Hot Tensile and Creep Rupture Data Extrapolation on 2.25Cr-1Mo Steel Using the CDM Penny-kachanov Methodology

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Hot tensile and creep data were obtained for 2.25Cr-1Mo steel, ASTM A387 Gr.22CL2, at the temperatures of 500-550-600-650-700 °C. Using the concept of equivalence between hot tensile data and creep data, the results were analyzed according to the methodology based on Kachanov Continuum Damage Mechanics proposed by Penny, which suggests the possibility of using short time creep data obtained in laboratory for extrapolation to long operating times corresponding to tens of thousands hours. The hot tensile data (converted to creep) define in a better way the region where β =0 and the creep data define the region where β =1, according to the methodology. Extrapolation to 10,000 h and 100,000 h is performed and the results compared with results obtained by other extrapolation procedures such as the Larson-Miller and Manson-Haferd methodologies. Extrapolation from ASTM and NIMS Datasheets for 10,000 h and 100,000 h as well as data from other authors on 2.25Cr-1Mo steel are used for assessing the reliability of the results.

Keywords: 2.25Cr-1Mo steel, hot tensile data, creep data, CDM Penny methodology, data extrapolation

1. Introduction

A simplified extrapolation procedure from shorter creep rupture data to longer times was proposed by Penny¹ based on Continuum Damage Mechanics (CDM) concepts originally developed by Kachanov². According to this method, the time to failure, t_{ρ} is given by:

$$t_f = t_r - \overline{t} \tag{1}$$

where

$$t_r = \frac{1}{Bk \, \sigma^k} \tag{2a}$$

and

$$\overline{t} = \frac{1}{Bk\overline{\sigma}^k}$$
(2b)

B and *k* are material constants obtained from curve fitting, σ is the applied creep stress (in fact $\sigma = \sigma_0$, the initial stress in a constant load creep test) and $\overline{\sigma}$ is the flow stress. The value of $\overline{\sigma}$ has a lower limit equal to the Yield Strength and an upper limit equal do the Ultimate Tensile Strength, and can be set equal to the stress level of a short-time creep rupture test for calculation and graphing purposes, as recommended by Penny^{1,3}.

Figure 1 illustrates the stress-strain-time relationships for tensile deformation in general, involving tensile testing, creep testing and stress relaxation testing³.

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Figure 2 shows schematically how the parameters t_{r} , β and k are defined on the modified Kachanov brittle rupture curve³.

It is interesting to notice that Equation 2b produces the following relation between $\overline{\sigma}$ and \overline{t} :

$$Log(\overline{\sigma}) = (1/k) Log(1/Bk) - (1/k) (Log(\overline{t}))$$
(3)

Therefore, the value A = -Log(BK)/k corresponds to the intercept of the brittleness line $\beta = 1$ with the Log(σ) axis, and (-1/k) corresponds to its slope.

The time to creep failure is given by: $t_f = \beta t_r$, so that $Log t_f = Log\beta + Log t_r$, and the characterization of the β factor is of also of great importance.

The values of $\overline{\sigma}$, *k*, *B* and \overline{t} can be determined by curve fitting using the experimental data of $Log\sigma$ versus $Log t_{f}$ i.e. using the relation:

$$Log(t_f) = Log\left(\frac{1}{Bk \sigma^k} - \overline{t}\right)$$
(4)

The sensitivity of the method to the procedure of curve fitting, which includes a manually chosen value of k, has been discussed by Penny¹. The performance of the method using curve fitting procedure has also been discussed and several examples of extrapolation presented in literature^{1,4,5}. Le May⁶ has recently reviewed the principles of this methodology from the standpoint of remaining life prediction.



Figure 1. Schematic stress-strain-time relationships in tension³.



Figure 2. The modified Kachanov brittle rupture curve³.

In the present work, the characterization of the σ parameter was performed with better accuracy, since, instead of using "short time creep tests", a set of hot tensile tests were carried out at different temperatures and crosshead speeds, with their results combined with the creep results in the analysis, as will be described in the next session.

2. Material and Methods

The steel was supplied in plate form with 25.4 mm thickness, according to ASTM A 387, grade 22 class 2, in the normalized and tempered condition, with the following chemical composition: Fe - 2.09Cr - 1.08Mo - 0.097C - 0.32Si - 0.50Mn - 0.007P - 0.002S - 0.03Ni - 0.01Cu - 0.05Al. Metallographic analysis indicated the presence of about 30% bainite and 70% ferrite, as shown in Figures 3a and 3b.

