Adaptive Fuzzy Sliding-Mode Control of Wheel Slide Protection Device for ER24PC Locomotive

Abstract
Wheel Slide Protection Devices (WSPD) are employed in railway vehicles to maximize the average of the possible frictional braking force, which is a nonlinear function of the slip ratio of the wheel sets. In this paper, to control the WSPD, a low-order model is presented and un-modeled dynamics are considered as uncertainties. Due to the nonlinear dynamics of the system and presence of uncertainties, Adaptive Fuzzy Sliding-Mode Control (AFSMC) is employed to regulate the slip ratio towards the desired value. The proposed controller employs a Pulse Width Modulation (PWM) technique to generate the braking torque. The second Lyapunov theorem is used to prove the closed-loop asymptotic stability. In the simulations, the switching dynamics of WSPD is considered and the multi-body dynamics method is used for modeling the longitudinal dynamics of ER24PC locomotive. The obtained results reveal that by using the AFSMC method, the slip ratios of wheel sets converge to the reference values. Unlike the conventional method, in which the fluctuations of slip ratio diverge near the stopping time, simulation studies reveal that with the AFSMC method, the stopping time of the locomotive and the fluctuation amplitude of the slip ratios are reduced.

Keywords
WSPD; ER24PC locomotive; wheel-set slip ratio; adaptive fuzzy sliding-mode control; AFSMC.

1 INTRODUCTION
Wheel slide protection device of the trains is the main part of the braking system used to increase the opposite acceleration while cars stability and steer ability are not adversely affected. Thus, with this system, train will stop in shorter distance. In positive and negative acceleration of the train a horizontal force is produced related to the normal force of the surface, imposed by rail to the wheel set. This corresponding force is called rail friction force which changes with rail condition. In a cer-
tain condition of the rail surface, the friction force is a nonlinear function of the slip ratio of the wheel sets. Therefore, a controller should be designed to set the desired value of the slip ratios. However, challenges in project implementation are as follows: 1-nonlinear dynamic behaviour of the train motion, 2- controlling the plant around an unstable set point and 3-sever variations of plant parameters due to changes in rail and cars.

Previously, heuristic knowledge-based (Cheok and Shiomi, 2000; Cocci et al., 2001; Barna, 2012) and model-based methods (Kim et al., 2011) have been employed to control the wheel slide protection device reported in literature. In Cheok and Shiomi (2000), a fuzzy controller is presented for the WSPD. In this controller, the fuzzy rules are determined based on the performed experiments and the knowledge of relevant experts. To evaluate the performance of this controller, the empirical results were compared with the results obtained from a PID controller. By comparing the results for different climatic conditions, they found out that the stopping time and distance were considerably reduced by using the fuzzy controller. This controller has been employed by the Mitsubishi Company. It should be mentioned that, in Pugi et al. (2017), a fuzzy logic controller has been implemented in the traction/braking system of a four-wheeled vehicle under degraded adhesion conditions. In Cocci et al. (2001), to investigate the performance of WSPD, the multi-body dynamics simulations is performed. In this work, they used the control method devised by Trenitalia Company designed based on knowledge of experts. In the mentioned controller, upper and lower bounds are set for the velocities and the accelerations of the wheel sets. Also in Pugi et al. (2006), Hardware In the Loop (HIL) testing of WSPD has been done using MI-6 test rig that is manufactured by Trenitalia and University of Florence. HIL model is able to generate the dynamical behaviour of the simulated train according to the main features of the mechanical and electrical subsystems. In Barna (2012), the longitudinal dynamics of the train is modeled and the pneumatic braking system has been considered as a first-order linear system. Then, to control the WSPD, a fuzzy controller has been presented; and to evaluate its performance, the obtained empirical results have been compared with the results of the method developed by the Knorr-Bremse Company. By reviewing the aforementioned works, it can be concluded that the stability of the heuristic knowledge-based methods has not been investigated.

To design WSPD using model-based control methods, like antilock braking system of road vehicles (Mirzaeinejad and Mirzaei, 2010, 2014), the full-order mathematical dynamic model should be created. Due to the existence of uncertainties, the order of the real plant dynamics increases. So, the stability of the closed-loop model-based control system is affected. The dissimilar friction forces exerted on the wheel sets, the lateral and the vertical vibrations, and severe changes in the wheel-rail friction are examples of plant uncertainties. In this work, a low-order model is presented to design the controller and the unmodeled dynamics are considered as uncertainties.

So, a robust control method should be used to regulate the braking torques. Sliding-Mode Control (SMC) is a robust method that has an appropriate performance to overcome the disturbances and plant uncertainties. SMC is effective when the bounds of disturbances and uncertainties are known (Shim, Chang, and Lee, 2008; Patil et al., 2016; Harifi et al., 2008; Bhandari, Patil, and Singh, 2012). A sliding-mode controller is designed using a presumed upper bound of uncertainties as a control parameter, which may generate large amplitude chatters in the control input. If the uncertainty is in the allowable range of the designed controller, the controller will perform well. But
if the uncertainty exceeds the limits, the system will become unstable or the controller performance will be degraded. To overcome the mentioned problems in the design of SMC, adaptive fuzzy sliding-mode control is proposed in Poursamad and Markazi (2009a) as a model-free controller scheme.

In Lin and Hsu (2003), an adaptive fuzzy sliding-mode controller has been designed for controlling the antilock braking system of road vehicles. In this approach, the adaptation laws are established according to the Lyapunov method. It should be mentioned that, in this work, it is not necessary to know the exact vehicle model and the friction forces.

Several methods of AFSMC were presented based on the estimation of plant parameters (Yoo and Ham, 1998), parameter uncertainties (Hwang and Kuo, 2001), and the robust control term of the SMC (Lhee et al., 2001; Wong and Rad, 2009). Also, AFSMC algorithms are developed to control the nonlinear Multi-Input and Multi-Output (Tong and Li, 2003; Poursamad and Markazi, 2009b; Gholami and Markazi, 2012) and input-delayed systems (Khazaee et al., 2015).

In this research, based on Poursamad and Markazi (2009a, b), adaptive fuzzy sliding-mode PWM controller is designed in direct form. A Takagi-Sugeno fuzzy system estimates the equivalent term of the conventional SMC as a replacement for the ideal controller. Then, a robust controller compensates the difference between the fuzzy and the unknown ideal controller. In this method, the upper bound of uncertainty and the output of the fuzzy system are estimated using an adaptive scheme even when the exact model of the plant is not available. The estimation of the upper bound of uncertainty prevents the excessive switching of the robust part of the controller. The adaptation rules are extracted based on the second Lyapunov theorem. Such adaptations are performed based on the deviations of the closed-loop system from a prescribed sliding surface. In the end, the AFSM controller employs PWM to generate the braking torque.

