A mass-spring model of the auditory system in otosclerosis

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Abstract Introduction: This paper aims to describe a model to simulate otosclerosis using a mass-spring model and to correlate the results with the clinical and audiological data on the disease. Methods: A mass-spring model was used to represent the behavior of the auditory system simulating otosclerosis. The model consisted of six masses (air volume in the external auditory canal; tympanic membrane; malleus; incus; stapes, and cochlear fluid), springs and dashpots simulating the supporting ligaments and muscles. The parameters to simulate the disease were obtained from the literature; stapedial annular ligament stiffness was increased by 10-fold and to 100-fold and stapes mass increased by 5-fold. Results: There was a decrease in stapes displacement in the lower frequencies when the stiffness of the stapedial annular ligament was increased. It was also found a reduction in stapes displacement in the higher frequencies with increased stapes mass. Conclusions: The increased stiffness of the stapedial annular ligament can be an indication of early stage disease, whereas increased bone growth suggests disease progression. The results of the simulation are in agreement with the clinical and audiological disease and support the need for further study of the stapedial annular ligament to find ways to evaluate its functioning and thus enable early detection of hearing losses caused by changes in that structure.

Keywords Biomechanics, Otosclerosis, Hearing.

Introduction

Biomechanical studies of human hearing have been widely reported in the literature (Dai et al., 2007; Feng and Gan, 2002, 2004; Gan et al., 2004, 2007, 2010; Garbe et al., 2010; Huber et al., 2003; Koike et al., 2002; Liu et al., 2009; Sun et al., 2002; Zhao et al., 2009). The main reason for this interest is that the ear is a key sensory organ in communication, which is a basic human need (Bertachini and Gonçalves, 2002).

Hearing loss can compromise language and cognitive development, the intelligibility of the spoken message, and have an impact on an individual’s social life. Therefore, early diagnosis of hearing impairment is of paramount importance (Roslyn-Jensen, 1996). In this context, the need to better understand hearing function, simulate the pathologies of the ear, anticipate the consequences of ear diseases, and conceive potential modalities of treatment has prompted biomechanical studies of this complex sensory system.

The function of the human auditory system is to transform the mechanical sound wave collected from the external environment into electrical impulses that are sent to the brain, where the auditory information is interpreted (Hungria, 1988; Zemlin, 2005). Hearing loss occurs when an alteration is present in any segment of the auditory system; one causative factor of such alterations is otosclerosis.

Otosclerosis is a hereditary, degenerative disease of the otic capsule and inner ear walls, with foci of new bone formation and increased local vascularization. The second most frequently involved site is the area of the oval window and the stapedial footplate (Beales, 1987). The characteristic changes of otosclerosis in the auditory system are increased stiffness of the stapedial annular ligament (Dai et al., 2009; Feng and Gan, 2004; Huber et al., 2003; Min et al., 2010) and abnormal bone growth (Brookler, 2008; Frost, 1962; Hungria, 1988; Miller and Schein, 2005; Min et al., 2010; Vicente et al., 2004).

Typically, the symptoms of otosclerosis are hearing loss, tinnitus, and vertigo, or a combination of these; symptoms may vary depending on the course of the disease (Hungria, 1988; Menger and Tange, 2003). From the audiometric point of view, the course of otosclerosis can be divided into four grades of severity: I, II, III, and IV. Grade I corresponds to the onset of the disease and is marked by an ascending audiometric curve with a more prominent loss for low-pitched sounds, which does not occur beyond 60 dB. In grade II, the audiometric curve is more horizontal, showing an initial decrease in the perception of high-pitched sounds. In grade III, audiometry shows a descending curve and hearing loss may reach up to 90 dB, predominantly for high-pitched sounds. In grade IV, a lack of response for high-pitched sounds is already observable (Hungria, 1988).

Biomechanical studies on normal hearing have been widely reported in the literature (Dai et al., 2007; Feng and Gan, 2002; Gan et al., 2004, 2007, 2010; Huber et al., 2003; Liu et al., 2009; Sun et al., 2002; Zhao et al., 2009). However, the same is not true for the simulation of the auditory system pathologies.
Regarding otosclerosis, there are few biomechanical studies of the ear simulating the disease. A one-dimensional physical model of the auditory system constituted by six masses suspended by springs and dashpots showed a reduction in stapes displacement and, consequently, in auditory response, after a 10-fold increase in the stiffness of the stapedial annular ligament—one of the features of otosclerosis (Feng and Gan, 2004). In another study using the finite element method, a three-dimensional (3-D) model of the ear was developed and two simulation groups were created: one with otosclerosis and the other with otosclerosis associated with fixation of the anterior malleolar ligament. The first group had increased stapedial annular ligament stiffness while the second also had anterior malleolar ligament stiffness. The results revealed a dramatic reduction in middle ear sound transfer gain, especially at low frequencies (Huber et al., 2003).