The specimens for the hot tensile tests and creep tests were extracted from the rolling direction. A gauge length Lo = 25 mm and an initial diameter do = 6.25mm were used for all specimens.

The hot tensile tests were carried out in a servo-hydraulic 8802 model INSTRON machine, at 500 °C, 550 °C, 600 °C, 650 °C and 700 °C, using the following constant crosshead speeds: 0,01 - 0,25 - 1,0 - 5,0 and 20 mm/min. In this way, 25 hot tensile tests were performed with a total variation of 3 orders of magnitude in strain rate, i.e. in the range from 6.7×10^{-6} to 1.3×10^{-2} s⁻¹. The hot tensile tests were carried out according to ASTM E21⁷, however, employing different values of crosshead speeds and not a single value (equivalent to a fixed strain rate), as recommended by the standard.

The creep tests were carried out at constant load, according to ASTM E139⁸, using a set of 10 creep machines model STM-MF 1000. Information about this equipment and testing techniques appeared in a previous publication^{9,10}. The elongation of the specimens was followed with creep extensometers having LVDT transducers. The readings from the transducers were collected by a Data Logger, using a scan rate of 6 readings/h. The creep tests were carried out



Figure 3. Microstructure of 2.25Cr1Mo steel in the as received condition: a) Optical micrograph (500 x, with Nital 2%); b) SEM micrograph (2000 x).

in 9 temperatures levels, namely: $500 \,^{\circ}$ C, $525 \,^{\circ}$ C, $550 \,^{\circ}$ C, $575 \,^{\circ}$ C, $600 \,^{\circ}$ C, $625 \,^{\circ}$ C, $650 \,^{\circ}$ C, $675 \,^{\circ}$ C and $700 \,^{\circ}$ C, with 17 levels of applied stress, varying from 34.5 MPa to 414 MPa, so that 51 creep tests were produced with rupture times varying from 2 to about 1300 hours.

3. Results and Discussion

Figure 4 shows the hot tensile data plotted together with the creep rupture data, using a criterion of equivalence proposed to correlate results from both kind of tests^{11,12}. According to this criterion: the UTS, the nominal strain rate and the time to reach UTS in a hot tensile test corresponds respectively to the applied stress, the minimum creep rate and the rupture time in a creep test.

The verification of validity of this methodology for various materials has been demonstrated in various publication¹³⁻¹⁷.

Figure 5a and 5b show the data presented in Figure 4 subjected to parameterization analysis, according to two different procedures: the Larson-Miller and the Manson-Haferd methodologies, respectively¹⁶. Although the Larson-Miller analysis is more popular and widely applied for extrapolation in several situations, with the present data the best results were obtained with the analysis of Manson-Haferd, as evident from comparison between Figures 5a and 5b¹⁷.

Figure 6a shows the hot tensile plotted together with creep data at 500 °C on the diagram $Log(\sigma) \times Log(\mathbf{t}_{runt})$, with



Figure 4. Hot tensile data plotted with creep data, according to the equivalence criterion proposed for analysing both kind of results together. Loss of creep strength with the rupture time.



Figure 5. Hot tensile data plotted with creep data, according to the equivalence criterion proposed for analysing both kind of results together: a) result by the Larson-Miller analysis; b) result by the Manson-Haferd method.



Figure 6. Hot tensile and creep data on 2.25Cr-1Mo steel analysed by the Penny procedure¹, at temperatures of : a) 500 °C; b) 550 °C; c) 600 °C; d) 650 °C; e) 700 °C.

the curve \mathbf{t}_f (in blue), determined by the Penny-Kachanov^{1,2} fitting, and the straight line corresponding to \mathbf{t}_f Kachanovbrittleness obtained by extrapolation (in red). The horizontal line (in green) represents the condition where $\beta = 0$. The rupture strengths predicted for 10,000 and 100,000 h are also indicated. The parameter \mathbf{t}_{rupt} used to plot the experimental data corresponds here to the parameter \mathbf{t}_f adopted by Penny¹ in his methodology.

Using a standard procedure of curve fitting, considering Equation 4, the following constants were determined: k = 8, $\overline{\sigma} = 486.41$ MPa, $\overline{t} = 15.000$ h, Bk = 2.128×10^{-23} and A = 2.834 (the intercept of the brittleness line ($\beta = 1$) with the Y-axis, for Log(\mathbf{t}_{rupt}) = 0). The stress levels for attaining 10,000h and 100,000h are, respectively, 215.7 MPa and 161.8 MPa, which are shown by the triangles (in light blue e dark blue, respectively) in Figure 5a. Several values of k were tried in the analysis, but finally it was chosen the value of k = 8, which was verified to minimize the sum of the squared error between the predicted and the observed ruptures times.