To demonstrate the performance of the proposed control strategy, AFSMC algorithm is applied to the WSPD for numerical simulations. The multi-body dynamics method is used for simulating the longitudinal dynamics of the ER24PC locomotive. It should be mentioned that the modeled locomotive has been validated using the test data provided by Mapna Locomotive and Siemens Companies. Moreover, random track irregularities and wheel-rail friction force uncertainties are considered. In addition, for comparison, Trenitalia, Knorr-Bremse, and Mitsubishi control techniques are implemented.

This paper is organized as follows. The longitudinal dynamics of the locomotive and the WSPD are modeled in Sections 2 and 3, respectively. In Section 4, the common methods for controlling the WSPD are introduced. In Sections 5 and 6, sliding-mode and adaptive fuzzy sliding-mode controllers are described for the wheel slide protection system. In Section 7, the results are presented and the performance of the considered methods are compared. Finally, the paper is concluded in Section 8.

2 MODELLING THE LONGITUDINAL DYNAMICS OF LOCOMOTIVE

In practice, the locomotive dynamics is very complicated. So, it is impracticable to consider all relevant characteristics of the locomotive when designing the controller. As Kim et al. (2011), Lin and Hsu (2003), Mirzaei and Mirzaeinejad (2012), Mirzaei, et al. (2006), Jing, Liu, and Chen (2011) and Anwar and Zheng (2007), like the road vehicles, the quarter locomotive longitudinal dynamics is considered as a low-order model of the plant (Figures 1 and 2). This model is obtained from a
straight line braking on a flat rail without considering the lateral and vertical motions. Thus, the weight shifting is not considered during braking and the value of friction forces is equal for each wheel set. In addition to the friction forces resulting from the wheel-rail contact (a function of the longitudinal slip ratio of the wheel sets \( \lambda_x \)) \( f_{fr} \), resistance forces \( f_d \) are applied on the locomotive. So, considering the Newton’s laws, the variations in the velocity of locomotive \( v(t) \) and angular velocity of the wheel sets \( \omega(t) \) can be presented using following equations.

\[
\begin{align*}
\dot{m}v &= -f_d(v) - 8f_{fr}(\lambda_x) \\
I_W\dot{\omega} &= -0.5T_{brake} - B_W\omega + R_Wf_{fr}(\lambda_x)
\end{align*}
\]

In Equation (2), \( I_W \), \( R_W \) and \( B_W = 0.25^{-0.01t} \) respectively denote the wheel’s moment of inertia, the wheel radius, and the coefficient of torque damping between the wheels and braking pads. Also, the longitudinal slip ratio of wheel sets \( \lambda_x \) is a function of its angular velocity and the velocity of the locomotive.

\[
\lambda_x = \frac{v - R_W\omega}{v}
\]

The resistant force applied on the locomotive comprises the mechanical \( a_0 + a_1v \) and the aerodynamical resistance \( a_2v^2 \) as well as the resistant forces resulting from path slope \( f_r \), path curva-
ture $f_c$ and travel through a tunnel $f_l$. Thus, the total of these forces $f_d$ is obtained from the following equation (Song and Song, 2010):

$$f_d = a_0 + a_1v + a_2v^2 + f_r + f_c + f_l$$

(4)

2.1 Frictional Forces Exerted on the Wheels

The creep force applied on a wheel $F_{\text{creep}}$ is computed based on the distribution of shear stresses on the wheel-rail contact surface (Polach, 1999, 2005; Leva, Morando, and Colomboani, 2008; Colombo et al., 2014; Li et al., 2007). In this regard, $x$ and $y$ components of the creep force have been taken to be proportional to the longitudinal creep and lateral creep, respectively. The contact surface is considered as elliptical (with $a$ and $b$ assumed as elliptic constants (Polach, 1999)), and the distribution of shear stresses is based on the Hertz contact stress. Considering variable friction coefficient $\mu$ and neglecting the lateral creep, the magnitude of the longitudinal wheel creep force $F_{\text{creep},x}$ and gradient of the tangential stress in the area of adhesion in longitudinal direction $\varepsilon_x$ will be obtained from the following equations (Polach, 2005):

$$F_{\text{creep},x} = f_r = \frac{2Q\mu}{\pi} \left\{ \frac{k_A \varepsilon_x}{1 + (k_A \varepsilon_x)^2} + \arctan(k_S \varepsilon_x) \right\}, \quad k_S \leq k_A \leq 1$$

(5)

$$\varepsilon_x = \frac{1}{4} G \pi a b c_{11} \frac{\mu}{Q \mu} \lambda_x$$

(6)

Where $k_A$, $k_S$, and $Q$ represent reduction factor in the area of adhesion, reduction factor in the area of slip, and the wheel load, respectively. Also, $G$ and $c_{11}$ respectively represent the shear module and the coefficient from Kalker’s linear theory. In the following, the variable friction coefficient $\mu$ is expressed as Equation (7).

$$\mu = \mu_0 \left[ (1 - A) \exp \left[ -B(v - R_W \omega) \right] + A \right], \quad A = \frac{\mu_x}{\mu_0}$$

(7)

Where $\mu_x$ and $\mu_0$ denote the sliding friction coefficient at the sliding speed of infinity and the maximum wheel sliding friction, respectively. $B$ denotes the coefficient of the exponential friction decrease. In Table 1, frictional coefficient values are presented for different rail surface conditions (Polach, 2005). It should be mentioned that, in Meli, Pugi, and Ridolfi (2014) and Meli and Ridolfi (2015), an adhesion model has been presented to improve the accuracy of the modeled friction forces under degraded adhesion conditions. In the new approach, the dissipation of energy at the contact surfaces is considered. This phenomenon has a cleaning effect on the rolling surface that recovers the adhesive forces. This model can be used for more precise evaluation of the WSPD performance.
Now, the longitudinal slip ratio should be brought within a proper range. So that by increasing the friction force applied to the wheels, the locomotive stopping time can be reduced (Figure 3). It has been examined that for each rail condition, $f_{fr}$ is maximized at slip value of approximately 0.1 to 0.2 (Cheok and Shiomi, 2000). The target is to regulate the slip value towards the desired value of $\lambda_{sd} = 0.14$ to compromise between the effective braking and lying near the unstable negative sloped region (Cheok and Shiomi, 2000). However, an optimum value cannot be set that will satisfy all track conditions. In this work, in order to calculate the longitudinal slip ratio of the wheel sets $\lambda_x$, it is assumed that the locomotive velocity can be measured.