There are other studies, but these only mention the possibility of simulating otosclerosis and other pathological conditions using a biomechanical model of the ear (Costa, 2008; Garbe et al., 2010; Kelly et al., 2003).

The aim of the present study was to use a previously validated (Feng and Gan, 2004) one-dimensional mass-spring model to simulate otosclerosis, and compare the results with the audiological findings and different grades of the disease.

**Methods**

The discrete mass-spring model of the auditory system (Figure 1) is intended to simulate the behavior of normal hearing and when affected by otosclerosis.

In a damped mass-spring system, the equation of motion can be represented as

$$ m\ddot{x} + c\dot{x} + kx = f(t) $$

(1)

$$ x = Xe^{jwt} $$

(2)

$$ \dot{x} = jwXe^{jwt} $$

(3)

$$ \ddot{x} = -\omega^2 X e^{jwt} $$

(4)

where $m$ is the mass, $c$ is the damping parameter, $k$ is the stiffness, $x$ is the displacement, $\dot{x}$ is the velocity of the system matrices, and $f(t)$ denotes an externally applied force.

Therefore, a mass-spring system includes the basic components of an oscillating system: mass, spring (stiffness), and damping. When a force acts on the system, the resulting equations of motion are

$$ \omega = 2\pi f $$

(5)

$$ \omega = \sqrt{\frac{k}{m}} $$

(6)

$$ f = \frac{1}{2\pi} \sqrt{\frac{k}{m}} $$

(7)

where $\omega$ is the angular frequency of the system in radians per second and $f$ is the frequency in Hz.

In the present study, the mass-spring model of the auditory system was composed of six masses - M1, M2, M3, M4, M5, and M6 - representing, respectively, the masses of the external auditory canal, tympanic membrane, malleus, incus, stapes, and cochlear fluid. The mass of the external auditory canal corresponds to the volume of air that fills the canal. Masses M1, M2, M3, M4, M5, and M6 are suspended by massless springs and dashpots that simulate the ligaments, supporting muscles, and interfaces, and are represented in Figure 2, respectively, by K1, C1, K2, C2, K3, C3, K5, C5, K6, C6, K8, C8, C4, C7, C9, C10.

Element K8 represents the stapedial annular ligament, which will be used later to simulate otosclerosis. The mathematical model in this study was adapted from a model used by Feng and Gan, and the parameters of mass, stiffness, and damping used in the present discrete mass-spring model were obtained directly from anatomical data found in the literature (Feng and Gan, 2004), as shown in Tables 1 and 2.

According to Equation 1, the following matrices for a damped mass-spring system are obtained:
A force equivalent to 90dB(SPL) was applied to this system. To obtain the force in Newtons (N) from the intensity in decibels (dB), we used Equation 12 to convert the 90dB into sound pressure. Then, the sound pressure value was substituted in Equation 13 to yield the force in N.

\[ dB = 20 \log \left( \frac{P}{P_0} \right) \]  

\[ P = \frac{F}{A} \]  

Where \( P_0 = 2 \times 10^{-5} \text{N/m}^2 \)  

\( F = \) Force (N)  

\( A = \) Area (m²)  

\( P = \) Pressure (N/m²)

Equation 13 leads to the force in (N) based on the surface area of the tympanic membrane. In the literature, the total surface area of the tympanic membrane is considered to be 85mm². However, only approximately 56mm² of the total surface has motility (Costa, 2008). For that reason, surface area of 56mm² was considered.

The system of equations described earlier was plotted using MATLAB. The displacement of the stapes in normal conditions and with increased stapedial annular ligament stiffness and stapes mass was obtained.