Figure 6b refers to the data obtained at 550 °C. In this case, the same procedure of analysis was applied, i.e. the value of k was best taken as k = 8, and the following parameters determined: $\overline{\sigma} = 449.50$ MPa, $\overline{t} = 0.600$ h, Bk = 1.00×10^{-21} and A = 2.625. The stress levels for attaining 10,000h and 100,000h are, respectively, 133.4 MPa and 100.0 MPa at 550 °C.

Figure 6c refers to the data obtained at 600 °C. In this case, the value of k was best taken as k = 6.5 and the parameters were: $\overline{\sigma} = 401.05$ MPa, $\overline{t} = 0.180$ h e Bk = 6.667×10^{-17} and A = 2.489. The stress levels for attaining 10,000h and 100,000 h are, respectively, 74.7 MPa and 52.4 MPa at 600 °C.

In the analysis of the data at 650 °C (Figure 6d) and 700 °C (Figure 6e) the value of *k* was best taken as k = 5.5and k = 5.0, respectively, with the following set of parameters determined: $\overline{\sigma} = 375.26$ MPa, $\overline{t} = 0.05$ h, Bk = 1.818×10^{-13} and A = 2.316 for 650 °C and $\overline{\sigma} = 282.52$ MPa, $\overline{t} = 0.01$ h, Bk = 5.556×10^{-11} and A = 2.051 for 700 °C. The stress levels for 10,000 and 100,000 h are respectively: 38.8 MPa and 25.6 MPa at 650 °C, and 17.8 MPa and 11.2 MPa at 700 °C.

Table 1 gives the complete set of values for the parameters k, **B**, $\overline{\sigma}$ and \overline{t} and Figures 7a, 7b, 7c and 7d show, respectively, their variation with temperature.

Figure 7a and 7b indicate that the values of *k* and **B** decrease and increase linearly, respectively, with the increase in temperature and the legends in the figures present the regression coefficients determined for the data. According to Equation 2a and Figure 2, the value -1/k correspond to the slope of the Kachanov² brittleness line, and it is easy

to verify that the slopes of the curves in Figures 6a to 6e decrease as temperature increases, and therefore k decreases.

Figure 7c and 7d indicate that the parameters $\overline{\sigma}$ and \overline{t} also decrease linearly with temperature. The values of $\overline{\sigma}$ are connected to the ultimate tensile stress of the material, and their reduction with temperature is a predictable behavior. The value of \overline{t} corresponds to the intersection of the line t_r with the line of ultimate tensile stress $\overline{\sigma}$. The decrease of \overline{t} with temperature is also a predictable behavior, since rupture times always decrease with increase in temperature at certain level of stress. The decrease of \overline{t} with temperature is easily verified in Figures 6a to 6e.

It is important to emphazise the inclusion of the hot tensile data in the present analysis. These kind of data, expressed as creep data (using the criterion of equivalence mentioned previously¹¹), proves to be very useful for defining the left side of the curve $\text{Log}(\sigma)$ vs. (Log \mathbf{t}_{f}), in Figure 2, or of the curves $\text{Log}(\sigma)$ vs. (Log \mathbf{t}_{rupl}) in Figures 6a to 6e. Thereby, the value of $\overline{\sigma}$ is better identified in the analysis. The values of \overline{t} are also better characterized. A careful observation of Figures 6a to 6e, shows the evident decrease of $\overline{\sigma}$ nd \overline{t} , as test temperature increases.

Figure 8a shows the variation of Creep Rupture Strength for 10,000h and for 100,000h for the 2.25Cr-1Mo steel under investigation, according to the analysis by the method of Penny-Kachanov^{1,2}. The present set of data (with 25 hot tensile results + 51 creep test results) were also analyzed by various traditional parameterization methodologies¹⁷, like: Larson-Miller, Orr-Sherby-Dorn, Goldhoff-Sherby, Manson-Haferd and Manson-Succop. The results according to the methods of Larson-Miller and Manson-Haferd were presented in Figures 5a and 5b. With these two reference curves it was also possible to obtain data of $\sigma_{_{10,000h}}$ and σ 100,000h. Data of these allowable stresses could also be obtained for 2.25Cr-1Mo steel in the normalized and tempered condition from the work of Viswanathan¹⁸ and from the ASTM Special Report DS 6S1¹⁹, that employed in both cases the Larson-Miller method in their analysis. It was also considered information of the NIMS Datasheets for a similar version of 2.25Cr-1Mo steel for comparison^{20,21}. In this case, according to their publication^{20,21}, the data were rationalized by the Manson-Haferd method.