3 MODELLING THE ELECTRO-PNEUMATIC BRAKING SYSTEM

The goal of designing a controller is to maintain the slip ratio of wheels, and thus the friction force, within an appropriate range. This is accomplished by tuning the braking torque in each wheel set and by the controller of the electro-pneumatic braking system. Figure 4 shows a schematic view of the electro-pneumatic braking system in a train car (FAIVELEY, 2010). In the electro-pneumatic braking system of the train, the air supply system acts as a first-order system. Thus, the pressure of air coming into the valves of the wheel slide protection system $P_{c_{in}}$ is obtained as follows (Barna, 2012):

$$P_{c_{in}} = P_{c_{max}} (1 - \exp(-0.75t))$$

(8)
In the above equation, \( P_{\text{max}} \) denotes the maximum air pressure generated by the air supply system. In this system, the air supply valve (BV) and the air discharge valve (EV) regulate the pressure of a brake cylinder by supplying more air into it or discharging air from it (Figure 4). In this way, the internal pressure of the brake cylinder \( P_e \) varies as a function of control valve input \( \bar{u}_{EV} \) and \( \bar{u}_{BV} \), as the following equation:

\[
\dot{P}_e = \bar{u}_{EV} \left( -\frac{1}{T_V} P_e \right) + (1 - \bar{u}_{BV}) \left( \frac{1}{T_F} (P_{c_{in}} - P_e) \right)
\]  

(9)

Where \( T_F \) and \( T_V \) denote the air filling and the air venting time constants for the cylinder. In Table 2, the states of the electro-pneumatic valves of the WSPD during increasing, decreasing, or maintaining of the cylinder air pressure are presented. Thus, the cylinder air pressures during air filling \( P_{e_{\text{filling}}} \) and air venting \( P_{e_{\text{venting}}} \) are obtained by (10) and (11), respectively (Barna, 2012).

![Schematic view of the electro-pneumatic braking system in a train car (FAIVELEY, 2010).](image)

**Figure 4**: Schematic view of the electro-pneumatic braking system in a train car (FAIVELEY, 2010).
<table>
<thead>
<tr>
<th>Control Command</th>
<th>EV</th>
<th>BV</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reduction of Pressure</td>
<td>Active ($\bar{u}_{EV} = 1$)</td>
<td>Active ($\bar{u}_{BV} = 1$)</td>
</tr>
<tr>
<td>Maintenance of Pressure</td>
<td>Inactive ($\bar{u}_{EV} = 0$)</td>
<td>Active ($\bar{u}_{BV} = 1$)</td>
</tr>
<tr>
<td>Increase of Pressure</td>
<td>Inactive ($\bar{u}_{EV} = 0$)</td>
<td>Inactive ($\bar{u}_{BV} = 0$)</td>
</tr>
</tbody>
</table>

Table 2: The states of BV and EV valves during increase, decrease and maintenance of cylinder air pressure.

\[
P_{\text{filling}} = P_0 + (P_{\text{in}} - P_0)\left(1 - \exp\left(-\frac{t - t_0}{T_F}\right)\right)
\]

(10)

\[
P_{\text{venting}} = P_0\exp\left(-\frac{t - t_0}{T_V}\right)
\]

(11)

In the above equations, $t_0$ and $P_0$ denote the time and the cylinder air pressure at the onset of air filling and air venting, respectively. Thus, the braking torque $T_{\text{brake}}$ is expressed as follows (Kim et al., 2010):

\[
T_{\text{brake}} = 2A_{\text{eff}}E_b\eta_bR\mu_{\text{brake}}(v_{\text{rel}})P_e
\]

(12)

Where $A_{\text{eff}}$ is the cross section of each cylinder. $E_b$ and $\eta_b$ denote the magnification coefficient and the efficiency of the brake mechanism, respectively. $R$ is the impact point radius of the force applied to the disk and $\mu_{\text{brake}}$ is the coefficient of the friction between the brake pad and the disk. It should be noted that, $\mu_{\text{brake}}$ is a function of the relative velocity between the brake pad and the disk $v_{\text{rel}}$. The pulse width modulation technique is employed to regulate the desired output torque to improve the slip ratio. For this purpose, BV and EV will be simultaneously activated or deactivated. Thus, based on (9) and (12), Equation (13) is derived as follows:

\[
\dot{T}_{\text{brake}} = K_bR\mu_{\text{brake}}\dot{P}_c = K_bR\mu_{\text{brake}}\left[\frac{1}{T_V}P_c + \frac{1}{T_F}(P_{\text{in}} - P_c)\right]\bar{u} - \frac{1}{T_V}P_c
\]

(13)

When increasing the braking torque (air filling), the issued command of $\bar{u}$ will be ‘1’, and when reducing the braking torque (air venting), it will be ‘0’. Now by assuming $T_F = T_V = tau$, the above equation is simplified as

\[
tau.\dot{T}_{\text{brake}} + T_{\text{brake}} = T_{\text{brake max}}\bar{u}
\]

(14)

Therefore, and altogether, the braking system acts as a stable first-order system. Now the goal of designing a controller is to tune the input bandwidth of $\bar{u}$ ($dc$). It should be mentioned that when the input frequency approaches infinity, the following dynamic equation is obtained for the mentioned system:

\[
tau.\dot{T}_{\text{brake}} + T_{\text{brake}} = T_{\text{brake max}}dc
\]

(15)
Thus, by determining bandwidth \( dc \), the value of the braking torque will eventually converge to \( T_{\text{brake max}}.dc \).

