Delta H_{\text{mic}} \) (at c.m.c) of SDS is small (−0.2 kJ mol\(^{-1}\)) so the dilution curve in water shows only a change of slope at the c.m.c. Differences between the titration curve in the polymer solution and the dilution curve in water are dominated by SDS-PEO interactions. The slope of the curve in the PEO solution starts to deviate from the dilution curve in water above 3.5 mmol kg\(^{-1}\) SDS to give a pronounced endothermic peak followed by a broad and shallow exothermic one. Then the curve joins the dilution curve at about 20 mmol kg\(^{-1}\). The onset of aggregation of surfactant in the presence of polymer is characterized by a critical aggregation concentration, c.a.c. As for c.m.c, there is no generally agreed way to evaluate c.a.c. It can be defined as the concentration at the start of the endothermic peak and can be determined as the concentration at the crossing point between the extrapolated dilution curve and the linear ascent of the peak.\(^{36-38}\) This definition of the c.a.c. as the start of aggregation differs from the usual definition of the c.m.c. as the concentration at the inflection point in the titration curve that is midway through the aggregation process. However, the shape of the titration curves of addition of
surfactant to polymer solution vary with temperature and the system studied and the concentration where the titration curve in polymer solution starts to deviate from the dilution curve in the same solvent is the most practical choice, see Figures 4b and 4c. Figure 4b shows a titration curve of SDS in PEO solution at 15 °C and 4c the results of titrations at 35 °C. At 15 °C ΔH_{mic} is 4.8 kJ mol^{-1} and at 35 it is −5.4 kJ mol^{-1}. The initial endothermic peak has decreased at 35 °C and has completely vanished at 45 °C. At the same time the subsequent shallow exothermic peak disappears and the curve in the polymer solution will join the dilution curve in water from the endothermic side. At a second critical concentration, denoted c_{2}, the influence of the polymer on the aggregation of surfactant in the calorimeter cell ceases, the free monomer concentration reaches the c.m.c and free micelles start to form. We define c_{2} as the concentration where the titration curve in polymer solution joins the dilution curve in water. The value of c_{2} increases in proportion to increasing polymer content. It is a less well-defined concentration and derived values will be quite uncertain. The pronounced features of the titration curve show that the interaction between SDS and PEO is complex and goes through different stages. Similarly shaped titration curves have been observed for other polymer–SDS systems and for sodium dodecylbenzenesulfonate and poly(vinylpyrrolidone) (PVP) at ambient temperatures, where ΔH_{mic} of the surfactant is close to zero. The shape of the titration curves will change considerably if the temperature changes because both ΔH_{mic} and surfactant–polymer interactions vary strongly with temperature. However, it is still possible to estimate values for the c.a.c. and c_{2} as the concentration where the curve in the polymer solution starts to deviate from the curve in water and where the two curves join again. The value of c.a.c. is important because it indicates the free energy change for surfactant-polymer interactions. The decrease in free energy for surfactant aggregation in the presence of polymer can be estimated from: ΔΔG_{agg} = RT ln(c.a.c./c.m.c.). For “true” polymers, as in the case of PEO with molar masses above about 4000 g mol^{-1}, the value of c.a.c. is independent of polymer chain length and concentration. Before we continue the discussion we will look in more detail at the events when SDS is added to PEO in solution in order to get a better description of the titration curves. We will refer to experiments giving the curves shown in Figure 4. The concentration of the SDS solution in the syringe was 10 mass % so the monomer concentration is negligible and the PEO concentration was 0.1 mass %. In the first few injections, that give final concentrations below the c.a.c., the processes will be the same as described by equations (1) to (3). However, the observed differential enthalpies of dilution ΔH_{dil}(c_{k}) differ somewhat from those in pure water. The difference indicates a weak endothermic interaction between SDS monomers and polymer chains. When the total surfactant concentration increases to above the c.a.c., the added micelles will break up to monomers and a fraction β will aggregate on the polymer while the fraction (1−β) stays in non-aggregated form in solution: N S_{N}(c_{0}) + P(c_{k-1}) = (1−β) S(c_{k}) + β (M S_{M} P(c_{k})) (13) ΔH(13) = ΔH_{dil}(c_{k}) + (1−β) ΔH_{demic} + β ΔH_{aggM}