To compare the results of the application of a 90dB(SPL) force (sound pressure level) with the audiometric test results, which employs dB(HL) (hearing level), a correction was made for each octave.

\[ \begin{bmatrix} m1 & 0 & 0 & 0 & 0 & 0 \\ 0 & m2 & 0 & 0 & 0 & 0 \\ 0 & 0 & m3 & 0 & 0 & 0 \\ 0 & 0 & 0 & m4 & 0 & 0 \\ 0 & 0 & 0 & 0 & m5 & 0 \\ 0 & 0 & 0 & 0 & 0 & m6 \end{bmatrix} \]  

\[ \begin{bmatrix} c2 & -c2 & 0 & 0 & 0 & 0 \\ -c2 & c1 + c2 + c3 & -c3 & 0 & 0 & 0 \\ 0 & -c3 & c3 + c4 + c5 & -c5 & 0 & 0 \\ 0 & 0 & -c5 & c5 + c6 + c7 & -c6 & 0 \\ 0 & 0 & 0 & -c6 & c6 + c8 + c9 & -c9 \\ 0 & 0 & 0 & 0 & -c9 & c9 + c10 \end{bmatrix} \]  

\[ \begin{bmatrix} k2 & -k2 & 0 & 0 & 0 & 0 \\ -k2 & k1 + k2 + k3 & -k3 & 0 & 0 & 0 \\ 0 & -k3 & k3 + k5 & -k5 & 0 & 0 \\ 0 & 0 & -k5 & k5 + k6 & -k6 & 0 \\ 0 & 0 & 0 & -k6 & k6 + k8 & 0 \\ 0 & 0 & 0 & 0 & 0 & k8 \end{bmatrix} \]
band. The filters dB(SPL) or dB (linear) correspond to the distribution of sound energy as a function of the frequency of the measured noise, while dB(HL) is intended to approximate the response of the auditory system to the measured noise (Bistafa, 2006).

Results

Using a discrete mass-spring model capable of representing the auditory system, the characteristic features of otosclerosis was considered, consistent with clinical and audiological findings. The former include progressive hearing loss, tinnitus, and vertigo, or a combination of these depending on the disease stage (Menger and Tange, 2003). The latter are marked by conductive hearing loss, initially for the low frequencies, that progresses to compromise the subsequent frequencies. As bone resorption and remodeling worsen, the disease eventually compromises also the high frequencies (Brookler, 2008; Hungria, 1988).

Initially, the applied force equivalent to 90dB(SPL) was converted for each octave band - which ranged between 250Hz and 8000Hz - into dB(HL). Except for the 250Hz octave band, it was found that the two spectra had similar values; therefore, the results of the study using a force in dB(SPL) could be compared with the audiometric test results, as illustrated in Figure 3.

In the present discrete mass-spring model of the auditory system, the normal displacement of the stapes was simulated, as well as displacements after 10-fold and 100-fold increases in stapedial annular ligament stiffness. Stapedial displacement after a 5-fold increase in the mass of the stapes was also simulated. Mass and stiffness changes are the clinical parameters that can be directly related to the presence of otosclerosis.

Figures 4, 5, and 6 represent displacements of the stapes with alterations that are typical of otosclerosis. For the lower frequencies (i.e., below 1500Hz), the percent difference in stapedial displacement was inversely proportional to the increase in stiffness. In other words, when stiffness was augmented by 10-fold, stapes displacement was approximately 10 times less. For the higher frequencies (above 1500Hz), the displacement of the stapes decreased linearly at a rate of approximately 10-fold per octave. With the increase in stapes mass, however, there was no significant variation in stapes displacement at the lower frequencies. In the higher frequencies, stapes displacement declined linearly until a maximal difference of $0.5 \times 10^{-10}$m was reached, at 8000Hz.

The normal displacement of the stapes was $10^{-8}$m, $10^{-9}$m, and $10^{-10}$m, respectively, for the frequencies 250-2000Hz, 4000Hz, and 8000Hz. These results are comparable to those found in the literature for normal stapedial displacement (Feng and Gan, 2002, 2004; Gan et al., 2007, 2010; Huber et al., 2003; Sun et al., 2002). However, the normal stapes displacement

![Figure 3. Spectrum in octave bands with sound pressure levels in dBHL and dBSPL (dB relative to $10^{-9}$m).](image)

![Figure 4. Normal displacement of the stapes and displacements after 10-fold and 100-fold increases in stapedial annular ligament (SAL) stiffness.](image)

![Figure 5. Normal displacement of the stapes and displacement after a 5-fold stapedial mass increase.](image)
in other studies (which adopted 3-D finite element modeling) was slightly greater and/or smaller (of the order of \( \sim 1 \times 10^{-10} \text{m} \)) (Dai et al., 2007; Gan et al., 2004; Liu et al., 2009), depending on the frequency range considered. A difference of up to 12.5% was noted in the range 100-8000Hz between the results of 3-D modeling reported in the literature and those of the discrete model presented herein. This difference in stapes displacement is small, considering the difference in methods among the studies.