4 COMMON METHODS FOR CONTROLLING WHEEL SLIDE PROTECTION DEVICE

4.1 Trenitalia Technique

In the method presented by Trenitalia, the input of the wheel slide protection system is determined based on the velocity and the acceleration values of each wheel set. In this algorithm by specifying two ranges for the velocity and acceleration of wheel sets, the WSPD can be tuned at states of pressure increase, pressure maintenance, and pressure reduction. The mentioned algorithm has been presented in Table 3 (Cocci et al., 2001). In Table 3, \( i \), \( \text{ACC} \) and \( \text{DEC} \) indicate the number of wheel set, the maximum and minimum accelerations of wheel sets, respectively. On the other hand, the variable maximum velocity \( V_{\text{max}} \) and minimum velocity \( V_{\text{min}} \) of wheel sets are determined as follows:

\[
V_{\text{min}} = 0.78v, \quad V_{\text{max}} = 0.90v
\]  

(16)

4.2 Knorr-Bremse Technique

In the method presented by this company, the input of the WSPD is determined based on the absolute slide values and the acceleration of each wheel set (Barna, 2012). For this purpose, by defining the absolute slide of the \( i^{th} \) wheel set as

\[
\sigma_i = v - R_W\omega_i
\]  

(17)

The plane of absolute slide versus car speed is divided into four regions by means of \( \Delta\sigma_1 \), \( \Delta\sigma_2 \) and \( \Delta\sigma_3 \) as follows:

\[
\Delta\sigma_1 = \begin{cases} 
\frac{7v}{60} + 3 & \text{if } v \leq 60 \text{ km/h} \\
10 & \text{if } v > 60 \text{ km/h}
\end{cases}, \quad \Delta\sigma_2 = \begin{cases} 
\frac{9v}{60} + 6 & \text{if } v \leq 60 \text{ km/h} \\
15 & \text{if } v > 60 \text{ km/h}
\end{cases},
\]

\[
\Delta\sigma_3 = \begin{cases} 
\frac{11v}{60} + 9 & \text{if } v \leq 60 \text{ km/h} \\
20 & \text{if } v > 60 \text{ km/h}
\end{cases}
\]  

(18)

So in Table 4, the decision table of the Knorr-Bremse controller is presented. In Table 4, symbols U3, U2, U1, H, P1, P2 and P3 indicate various levels of air pressure supplied to the system. Data sampling is carried out and then the product of an inverse unit step function and \( u_i / |u_i| \) is applied to the system as input. In the inverse unit step function, the bandwidth \( dc \) is equal to 0, 0.33, 0.5 and 1 for the value of \( |u_i| = 0, 1, 2 \) and \( 3 \), respectively. Also, note that in applying a new input to the system, the negative and positive signs will lead to pressure reduction and pressure increase in system lines, respectively. The number zero (0) will cause no pressure change.
In this method, a fuzzy controller is employed to control the WSPD (Cheok and Shiomi, 2000). The structure of this controller has been designed using the reference measured data and the experimental knowledge of experts. In this controller, the values of absolute slide and its derivative is chosen as the inputs of the system, and the maximum cylinder pressure (%) is considered as its output. By determining the membership functions of the system inputs and output in the form of Figure 5, the fuzzy rules are expressed as in Table 5. It should be noted that in this approach, deduction based on separate rules, Max-Product rule implication, and the center average defuzzification method are used to reduce the computational complexity. Now, the data is sampled and the achieved output is applied to the valves of the WSPD as the bandwidth of the PWM signal.

**Table 3**: The decision table presented by Trenitalia.

<table>
<thead>
<tr>
<th>$\frac{d}{dt}(R_{W_{0i}})$ $(\text{km/h/s})$</th>
<th>$\sigma_i$</th>
<th>$\Delta \sigma_1 &lt; \sigma_i &lt; \Delta \sigma_2$</th>
<th>$\Delta \sigma_2 &lt; \sigma_i &lt; \Delta \sigma_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-10$</td>
<td>$-19.8 \rightarrow -2.52$</td>
<td>$18.36 \rightarrow 18.36$</td>
<td>$0.36 \rightarrow 19.8$</td>
</tr>
<tr>
<td>$-1$</td>
<td>$H \ (u_i = 0)$</td>
<td>$H \ (u_i = 0)$</td>
<td>$U3 \ (u_i = -3)$</td>
</tr>
<tr>
<td>$0$</td>
<td>$H \ (u_i = 0)$</td>
<td>$P3 \ (u_i = 3)$</td>
<td>$U3 \ (u_i = -3)$</td>
</tr>
<tr>
<td>$1$</td>
<td>$U1 \ (u_i = -1)$</td>
<td>$P2 \ (u_i = 2)$</td>
<td>$U3 \ (u_i = -3)$</td>
</tr>
<tr>
<td>$2$</td>
<td>$U2 \ (u_i = -2)$</td>
<td>$H \ (u_i = 0)$</td>
<td>$U3 \ (u_i = -3)$</td>
</tr>
<tr>
<td>$3$</td>
<td>$U3 \ (u_i = -3)$</td>
<td>$U3 \ (u_i = -3)$</td>
<td>$U3 \ (u_i = -3)$</td>
</tr>
</tbody>
</table>

**Table 4**: The decision table of the controller developed by Knorr-Bremse.

**4.3 The Technique Presented by Mitsubishi**

In this method, a fuzzy controller is employed to control the WSPD (Cheok and Shiomi, 2000). The structure of this controller has been designed using the reference measured data and the experimental knowledge of experts. In this controller, the values of absolute slide and its derivative is chosen as the inputs of the system, and the maximum cylinder pressure (%) is considered as its output. By determining the membership functions of the system inputs and output in the form of Figure 5, the fuzzy rules are expressed as in Table 5. It should be noted that in this approach, deduction based on separate rules, Max-Product rule implication, and the center average defuzzification method are used to reduce the computational complexity. Now, the data is sampled and the achieved output is applied to the valves of the WSPD as the bandwidth of the PWM signal.

**Figure 5**: Membership functions of (a) absolute slide, (b) deceleration of wheel set and (c) the brake pressure in the Mitsubishi fuzzy controller (Cheok and Shiomi, 2000).
It should be mentioned that, for implementing the common algorithms, data sampling is performed at 100 ms time intervals to generate the input for the WSPD. But by reviewing the aforementioned works, it is concluded that the stability of the heuristic knowledge-based methods have not been investigated at all. It should be mentioned that fuzzy control method has been used for tire antilock braking systems in vehicles (Moallem et al., 2006; Cabrera et al., 2005).