Here S(c_{k}) denotes monomeric amphiphile of concentration c_{k} and S_{M} P(c_{k}) is the amphiphile in the aggregated form of the concentration after the k^{th} injection, M is the aggregation number of polymer-bound aggregates
formed at this concentration and P indicates polymer. The aggregation number \( M \) will increase with increasing total concentration and the monomer concentration also increases. Above \( c_\alpha \), the free monomer concentration has reached the c.m.c. and the added micellar solution will only be diluted, see equation (4). The observed enthalpy change will be \( \Delta H_{\text{obs}}(c_k) \) at the final concentration \( c_k \).

In order to evaluate the (differential) enthalpy change for aggregate formation, \( \Delta H_{\text{agg}M} \), we must be able to evaluate the extent of binding, \( \beta \), which means that we must know the binding isotherm. The determination of binding isotherms is more cumbersome than the calorimetric experiments and, therefore, they are usually not known. When \( \Delta H_{\text{demic}} \) is close to zero, as in Figure 4a, the difference between the titration curve in polymer solution and the dilution curve in water at a certain SDS concentration indicates the enthalpy of formation of polymer-bound aggregates at that total concentration. But, as the amount of aggregates formed is not known, we cannot calculate the (differential) molar enthalpy change \( \Delta H_{\text{agg}M} \). However, the features of the curves give qualitative information about the progress of aggregation with increasing concentration.\(^{39,41} \)

In case the binding isotherm has been determined, the differential enthalpy of aggregation, \( \Delta H_{\text{agg}M}^* \) can be calculated as a function of amphiphile concentration. We can elaborate equation (13) to indicate the process during the \( k \)th injection of \( n^{(i)} \) mol of S in micellar solution with concentration \( C_o \):

\[
n^{(i)} S_M(C_o) + n_{k-1} S_{\text{mon}}(c_{k-1}) + n_k S_M P(c_k) \rightarrow n_k S_{\text{mon}}(c_k) + n_k S_M P(c_k) \quad (13a)
\]

The amount of S in monomeric and bound form, respectively, before injection is denoted \( n_{k-1} \) and after injection is \( n_k \). The observed enthalpy change \( q_{\text{obs}} \) consists of enthalpies of demicellization, dilution and aggregation. The fraction \( \beta \) of added surfactant that binds to the polymer is:

\[
\beta = (n_k S_M P(c_k) - n_{k-1} S_M P(c_{k-1}))/n^{(i)}
\]

(14)

The concentration of polymer-bound surfactant before and after injection can be calculated from the binding isotherm.

Now we inject the same amount of micellar S in a solution that already contains monomeric S at a concentration \( c_{k-1} \) so that after the injection the monomer concentration is \( c_k \):

\[
n^{(i)} S_M(C_o) + S_{\text{mon}}(c_{k-1}) \rightarrow n^{(i)} S_{\text{mon}}(c_k) \quad (15)
\]

The observed enthalpy is \( q_{\text{demic + dil}} \). Equation (13a) minus (15) gives:

\[
(n^{(i)} + n_{k-1})S_{\text{mon}}(c_{k-1}) + n_{k-1} S_M P(c_{k-1}) \rightarrow n_k S_{\text{mon}}(c_k) + n_k S_M P(c_k)
\]

(16)

Values of \( \beta \) for the various injections are calculated from the binding isotherm and the differential aggregation enthalpies calculated from

\[
\Delta H_{\text{agg}}^k = \frac{(q_{\text{obs}} - q_{\text{demic + dil}})}{\beta n^{(i)}}
\]

(17)