Figure 8b presents a comparison of the Creep Rupture Strength for 10,000h of the steel according to the Penny-Kachanov¹ analysis with results of the same kind reported by the authors mentioned above. It can be observed that the Penny-Kachanov^{1,2} curve is situated in between the Viswanathan's curve¹⁸, indicating higher creep rupture strength, and the ASTM curve¹⁹, with lower creep rupture strength.

Table 1.	Variation of the	parameters k, B,	σ, i	<i>t</i> , σ	$10,000$ and σ	on ooob with	temperature,	according to	o the Penny-	-Kachanov ^{1,2} a	analysis.
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T(°C)	k	В	$\bar{\sigma}$ (MPa)	\overline{t} (h)	$\sigma_{10,000h}$	$\sigma_{100,000h}$
500	8.0	2.660E-24	486.41	15.000	215.7	161.8
550	8.0	1.250E-22	449.50	0.600	133.4	100.0
600	6.5	1.026E-17	401.05	0.180	74.7	52.4
650	5.5	3.306E-14	357.26	0.050	38.8	25.6
700	5.0	1.111E-11	282.52	0.010	17.8	11.2



Figure 7. Variation with temperature of the parameters: a) *k*; b) **B**; c) $\overline{\sigma}$; d) \overline{t} .

The predictions made according to the Larson-Miller and Manson-Haferd methods are situated a little bellow the Penny-Kachanov^{1,2} curve.

In Figure 8c, the comparison refers to the Creep Rupture Strength for 100,000 h and approximately the same situation is verified: the Penny-Kachanov^{1,2} prediction is located again in between the four other curves.

Figures 8d and 8e indicate that the NIMS data show reasonable agreement with the ASTM data, for 10,000h and 100,000h respectively. In both situations, the Penny-Kachanov^{1,2} results are above these predictions.

It is important to point out that the creep rupture strength of the 2.25Cr-1Mo steel is highly dependent on the heattreatment conditions employed in the manufacturing of the material. Figure 9 shows data reported by Viswanathan¹⁸ presenting Larson-Miller reference curves for this steel under four different heat-treatment states, with remarkable difference between them. Therefore, in the comparison illustrated in Figures 8b and 8c, involving the normalized and tempered version of the steel from various sources, and subjected to different procedures of analysis, it seems acceptable that the five curves present the observed differences between each other.





(b)



Creep Rupture Strength for 100.000h for



(c)



STRESS (MPa

Figure 8. a) Creep rupture strength for 10,000 h and 100,000 h estimated by the Penny-Kachanov method^{1,2}; b) Creep rupture strength for 10,000 h, compared with data from: Viswanathan¹⁸, ASTM D61¹⁹, Larson-Miller and Manson-Haferd extrapolations¹⁷; d) Creep rupture strength for 10,000 h and e) Creep rupture strength for 100,000 h, compared with data from: ASTM D61¹⁹ and NIMS^{20,21} Datasheets.



Figure 9. Variation in Creep Rupture Strength of 2.25Cr-1Mo steel under different heat-treatment conditions, plotted using the Larson-Miller parameter. Q = quenched and tempered; NT = normalized and tempered; A = annealed; UTS = ultimate tensile stress. Obsv. Adapted from R.Viswanatan¹⁷.

4. Conclusions

- The methodology proposed by Penny¹, based on Kachanov work² was used to analyze a set of high temperature data from hot tensile and short duration creep tests, and it has been observed that the hot tensile data presents the great advantage or revealing better the region where β =0, and the creep data the region where β =1, according to the model;
- In the temperature range investigated, i.e. from 500 °C to 700 °C, the parameters k, $\overline{\sigma}$ and $\text{LOG}(\overline{t})$ where observed to decrease linearly with increase in temperature. On the other hand the parameter LOG(B) was observed to decrease linearly with increase in temperature;
- The Creep Rupture Strength of 10,000h and 100,000h were obtained by extrapolation from the Penny-Kachanov^{1,2} methodology and the results are satisfactorily compatible with similar data from other sources in literature;

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- The results obtained with Penny-Kachanov^{1,2} methodology in this work are satisfactorily consistent and the methodology seems viable to be employed with great advantage to generate data for long term operating times, from extrapolation of results of short duration produced in laboratory;
- Validation of the methodology should be tested extensively with data as done in this work (i.e. considering hot tensile and creep testing results) from different metals and alloys.

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