5 SYSTEM CONTROL BY MEANS OF SLIDING-MODE METHOD

By taking the derivative of (3) and using (1) and (2), the equation for the changes of the longitudinal slip ratio of the wheel sets is obtained.

$$\frac{dx}{dt} = \frac{F(x, t)}{v} - \frac{0.5T_{brake} - B_W \omega + R_W f_p(\lambda_x)}{I_W} + \frac{R_W \omega}{v^2} \left[ -f_d(v, t) - 8f_p(\lambda_x) \right]$$

In the above equation, the braking torque is considered as the input of the system, and the longitudinal slip ratio is taken as its output. Now by assuming uncertainties in the system structure such as severe changes in the friction, the car masses, and inertia properties, the above equation will be written as

$$\dot{x}_e = [F(x_e, t) + \Delta F(x_e, t)] + [G + \Delta G]T_{brake}(t)$$

To design the sliding-mode controller, it is assumed that $|\delta| \leq W$. By defining the tracking error and the sliding surface of the wheel sets as

$$\lambda_x(t) = \lambda_{x, d} - \lambda_x(t)$$

$$s(t) = K_P \lambda_x(t) + K_I \int_0^t \lambda_x(\tau) d\tau, \ K_P, K_I > 0$$

and based on the sliding-mode method (Slotine and Li, 1991), the control input (braking torque) is applied as follows:

Table 5: Fuzzy rules in the controller presented by Mitsubishi (Cheok and Shiomi, 2000).
Where the equivalent control term $u_{eq}$ is obtained by $\dot{s} = 0$ and the robust control term $u_{ht}$ compensates the uncertainties effect. In the designed sliding-mode controller, $u_{eq}$ is a function of $F$ and $G$ (Equation (23)). Therefore, $u_{eq}$ is computed using the values of friction coefficient and the locomotive parameters. In the SMC, the uncertainty upper bound $W$, which include the unknown dynamics and parameter variations, must be available. However, it is difficult to obtain $W$ for the plant. The disadvantages of the SMC are fully dependency on dynamic model and the need for uncertainty upper bound $W$.

Chattering phenomena can be improved by using $sat$ function instead of $sgn$. It should be mentioned that the boundary layer thickness of $sat$ function is equal to $\Phi$. By choosing the Lyapunov function as

$$V = \frac{1}{2} s^2$$

In the case in which $sat$ function is equal to $sgn$ function (outside the boundary layer), the derivative of $V$ is written as follows:

$$\dot{V} = s \times \dot{s} = s \times (K_p \lambda + K_I \lambda) = K_p s \times (-\delta - W |s| / s)$$
$$= -K_p s \times \delta - K_p W |s| \leq K_p \delta \times |\delta| - K_p W |s| = -K_p (W - |\delta||s| \leq 0$$

Thus, the designed sliding-mode controller will ensure the stability of the system according to the Lyapunov stability criterion (Slotine and Li, 1991). Now, to apply the input to the actuator, the computed torque must be converted to its corresponding bandwidth.

$$dc(t) = \frac{u(t)}{T_{brake_{max}}}$$

6 PROPOSED ADAPTIVE FUZZY SLIDING-MODE CONTROLLER

By assuming all the parameters of the system (19) to be known, the ideal control input $u^*$ is obtained from the following equation:

$$u^* = G^{-1} \left[ -F(\lambda, t) + \frac{K_I}{K_p} \lambda_e (t) \right]$$

By substituting (27) into (19), it is revealed that the tracking error is stable and it changes according to the following differential equation:
$$\dot{\lambda}_e(t) + \frac{K_I}{K_P} \lambda_e(t) = 0$$  

(28)

Since the implementation of $u^*$ is not practically possible, the ideal control input is approximated by an ideal fuzzy system $u_{\text{fuzz}}$. Thus, there is no need to determine the values of friction forces and the locomotive parameters. After choosing a sliding surface such as (22), a Takagi-Sugeno (TS) fuzzy system with sliding surface input $s$ and output $u_{\text{fuzz}}$ is considered as follows:

**Rule r**: If $s$ is equal to $A^r$, then $u_{\text{fuzz}}$ will be equal to $b^r$ ($r = 1, \ldots, n_r$).

$b^r$ is the fuzzy singleton output associated with rule $r$, and $A^r$ is a fuzzy set, determined iteratively by a Gaussian membership function, as follows:

$$\mu_{A^r}(s) = \exp \left[-\frac{(s-c^r)^2}{\sigma^r}\right]$$  

(29)

![Figure 6: Membership functions for the sliding surface input.](image)

In the above equation, $c^r$ and $\sigma^r$ denote the center and width of a membership function, respectively. The selected membership functions are shown in Figure 6. By employing the singleton fuzzifier, the product inference, and the center average defuzzifier, the output of the fuzzy system is obtained as

$$u_{\text{fuzz}} = \frac{\sum_{r=1}^{n_r} b^r \mu_{A^r}(s)}{\sum_{r=1}^{n_r} \mu_{A^r}(s)}$$  

(30)

By defining the rule $r$ as

$$w^r = \frac{\mu_{A^r}(s)}{\sum_{r=1}^{n_r} \mu_{A^r}(s)}, \quad r = 1, \ldots, n_r,$$  

(31)
the output of the fuzzy system will be rewritten as (32).

$$u^{fuz}(s,b) = b^T w, \quad b = \left[ b_1, \ldots, b_n \right]^T, \quad w = \left[ w_1, \ldots, w_n \right]^T$$

Now, by considering the approximation error $\xi$, the ideal controller $u^*$ can be estimated from the following equation:

$$u^* = u^{fuz} + \xi = b^T w + \xi \quad (33)$$

The approximation error is presumed to be bounded.

$$|\xi| \leq \psi \quad (34)$$

Since the optimal values of $b$ and $\psi$ may not be practically known, therefore adaptive method is used to its evaluation. So, $\hat{u}^{fuz}$ is presented for approximating ideal controller $u^*$.

$$\hat{u}^{fuz}(s,\hat{b}) = \hat{b}^T w \quad (35)$$

In the above equation, $\hat{b}$ is the estimated value of vector $b$. Now, the system input is considered as

$$u = \hat{u}^{fuz}(s,\hat{b}) + u^r(s) \quad (36)$$

where controller $u^r$ compensates the difference between the ideal and fuzzy controllers, and it is computed from the following equation:

$$u^r = \hat{\psi}sgn(s)sgn(G) \quad (37)$$

It should be mentioned that $\hat{\psi}$ is the estimated limit of the fuzzy approximation error. To overcome adverse effect of chattering phenomena, $sat(s)$ is used instead of $sgn(s)$. Now, by substituting (36) into (19), the following relation is obtained.

$$\dot{\lambda}_x = F(\lambda_x,t) + G(\hat{u}^{fuz}(s,\hat{b}) + u^r(s)) \quad (38)$$

Thus, by adding the above equation with the product of (27) and $G$ (with regards to (21) and (22)), the dynamic equation of the tracking error is obtained as follows:

$$\dot{\lambda}_x(t) + \frac{K_I}{K_p} \lambda_x (t) = G(u^* - \hat{u}^{fuz}(s,\hat{b}) - u^r(s)) = \frac{\dot{s}}{K_p} \quad (39)$$