The value of \( \Delta H_{\text{agg}}^k \) for the \( k \)th injection relates to the total amphiphile concentration \( S(c_{(k)}) = [S_{\text{mon}}(c_k) + S_M P(c_k)] \). The correction for demicellization and dilution of the concentrated micellar solution is determined from dilution experiments where the final concentration of surfactant equals the monomer concentration in the binding experiment.\(^{40} \) The variation of the enthalpy of dilution of the monomeric surfactant with concentration is assumed to be small. The dilution of the polymer solution is assumed to be negligible (this can be checked by blank experiments injecting solvent into polymer solution). \( \Delta H_{\text{agg}}^k \) derived in this way is the differential enthalpy change for the formation of one mole of aggregate from monomers at the conditions of the \( k \)th injection:

\[
S_{\text{mon}}(c_k) = M S_M P(c_k)
\]

(18)

This enthalpy change is also called binding enthalpy. At the second critical concentration \( c_\beta \), the formation of polymer-bound aggregates is complete and they coexist with monomers of concentration equal to the c.m.c. The integral (total) enthalpy change for aggregate formation \( \Delta H_{\text{agg}}^\text{(int)} \) can be estimated without use of binding isotherm as follows. Assume that \( c_\beta \) has been reached after \( Y \) injections of \( n^{(i)} S_M(C_o) \) to give a total volume \( V_Y \). At \( c_2 \) the monomer concentration equals c.m.c. Then,

\[
\Delta H_{\text{agg}}^\text{(int)} = \frac{\sum q_{\text{obs}} - Y q_{\text{demic + dil}}}{(Y n^{(i)} - V_Y (c_{\text{m.c.}}))}
\]

(19)

where \( \sum q_{\text{obs}} \) is the sum of observed enthalpies of the \( Y \) injections, \( q_{\text{demic + dil}} \) is the combined demicellization and dilution correction measured below the c.m.c., cf. equation (15). \( \Delta H_{\text{agg}}^\text{(int)} \) is the enthalpy change for the formation of one mole of aggregated surfactant from monomers over the concentration range from c.m.c. up to \( c_\beta \) (saturation).

The differential enthalpies of formation of aggregates of SDS and ethyl(hydroxyethyl)cellulose (EHEC) vary strongly with the SDS concentration which shows that the character of the SDS aggregates changes as the SDS concentration increases.\(^{40} \) At ambient temperatures, the SDS aggregates initially formed give endothermic enthalpy
changes while the formation enthalpies become exothermic at higher SDS concentrations. Titration curves of SDS into dilute solutions of other uncharged polymers such as PEO and PVP show the same qualitative features.  

Titration calorimetric studies of polymer–surfactant interactions have been made where the titrant solution, in addition to the surfactant, contained polymer of the same concentration as the starting concentration in the calorimetric cell. This is made to avoid dilution of the polymer solution during titration. If the surfactant concentration in the titrant solution is $S(C_p)$ and the polymer content $P$ the mixed titrant solution can be described as $[(1-X) N S_n(C_p) + X M S_m P]$ where a fraction $X$ of the surfactant is bound to the (saturated) polymer. Dilution in water of the mixed titrant solution will give:

$$ (1-X) N S_n(C_p) + X M S_m P + \text{solvent} = S_{\text{molv}} + P + \text{solvent} \quad (20) $$

The observed enthalpy change will contain contributions from both dilution–demicellization and from the break-up of polymer-bound aggregates. The amount of $S$ bound to the polymer may be significant. For instance, in a solution containing 0.1 mol dm$^{-3}$ SDS and 0.1 mass % PEO the concentration of unbound SDS will be about 0.09 mol dm$^{-3}$ and of bound SDS 0.01 mol dm$^{-3}$. As the enthalpy of aggregation usually is not known, it is difficult to extract quantitative information from the results. Provided that the enthalpy of formation of the surfactant aggregates at $c_2$ is close to $\Delta H_{\text{mic}}$ it will be possible to estimate values of c.a.c. and $c_2$.

While anionic surfactants such as SDS interact strongly with neutral synthetic polymers such as poly(vinylalcohol), PVA, PEO, poly(propylene oxide), PPO and PVP, cationic surfactants interact only weakly or not at all. The reason for this difference between anionic and cationic surfactants is not clear.