**Discussion**

There is a paucity of articles reporting otosclerosis simulation, which is due to the difficulty in producing auditory system alterations consistent with the clinical findings of the disease. Our study was aimed at simulating the typical changes caused by otosclerosis using parameters from the literature, in order to better understand the impact of those changes on the different stages of the disease and to be able to contribute to future, more efficacious treatments.

The otosclerotic changes induce increased stiffness of the stapedial annular ligament, which can range from 10 to 100 times its normal value (Feng and Gan, 2004; Huber et al., 2003). They also lead to an increase in stapes mass, as evidenced by a 5-fold increment in the cell volume of the otosclerotic tissue (Frost, 1962). With the progression of the disease, new areas of bone tissue formation are found, which occur first in the otic capsule and may then extend into the oval window niche and stapes, and are rarely found in the malleus and incus (Beales, 1987; Hungria, 1988; Iyer and Gristwood, 1984).

Whatever the nature of the hearing loss, it can hinder communication, impact daily work activities, and even prevent an individual from listening to music (Albernaz, 2008). Therefore, any intervention towards a better understanding of the mechanisms of hearing loss and potential improvements is of extreme importance (Albernaz, 2008). These facts justify the study of otosclerosis, a disease that causes hearing loss, using a biomechanical model to investigate how certain changes that develop in otosclerosis can impact hearing and, consequently, the social interaction of individuals.

In the present study, a discrete mass-spring model was used to simulate the behavior of the normal and otosclerotic auditory system. In the literature, few articles can be found concerning the use of this type of model to study the auditory system in normal and otosclerotic conditions (Feng and Gan, 2002, 2004). Most of the published studies developed a 3-D model using the finite element method (Dai et al., 2007; Feng and Gan, 2002; Gan et al., 2004, 2007, 2010; Huber et al., 2003; Liu et al., 2009; Sun et al., 2002; Zhao et al., 2009). Regarding simulations of auditory system pathologies, the number of published studies using finite element modeling is smaller (Dai et al., 2007; Huber et al., 2003; Liu et al., 2009; Zhao et al., 2010), and there are even fewer reports on otosclerosis simulation (Huber et al., 2003). However, there are studies that merely mention otosclerosis (Garbe et al., 2010; Kelly et al., 2003).

In the model developed for the present study, a force equivalent to 90dB(SPL) was applied to the tympanic membrane and normal displacement of the stapes was noted between 250Hz and 8000Hz, as this range encompasses the frequencies assessed in audiometry. Between 250Hz and 2000Hz, the normal displacement of the stapes was \( 10^{-8} \)m; at 4000Hz, displacement was \( 10^{-9} \)m, and at 8000Hz, \( 10^{-10} \)m. These results are similar to those reported in the literature (Feng and Gan, 2002, 2004; Gan et al., 2007, 2010; Huber et al., 2003; Sun et al., 2002). However, the normal stapes displacement values found in other studies were slightly greater compared to our study (Dai et al., 2007; Gan et al., 2004; Liu et al., 2009). Probably, this small difference in displacement was due to the geometric models adopted in those studies.

Otosclerosis simulation, in this study, involved an increase in the stiffness of the stapedial annular ligament by 10-fold and 100-fold produced by a 90dB(SPL) force exerted on the tympanic membrane, which resulted—in both cases—in stapes displacement at the lower frequencies up to 1000Hz. This result is in line with the findings reported in the literature (Feng and Gan, 2004; Huber et al., 2003).

In addition to increased stapedial annular ligament stiffness, abnormal bony tissue formation is known...
to occur in otosclerosis (Brookler, 2008; Frost, 1962; Hungria, 1988; Miller and Schein, 2005; Min et al., 2010; Vicente et al., 2004). It is also known that the second most commonly affected site is the oval window area and the stapes footplate (Beales, 1987). Thus, our mass-spring model simulated a 5-fold increase in stapedial mass, based on the literature (Frost, 1962), and the influence of this parameter on the reduction of stapedial displacement was noted only at the higher frequencies, that is, above 2000Hz (Figure 5).

The results of these simulations showed that the reduction in stapedial displacements at certain frequencies could be related to the hearing losses observed in audiological tests according to the stage of otosclerosis.