Now, by defining the approximation errors as

$$\hat{b} = b - \hat{b} \quad \hat{\psi}(t) = \psi - \hat{\psi}(t)$$

$$\hat{u}^{fuz} = u^* - \hat{u}^{fuz} = \hat{b}^T w + \xi \quad (40)$$
the adaptation algorithms are expressed as (41) and (42).

\[
\dot{\hat{b}} = -\ddot{b} = \alpha_1 sw \\
\dot{\hat{\psi}} = -\ddot{\psi} = \alpha_2 s |s| \text{sgn}(G)
\]  

(41)  
(42)

In the adaptation algorithms, \(\alpha_1\) and \(\alpha_2\) are the adaptation rates and they are selected as positive constant numbers. The structure of the adaptive fuzzy sliding-mode controller is shown in Figure 7. Now, to evaluate the stability of the system in the presence of the designed controller, the following positive definite function is considered as the Lyapunov function:

\[
V_2(s, \hat{b}, \hat{\psi}) = \frac{1}{2K_p} s^2 + \frac{G}{2\alpha_1} \hat{b}^T \hat{b} + \frac{G}{2\alpha_2} \hat{\psi}^2
\]  

(43)

By taking the derivative of \(V_2(s, \hat{b}, \hat{\psi})\) with respect to time and considering (37) through (42),

\[
\dot{V}_2(s, \hat{b}, \hat{\psi}) = \frac{s}{K_p} \ddot{s} + \frac{G}{\alpha_1} \hat{b}^T \hat{b} + \frac{G}{\alpha_2} \hat{\psi} \hat{\psi} = sG(b^T w + \xi - u^r) + \frac{G}{\alpha_1} \hat{b}^T \hat{b} + \frac{G}{\alpha_2} \hat{\psi} \hat{\psi}
\]

\[
= Gb^T \left( sw + \frac{\hat{b}}{\alpha_1} \right) + sG(\xi - u^r) + \frac{G}{\alpha_2} \hat{\psi} \hat{\psi} = sG\xi - |s||G||\xi| - |s||G||\psi|
\]

\[
= -|s||G|(\psi - |\xi|) \leq 0
\]  

(44)

It is concluded that \(\dot{V}_2(s, \hat{b}, \hat{\psi})\) is always negative semi-definite; indicating the stability of the system according to the Lyapunov’s concept. Thus, all the parameters of \(\hat{\psi}, \hat{b}\) and \(s\) are bounded. Barbalat’s Lemma is used to verify the convergence of the tracking error to zero (Poursamad and Markazi, 2009a). So by considering the following equation

\[
\Gamma(t) \equiv |s||G|(\psi - |\xi|) \leq -\dot{V}_2
\]  

(45)
and integrating $\Gamma(t)$ with respect to time, the following equation is obtained:

$$\int_{0}^{t} \Gamma(\tau)d\tau \leq V_{2}(s(0), \ddot{b}, \ddot{y}) - V_{2}(s(t), \ddot{b}, \ddot{y})$$

(46)

Since $V_{2}(s(0), \ddot{b}, \ddot{y})$ is bounded and $V_{2}(s(t), \ddot{b}, \ddot{y})$ is non-increasing and bounded, (47) is written as follows.

$$\lim_{t \to \infty} \int_{0}^{t} \Gamma(\tau)d\tau \leq \infty$$

(47)

So considering Barbalat’s Lemma, Equation (48) is obtained.

$$\lim_{t \to \infty} \Gamma(t) = \lim_{t \to \infty} s(t) = 0$$

(48)

Thus, the tracking error converges to zero, and the system becomes asymptotically stable.

7 SIMULATION RESULTS

To demonstrate the performance of the proposed control strategy, the adaptive fuzzy sliding-mode controller is applied to the wheel slide protection device for numerical simulations. In addition, for the purpose of comparison, Trenitalia, Knorr-Bremse, and Mitsubishi control techniques are implemented. To consider the effects of unmodeled movements during the controller design, the multi-body dynamics method is used for simulating the longitudinal dynamics of ER24PC locomotive (Figure 8). In the simulations, the weight shifting is considered during braking. It should be mentioned that the modeled locomotive with 82 degrees of freedom, has been validated using the test data provided by Mapna Locomotive and Siemens Companies. The values of parameters, degrees of freedom, and masses and inertia properties of the components of the locomotive are presented in Tables 6, 7 and 8, respectively. Also, the constant values of $a$ and $b$ are considered based on Polach (1999). The initial velocity of the locomotive is assumed to be 120 km/h.

To compare the performance of the controllers in the presence of uncertainties, random track irregularities are considered. To generate the irregularities, Power Spectral Densities (PSDs) obtained from measurement data are used. The PSDs for horizontal, vertical and lateral track irregularities are defined in ERRI B176 (SIMPACK AG, 2016). With the wavenumber $\Omega$ and the wavelength $L$, the analytical representation of the PSDs $S_{\text{track}}$ is defined as Equation (49).

$$S_{\text{track}}(\Omega) = \frac{\beta_{0} + \beta_{2}\Omega^{2}}{\gamma_{0} + \gamma_{2}\Omega^{2} + \gamma_{4}\Omega^{4} + \gamma_{6}\Omega^{6}} , \quad \Omega = \frac{2\pi}{L}$$

(49)
**Figure 8**: Multi-body dynamics modelling of ER24PC locomotive during braking.

<table>
<thead>
<tr>
<th>parameter</th>
<th>value</th>
<th>unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>mass of locomotive</td>
<td>76841</td>
<td>kg</td>
</tr>
<tr>
<td>wheelbase</td>
<td>2700</td>
<td>mm</td>
</tr>
<tr>
<td>track gauge</td>
<td>1435</td>
<td>mm</td>
</tr>
<tr>
<td>wheel diameter</td>
<td>1100</td>
<td>mm</td>
</tr>
<tr>
<td>track cant</td>
<td>1:40</td>
<td>-</td>
</tr>
<tr>
<td>Young’s modulus</td>
<td>210</td>
<td>GPa</td>
</tr>
<tr>
<td>Poisson’s ratio</td>
<td>0.25</td>
<td>-</td>
</tr>
<tr>
<td>$P_{max}$</td>
<td>6</td>
<td>bar</td>
</tr>
<tr>
<td>$T_F$</td>
<td>0.6</td>
<td>s</td>
</tr>
<tr>
<td>$T_Y$</td>
<td>0.6</td>
<td>s</td>
</tr>
<tr>
<td>$T_{brake, max}$</td>
<td>60</td>
<td>kNm</td>
</tr>
</tbody>
</table>