The interaction between nonionic surfactants and polymers of this type is usually very weak or nonexistent. Brackman et al. were the first to observe that there can be a significant response in titration calorimetric measurements from polymer–surfactant interaction although the decrease in c.m.c. is small. The titration curve from addition of concentrated solution of n-octyl-$\beta$-D-thioglucopyranoside, OTG, to PPO solution differs significantly from the dilution curve in water but the bend in the curve indicating the change from demicellization to aggregation is not shifted much. The authors concluded that the c.m.c. was not significantly lowered. However, the titration curve in polymer solution is shifted about 1 mmol dm$^{-3}$ to lower concentrations, which shows that the aggregation of OTG is influenced by the presence of the polymer and starts at a lower concentration. The double peaks reported by Brackman et al. probably an artifact due to inefficient stirring, as they were not observed by Wang and Olofsson using a different calorimeter with good stirring (see chapter 8 of reference 48). But the titration curves also reveal that there is significant interaction between PPO and OTG at higher concentrations. This indicates that the polymer interacts preferably with micelles of OTG. The nonionic surfactant C$_{12}$E$_8$ interacts in the form of micelles with ethylhydroxyethyl cellulose in aqueous solution and other nonionic surfactants can be expected to interact in the same way as pseudo-polymers. We believe that if the polymer influences the aggregation of a surfactant that will lead to a lowering of the aggregation concentration c.a.c. However, the interaction may arise between surfactant micelles and the polymer and that may have only a minor effect, if any, on the c.a.c. values.

A different kind of polymer–surfactant interaction was observed in a calorimetric study of hexadecyltrimethylammonium bromide, CTAB, and starch polysaccharides. The shape of the titration curves differed from the curves observed for the linear homologues discussed above. Figure 5 shows an enthalpic titration curve from addition of 0.022 mol dm$^{-3}$ CTAB to solutions of amylose from potato at 27 °C. The curve for dilution in water is included. Binding isotherms were determined from careful surface tension measurements. The interaction is strong as shown by low c.a.c. and gave strongly exothermic binding enthalpies that amounted to $-60$ kJ (mol CTAB)$^{-1}$. This is more than six times the value for enthalpy of micelle formation of CTAB, $-9.5$ kJ mol$^{-1}$. In the amylose-CTAB inclusion complex the polysaccharide winds around the alkyl chain of CTAB and, thus, there is no self-aggregation of the surfactant.

The various reported studies of surfactants and polymers show that titration calorimetry gives useful information.

![Figure 5](image-url). Calorimetric titration curve from addition of 22.0 mmol L$^{-1}$ CTAB solution to (○) 0.5 mass %; (□) 0.25 mass %; (△) 0.1 mass % solutions of amylose and to (X) water, at 27 °C. (Adapted from reference 50).
However, the final remark in reference 40 is worth to bear in mind: “Finally, we would like to emphasize the utility of combining measurements of varying techniques and more important the need for good binding data, to the study of such systems.”

When performing calorimetric measurements, it is important to keep in mind that in a calorimetric experiment of, say, addition of surfactant to a polymer solution, the total heat effect caused by this addition will be measured. This means that if side reactions such as ionization or protonation occur, this enthalpy effect will be included. Therefore, it is necessary to keep track of changes in pH when amphiphiles or polymers with ionizable groups such as weak acids or bases are used. The enthalpy changes can be large. For instance the protonation of a primary amino group will give an enthalpy change of the order of ~50 kJ mol$^{-1}$ in water at 25 °C. Poly(ethylene imine), PEI, has primary, secondary as well as tertiary amino groups that can take up protons in aqueous solution. In the study by Winnik et al. of the SDS-PEI system using various experimental methods, the pH was monitored and the extent of protonation found too small to give any significant enthalpy contribution. In that article the authors also review and discuss a number of earlier calorimetric studies of polymer-surfactant interactions.