At the early stages of otosclerosis, which typically affects young individuals, the audiogram shows a hearing loss for low-pitched sounds, reflected in an ascending audiometric curve in grade I disease, and the onset of hearing loss for high-pitched sounds as evidenced by the horizontal audiometric curve in grade II otosclerosis (Hungria, 1988). With the present model, it was noted that increasing the stiffness of the stapedial annular ligament resulted in reduced stapes displacement in the lower frequencies and the inferior range of the high frequencies up to 1000Hz. These results make it possible to predict that increased stapedial annular ligament stiffness is associated with the early stages of the disease, as previously reported (Feng and Gan, 2004; Rocha, 1994). Speech audiometry shows good speech discrimination in grade I and a slight decrease in speech discrimination in grade II (Hungria, 1988). However, an individual is unlikely to manifest any auditory complaint, since the loss of low-pitched sounds accounts for only 5% of speech intelligibility (Russo, 2009).

At the most advanced stages of the disease, grades III and IV, audiological tests reveal a descending audiometric curve, with hearing loss for high-pitched sounds or even a lack of response for those sounds (Hungria, 1988). Further, there is overgrowth of bone tissue—initially in the otic capsule, which may progress further and extend to the oval window and stapes. This process is rarely found in the other ear ossicles (Beales, 1987; Hungria, 1988; Iyer and Gristwood, 1984). In our discrete mass-spring model of the auditory system, simulating increased stapedial mass resulted in reduced displacement of the stapes only at the higher frequencies (above 2000 Hz), as expected for the late stages of the disease. The overgrowth of bony tissue is probably associated with the more advanced stages of the disease, as reported qualitatively in the literature (Frost, 1962; Hungria, 1988; Miller and Schein, 2005; Min et al., 2010; Palacios and Valvassori, 2001; Vicente et al., 2004). Speech audiometry shows a marked decline in speech discrimination (Hungria, 1988); consequently, the individual complains of difficulties in understanding what is spoken, even with great intensity, particularly in the case of losses around 90 dB (Albernaz, 2008). This occurs due to the fact that the significant hearing loss for high-pitched sounds from 1000 Hz accounts for 60% of speech intelligibility (Russo, 2009).

The discrete mass-spring model of the ear contributed to an enhanced understanding of how the structures affected by otosclerosis influence hearing, and how they relate to the different grades of the disease. When investigating the altered parameters in otosclerosis, it was possible to predict both quantitatively and qualitatively, based on the discrete mass-spring model, the influence of stapedial annular ligament stiffness (Dai et al., 2009; Feng and Gan, 2004; Huber et al., 2003; Min et al., 2010) at the early stages and the influence of increased stapedial mass (Beales, 1987; Brookler, 2008; Frost, 1962; Hungria, 1988; Iyer and Gristwood, 1984; Miller and Schein et al., 2005; Min et al., 2010; Vicente et al., 2004) at the advanced stages, thereby corroborating the qualitative data already reported in the literature.

Despite the limitations of this model, considering that it is one-dimensional and constituted by masses and springs that do not accurately portray the geometry of the ear, it was found that it was capable of defining and relating the different parameters of otosclerosis to the different stages of otosclerosis. Thus, imaging studies in individuals with otosclerosis showing bony tissue overgrowth in the otic capsule, the oval window, or the stapes, can indicate advancing disease and predict the patient’s prognosis, as well as serve as an adjuvant in the investigation and treatment of the patient.

Furthermore, considering that increased stapedial annular ligament stiffness is suggestive of early stage otosclerosis—as shown in the present study—and that the disease is rarely symptomatic at this point, the inclusion of stapedial annular ligament status assessment in the audiological tests is justified. The immittance test includes the stapedial reflex test, which measures stapedial muscle contraction when strongly stimulated. We propose that this investigation should also be conducted for the stapedial annular ligament in order to assist in the early diagnosis of otosclerosis, a disease that affects between 0.5% and 1% of the population, and presents bilaterally in 70% to 85% of cases (Testa et al., 2002).

The early diagnosis of changes in the stapedial annular ligament can have a positive impact on sound transmission in the middle ear, as shown in previous
studies (Feng and Gan, 2004; Huber et al., 2003). Currently, there is no test to assess the stapedial annular ligament function. Therefore, research aimed at devising diagnostic tests of stapedial annular ligament compromise is critical to allow early interventions regarding the hearing losses deriving from such alterations.

Overall, the model described in this paper showed that increased stiffness of the stapedial annular ligament gives rise to reduced stapedial displacement at the lower frequencies, which is consistent with the early audiometric findings in otosclerosis. The increase in bony tissue mass caused decreased displacement of the stapes at the higher frequencies, which can also be noted in the audiometric configuration of individuals in a more advanced stage of otosclerosis.

The present study showed the important influence of the stapedial annular ligament in the transmission of the sound wave through the middle ear, which warrants further studies in order to find ways to include functional diagnosis of the stapedial annular ligament in audiological tests to enable the early detection of hearing losses.

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References

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