**Table 6**: Values of parameters in modelling of ER24PC locomotive.

<table>
<thead>
<tr>
<th>component</th>
<th>number of component</th>
<th>total degrees of freedom</th>
</tr>
</thead>
<tbody>
<tr>
<td>Locomotive body</td>
<td>1</td>
<td>6</td>
</tr>
<tr>
<td>bogie frame</td>
<td>2</td>
<td>12</td>
</tr>
<tr>
<td>wheelset</td>
<td>4</td>
<td>24</td>
</tr>
<tr>
<td>axle box</td>
<td>8</td>
<td>8</td>
</tr>
<tr>
<td>traction rod</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>gearbox</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>steering rod</td>
<td>8</td>
<td>24</td>
</tr>
</tbody>
</table>

**Table 7**: Total degrees of freedom of ER24PC locomotive components.

<table>
<thead>
<tr>
<th>component</th>
<th>$m$ (kg)</th>
<th>$I_{xx}$ (kg.m^2)</th>
<th>$I_{yy}$ (kg.m^2)</th>
<th>$I_{zz}$ (kg.m^2)</th>
<th>$I_{xy}$ (kg.m^2)</th>
<th>$I_{xz}$ (kg.m^2)</th>
<th>$I_{yz}$ (kg.m^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>cabin</td>
<td>57652</td>
<td>1164578</td>
<td>44086.36</td>
<td>1153040</td>
<td>-4682.9</td>
<td>1132.78</td>
<td>11547.58</td>
</tr>
<tr>
<td>bogie</td>
<td>2550</td>
<td>1722</td>
<td>1476</td>
<td>3067</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>wheelset</td>
<td>1931</td>
<td>1094.4</td>
<td>161.257</td>
<td>1094.4</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>gear box</td>
<td>676</td>
<td>38.783</td>
<td>102.075</td>
<td>79.827</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>traction motor</td>
<td>1595</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>axle box</td>
<td>215</td>
<td>2.6</td>
<td>6.2</td>
<td>6.2</td>
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<td>0</td>
<td>0</td>
</tr>
<tr>
<td>guiding rod</td>
<td>30</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>reaction rod</td>
<td>26.5</td>
<td>0.21</td>
<td>0.412</td>
<td>0.6</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

**Table 8**: Masses and inertia properties of the ER24PC locomotive.
According to EN 13848-1:2003+A1:2008 (2009), for typical track irregularities in the public transportation, the wavelength is chosen in the range of $3m \leq L \leq 25m$. Also, the PSD coefficients ($\beta_0$ to $\beta_2$ and $\gamma_0$ to $\gamma_6$) are chosen based on Table 9.

Due to the vibration of the brake pads at the onset of braking, the disturbing torque $T_d = 0.05T_{\text{brake}}\exp(-4t)\sin(10\pi t)$ is added to the braking torque. The initial output values of the membership functions, and the uncertainty limit are chosen as $\hat{b} = [-1, -0.5, 0, 0.5, 1]^T$ and $\psi = 1$, respectively. Also, the controller parameters are specified as $\alpha_1 = 10$, $\alpha_2 = 0.85$, $K_I = 550$ and $K_P = 1800$.

<table>
<thead>
<tr>
<th></th>
<th>$\beta_0$ ($10^7$)</th>
<th>$\beta_2$ ($10^6$)</th>
<th>$\gamma_0$ ($10^4$)</th>
<th>$\gamma_2$</th>
<th>$\gamma_4$</th>
<th>$\gamma_6$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Horizontal excitation</td>
<td>4.164787</td>
<td>0</td>
<td>2.8855</td>
<td>0.68038</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>Vertical excitation</td>
<td>7.343623</td>
<td>0</td>
<td>2.8855</td>
<td>0.68038</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>Lateral excitation</td>
<td>0</td>
<td>0.305533</td>
<td>0.55356</td>
<td>0.13081</td>
<td>0.8722335</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 9: PSD coefficients for the track-irregularities.

By applying Trenitalia, Knorr-Bremse and Mitsubishi methods for different frictional conditions, the diagrams of wheel sets slip ratios and velocities are plotted. In view of Figures 9 and 10, when using Trenitalia method, it is seen that the slip ratios and velocities go beyond the specified range (according to (16)). Due to the decrease of the locomotive velocity, the wheel sets slip ratios diverge near the stopping time. It should be mentioned that severe fluctuations in the wheel sets velocities will reduce the service life of the frictional parts involved (Barna, 2012). As shown in Figures 11 and 12, in comparison with Figures 9 and 10, the fluctuations of the slip ratios and velocities have been decreased by using Knorr-Bremse technique. The diagrams of the wheel sets slip ratios and velocities resulted from using Mitsubishi controller are presented in Figures 13 and 14, respectively. As shown in Figure 13, when applying Mitsubishi controller with braking on dry rails, the wheel sets slip ratios don’t exceed 0.3; while in the case of braking on wet rails, the slip ratios of the wheel sets fluctuate and eventually diverge. It is concluded that the performance of Mitsubishi method is affected in different frictional conditions.

![Figure 9](image_url)  
Figure 9: Slip ratio of wheel sets in the case of braking on (a) dry rails, and (b) wet rails, and by using the controller devised by Trenitalia.
Figure 10: Velocity of wheel sets and locomotive in the case of braking on (a) dry rails, and (b) wet rails, and by using the controller devised by Trenitalia.

Figure 11: Slip ratio of wheel sets in the case of braking on (a) dry rails, and (b) wet rails, and by using the controller presented by Knorr-Bremse.

Figure 12: Velocity of wheel sets and locomotive in the case of braking on (a) dry rails, and (b) wet rails, and by using the controller presented by Knorr-Bremse.
After applying the AFSM controller in different frictional conditions, the diagrams of the wheel sets slip ratios and velocities are presented in Figures 15 and 16, respectively. As is shown in Figure 15, in both frictional conditions, the wheel sets slip ratios fluctuates about the desired value of 0.14. Of course, at the end of braking, due to the reduction of the locomotive velocity, the amplitude of the slip ratios oscillations increases. It should be noted that in the case of braking on wet rails, the settling time of the slip ratios reduces. Also, as observed in Figure 16, by using the AFSM controller, the amplitude of the velocities fluctuations is low in comparison with the other approaches. So, the simulation results show that in comparison with Trenitalia and Knorr-Bremse techniques, AFSMC method can overcome the divergence of wheel sets slip ratios near the stopping time. Also, in comparison with Mitsubishi controller, AFSM controller can improve the robustness of the WSPD regarding various rail conditions.