3.2.2. Surfactants and hydrophobically modified uncharged polymers

Hydrophobically modified water-soluble polymers, HM-polymers, are polymers with hydrophobic groups chemically attached to a hydrophilic polymer backbone. The hydrophobic groups can be attached at the ends of the polymer backbone or the groups can be grafted along the polymer chain. Aqueous HM-polymers are capable of spontaneous aggregation through association of their hydrophobic moieties. The self-aggregation strongly increases the viscosity compared to the unmodified polymer. The self-association can be studied calorimetrically by performing measurements of dilution of concentrated polymer solutions in the same way as studies of micelle formation of surfactants, see section A.

Calorimetric titration curves from addition of surfactant to dilute HM-polymer solution will differ from curves observed for systems discussed in the previous section. Figure 6 shows titration curves from addition of SDS to 0.25 mass % solution of HM-EHEC and parent EHEC and of dilution in water. The degree of nonylphenyl substitution was 1.7%, corresponding to ca. 6.5 groups per molecule. The binding of surfactant started at a much lower concentration than for the parent polymer and was seen as an endothermic displacement of the observed enthalpy. When the SDS concentration exceeds the c.a.c., SDS will start to aggregate on the polymer in a way similar to the unmodified polymer. The effect of the hydrophobic groups is only evident at low SDS concentrations where SDS monomers solubilize in aggregates consisting of the grafted hydrophobic groups. However, as the SDS concentration increases, the HM-aggregates will become charged and disintegrate due to electrostatic repulsion between the DS$^-$ ions and the influence of the hydrophobic groups will fade away as their concentration is low. Above the c.a.c. the binding of DS$^-$ ions becomes more cooperative and resembles aggregation in the unmodified EHEC. Titration curves from addition of SDS to hydrophobically end-capped poly(ethylene oxide)dodecyl ether, \(\text{C}_{12}\text{EO}_{200}\text{C}_{12}\), and the parent PEO showed the same essential features, Figure 7 in reference 57. The addition of the cationic surfactant dodecyltrimethylammonium bromide, DTAB, to the \(\text{C}_{12}\text{EO}_{200}\text{C}_{12}\) polymer solution gave a different titration curve, see Figure 7 in reference 57. The first few injections gave significantly more endothermic enthalpy changes than the dilution in water. The differences decreased with increasing DTAB concentration, and were small at concentrations above the c.m.c. The results indicate that DTAB added in the beginning was solubilized in the \(\text{C}_{12}\) end-group aggregates that probably disintegrated, but showed no evidence of interaction between the surfactant and the PEO backbone at higher DTAB concentrations in accordance with expectation. This behavior will be observed when the main chain of the HM-polymer is so hydrophilic that it cannot induce aggregation of the surfactant. Titration curves from addition of surfactants to HM-polymer solutions can give interesting information about interactions in the systems. When performing experiments on HM-polymer-surfactant systems one should keep in mind that there may be large changes in viscosity that can have a strong influence on the stirring. Bench experiments with transparent cups will show if mixing is satisfactory. If this cannot be made, experiments with varying stirring speed are necessary. As in all studies of complex systems, calorimetric results must be combined with results from other types of experiments in order to gain an understanding of the system.

3.2.3. Surfactants and block copolymers

The most studied block copolymer systems are ethylene oxide-propylene oxide → ethylene oxide, \(\text{EO}_n\text{-PO}_m\text{-EO}_n\), triblock copolymers. In aqueous solution, the copolymers show a complex solubility and aggregation behavior that has been the topic of many studies (see reference 58). The \(\text{EO}_n\text{-PO}_m\text{-EO}_n\) copolymers are surface active and behave like nonionic surfactants in that many of the copolymers
form micelles above the c.m.c. A notable feature of the self-association process is that a small temperature increase at the critical micellar temperature, c.m.t., can give a dramatic decrease in c.m.c. The self-association arises from the limited and temperature dependent solubility of the PO-block that gives aggregates with an essentially water-free hydrophobic core surrounded by more hydrophilic EO blocks. The copolymers are used in a wide range of applications and often together with surfactants. Therefore, block copolymer-surfactant systems have been studied using a variety of methods including ITC and DSC (differential scanning calorimetry). To our knowledge the first report of the use of ITC is the study by Li et al. of the binding of SDS to EO\textsubscript{97}-PO\textsubscript{69}-EO\textsubscript{97} where calorimetry was used in addition to EMF and light scattering. Later studies have been carried out on the interaction between typical triblock copolymers and cationic and nonionic surfactants in addition to SDS, see references 60 to 64.

Figure 6. Calorimetric titration curves at 25 °C from additions of 10 mass % SDS to (C) 0.25 mass % ethylhydroxyethylcellulose (EHEC), (●) 0.25 mass % hydrophobically-modified EHEC and (□) water. (reprinted, with permission from the American Chemical Society, from ref. 56).

Figure 7. Calorimetric titration curves from addition of 10 mass % SDS to 1.00 mass % P123 at 40 °C: (●) in water and (□) in 20 mmol/L NaCl. Also included are the curves for dilution of 10 mass % SDS in water (▲) and in 20 mmol/L NaCl (◇). Letters U and B indicate unimodal and bimodal relaxation time distributions as determined from parallel dynamic light scattering experiments. Adapted from ref. 63.

In addition to give information about enthalpy changes for a process, titration calorimetry can also give kinetic information. In a study of the system C\textsubscript{12}EO\textsubscript{6}-P123 in water at 40 °C, where small portions of concentrated surfactant solution were added to dilute P123, the time to reach equilibrium suddenly increased over a narrow concentration range to 15 to 20 min from a couple of minutes, see Figure 8. The event giving the slow reaction was confirmed by light scattering to be a sphere-to-rod transition of the mixed micelles. No attempt was made to derive quantitative kinetic information from the calorimetric curves.

The block copolymers appear as unimers in solution at temperatures below the c.m.t. The ionic surfactant SDS interacts almost independently at 15 °C with the PO and EO blocks in EO-PO-EO copolymers and show a c.a.c. value ascribed to the PO block that is closely the same as for PPO 2000, about 0.8 mmol dm\textsuperscript{-3}. The calorimetric titration curve from addition of a concentrated SDS solution to a dilute solution of EO\textsubscript{52}-PO\textsubscript{35}-EO\textsubscript{52} shows similar features as the titration curve of a mixture of PEO 2000 and PPO 2000.

3.3. Surfactants and polyelectrolytes: complex formation

Macromolecules carrying ionic groups that dissociate in water (or another ionizing solvent) to give multiply charged polyions and ions of opposite charge are called polyelectrolytes. Systems containing polyelectrolytes and surfactants are common and of great practical as well as scientific interest. Conditions for titration calorimetric studies of interactions between polyelectrolytes and...
nonionic surfactants will resemble studies of ionic surfactants and nonionic polymers as discussed above. As pointed out previously, independent determination of binding isotherms is required in order to make full use of calorimetric results.

Oppositely charged polyelectrolytes are particularly efficient in lowering the aggregation concentration of ionic surfactants, the critical aggregation concentration c.a.c. being usually a factor 100 to 1000 smaller than the c.m.c in pure water. But additions of an aqueous solution of an ionic surfactant to a solution of an oppositely charged polymer generally results in a phase separation due to the low solubility of the complex salt formed by the surfactant ions and the polion. At increased surfactant concentrations the precipitate may “dissolve”. Thus, during a titration experiment where surfactant solution is added to a dilute solution of oppositely charged polyelectrolyte (or vice versa) a precipitate may form that may dissolve as more surfactant is added. The formation of the precipitate and its dissolution will have enthalpic effects. Therefore, before measurements are made on a new system with an unknown phase behavior, it is necessary to find out if precipitation will take place under the conditions of the intended calorimetric titration experiments. Prominent features in titration curves in such a system that appear at concentrations where precipitates form and disappear can then be ascribed to these events. As the system studied is complex, the resulting titration curve can be expected to be complex and difficult to evaluate, as can be seen in Figure 9, taken from reference 68. The article by Skerjanc et al. that reports enthalpy of binding of dodecyl- and cetylpyridinium cations to poly(styrenesulfonate) anion is to our knowledge the first calorimetric study of polyelectrolyte–surfactant interaction. The binding isotherms were determined using surfactant-ion-selective solid-state electrodes. The article reports the kind of information that can be gained from such a study. For instance, they found that although the two surfactants started to bind at the same concentration, $10^{-5}$ mol dm$^{-3}$, the degree of binding for the C$_{12}$-salt ranged from 70 to 99% depending on surfactant and salt concentration, while the C$_{16}$-salt was almost quantitatively bound to the polyelectrolyte. The observed enthalpy changes (expressed per mole of surfactant) were constant between the start of binding up to charge neutralization (and start of phase separation). Quantitative evaluation of enthalpies of binding could be made as the binding isotherms were known. The enthalpies of binding were of the same order of magnitude as the enthalpies of micelle formation for the studied surfactants.