Wheel set1 braking torque with braking on dry and wet rails and using Trenitalia, Knorr-Bremse, and Mitsubishi controllers are presented in Figures 17 and 18, respectively. Also, using the AFSM controller, wheel set1 input and braking torque in the case of braking on dry and wet rails are shown in Figures 19 and 20, respectively. As seen in Figures 17-20, in the case of braking on wet rails, the frequency of input (braking torque) fluctuations increases. Also, the lowest and the highest switching frequency of the braking torque are related to Trenitalia and Mitsubishi methods. It should be mentioned that using AFSM controller, the switching frequency of the actuator input is in the allowed range regarding the common sampling time interval (=100 ms).

Figure 13: Slip ratio of wheel sets in the case of braking on (a) dry rails, and (b) wet rails, and by using the controller presented by Mitsubishi.

Figure 14: Velocity of wheel sets and locomotive in the case of braking on (a) dry rails, and (b) wet rails, and by using the controller presented by Mitsubishi.
Figure 15: Slip ratio of wheel sets in the case of braking on (a) dry rails, and (b) wet rails, and by employing the adaptive fuzzy sliding-mode controller.

Figure 16: Velocity of wheel sets and locomotive in the case of braking on (a) dry rails, and (b) wet rails, and by employing the adaptive fuzzy sliding-mode controller.

At the end, the integral of wheel sets braking torque, the distance and time taken to stop the locomotive in each of the conditions are presented in Table 10. As shown in Table 10, by applying the AFSMC method, the stopping time and the braking distance of the locomotive have been decreased regarding various rail conditions. According to Equation (12), the amount of a wheel set braking torque is proportional to the pressure of the corresponding cylinder. Thus, as stated in Petrenko (2017) and EN 15595 (2011), the air consumption of the braking system can be evaluated.

using the value of $\sum_{i=1}^{4} \int_{0}^{t_{stop}} T_{brake_i} dt$. In the case of braking on dry rails and employing AFSM controller, the integral of wheel sets braking torque increases in comparison with the other control techniques.

\begin{align*}
\text{braking distance (m)} & \quad \text{stopping time (s)} & \quad \sum_{i=1}^{4} \int_{0}^{t_{stop}} T_{brake_i} dt \quad (\text{kNm.s}) \\
\text{control method} & \quad \text{dry rail} & \quad \text{wet rail} & \quad \text{dry rail} & \quad \text{wet rail} & \quad \text{dry rail} & \quad \text{wet rail} \\
\text{Trenitalia} & \quad 184.63 & \quad 221.15 & \quad 9.9 & \quad 12.3 & \quad 1572.48 & \quad 1564.66 \\
\text{Knorr-Bremse} & \quad 207.37 & \quad 246.68 & \quad 10.5 & \quad 13.1 & \quad 1570.26 & \quad 1576.44 \\
\text{Mitsubishi} & \quad 201.40 & \quad 235.33 & \quad 10.5 & \quad 12.8 & \quad 1556.8 & \quad 1570.31 \\
\text{AFSMC} & \quad 184.03 & \quad 220.60 & \quad 9.8 & \quad 12.2 & \quad 1578.03 & \quad 1565.84 \\
\end{align*}

\textbf{Table 10:} Comparing simulation results obtained by assuming an initial locomotive speed of 120 km/h.

While the value of $\sum_{i=1}^{4} \int_{0}^{t_{stop}} T_{brake_i} dt$ decreases in the case of braking on wet rails.

In Figure 21, the comparison of vertical forces exerted on two different wheel sets in the case of braking on wet rails (and using the AFSMC method) is shown. It can be realized that due to considering the 3D body dynamics in the co-simulation method, vertical forces exerted on different wheel sets are not equal. So, in the simulations, the weight shifting will happen during braking. As shown in Figures 15 and 16, this phenomenon causes differences between the slip ratios and veloc-
ties of front wheel sets (wheel sets 3 and 4) and rear wheel sets (wheel sets 1 and 2). It should be noted that, despite the different values of the normal forces, the slip ratios of the front and rear wheel sets converge towards the desired value.

![Figure 18: Wheel set1 braking torque in the case of braking on wet rails and using (a) Trenitalia, (b) Knorr-Bremse, and (c) Mitsubishi controllers.](image1)

![Figure 19: Wheel set1 (a) WSPD input and (b) braking torque in the case of braking on dry rails and by employing the adaptive fuzzy sliding-mode controller.](image2)

If large creepages between wheels and rails have a high endurance, the dissipation of energy at the rolling surfaces increases considerably. This phenomenon can lead to wheel/rail wear. In this work, the performed simulations and the obtained results are in accordance with the guidelines of EN 15595 (2011). In the guidelines of EN 15595 (2011), limits are set regarding the locking and the maximum absolute slide of the wheel sets. This standard covers the system acceptance requirements as well as the application specific requirements for wheel slide protection systems.
8 CONCLUSIONS

In this study, an adaptive fuzzy sliding-mode PWM controller is designed for the WSPD of ER24PC locomotive to regulate the wheel sets slip ratios in the presence of uncertainties with unknown bounds. On the contrary to the heuristic and knowledge-based techniques, no reference measured data and the experimental knowledge of relevant experts is needed for designing AFSM controller. The second Lyapunov theorem, guarantees the convergence of the slip ratio to the desired values. Unlike the SMC method which needs a relatively accurate model of the plant to guarantee the stability, the AFSMC method needs minimal information from the model of the plant. The reason is that the upper bound of the plant uncertainty is estimated online by the proposed method. This feature, furthermore, prevents excessive switching of the control input which is a common phenomenon in the conventional SMC methods.

**Figure 20**: Wheel set1 (a) WSPD input and (b) braking torque in the case of braking on wet rails and by employing the adaptive fuzzy sliding-mode controller.

**Figure 21**: Comparison of vertical forces exerted on different wheel sets in the case of braking on wet rails and by employing the adaptive fuzzy sliding-mode controller.

Multi-body dynamics model for simulation of the longitudinal dynamics of the ER24PC locomotive is employed. The model is consisting 82 degrees of freedom. The model has been validated using the test data provided by Mapna Locomotive and Siemens Companies. The simulation results depict that, in comparison with Trenitalia, Knorr-Bremse and Mitsubushi techniques, AFSMC method can improve the robustness of the WSPD regarding various rail conditions. It should be
mentioned that by applying the AFSMC method, the stopping time and the braking distance of the locomotive have been decreased, while only a minimum amount of information of the plant is employed in the control design process.

Acknowledgment

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References