The determination of binding isotherms for polymer-surfactant systems is usually more cumbersome than

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**Figure 8.** (A) Calorimetric titration curves for the addition of 10 mass % C$_{12}$EO$_6$ to (■) 1.0 mass % P123 solution and to (○) water, at 40 °C. (B) ITC raw data for the same experiment, showing that some composite peaks with a fast endothermic process followed by a slower exothermic one (inset shows in more details the peaks indicated by the arrow). Adapted from reference 64.

**Figure 9.** Calorimetric titration curves for the addition of 0.2 mol dm$^{-3}$ SDS into water (●) and into a 0.75 mass % solution of a hydrophobically modified dextran with a cationic pendant group (D40OCT30) (△). Arrows indicate the ascribed critical aggregation concentration (c.a.c.), the charge neutralization concentration (c.n.c.) and the point at which the complex redissolution was observed. Adapted from reference 68.
calorimetric measurements as no generally applicable experimental method with commercial equipment is available. Therefore, it is tempting to try to estimate the binding properties from titration calorimetric measurements by fitting observed enthalpy curves to a model isotherm. Lapitsky et al. report such an attempt to determine isotherms for the systems sodium perfluorononanate-hydroxyethyl cellulose and dodecyltrimethylammonium bromide–sodium polystyrenesulfonate. Their model is based on the Satake–Yang adsorption model. The success is limited and the authors discuss the limitations of the method. Their results show that this polymer-centered adsorption model is insufficient for the evaluation of quantitative binding isotherms from calorimetric titrations on polyelectrolyte-surfactant systems. Starting from a surfactant-centered viewpoint may be more fruitful but neither can a simple closed association (mass action law) model give quantitative predictions of binding isotherms (see chapter 5 from reference 34). More advanced models are needed to describe polymer-surfactant complexation. In our opinion it is not possible, except in very special circumstances, to determine binding isotherms from calorimetric titration curves. For the time being, independent experimental determinations are necessary.

4. Concluding Remarks

In titration calorimetry usually small portions of a concentrated solution of surfactant $R_2$ (or pure $R_2$) are added successively to a solution of reactant $R_1$ or pure solvent at the start of titration in the calorimeter vessel and the enthalpy change $q_i$ is measured. The concentration of $R_1$ increases for each addition and $q_i$ results from the processes that occur in the titration steps. Thus, the measured enthalpy changes are differential enthalpies that, for small concentration changes, approximate partial molar enthalpies. Very useful qualitative information can be obtained from calorimetric titration experiments as calorimetric titration curves can show that events take place and the concentration where they occur. In this way large concentration ranges can be mapped in a limited length of time. This is very useful when designing experiments by other methods that can probe the molecular nature of the processes.

In order to derive quantitative information about aggregation enthalpies, the processes that take place in the titration steps must be identified. In experiments were binding to, for instance, polymers occurs, the knowledge of the binding isotherm is necessary.

Modern commercial titration calorimeters are sensitive so measurements can be made at concentrations that are below the range of other methods.

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