

Experimental Evaluation of 300 °C section of Cu-In-Ni Phase Diagram, Hardness and Electrical Conductivity of Selected Alloy

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The paper reports comparative experimental and thermodynamic calculation of a Cu-In-Ni ternary system. An isothermal section of the Cu-In-Ni system at 300 °C was extrapolated using optimized thermodynamic parameters for the constitutive binary systems from literature. Microstructural and phase composition analysis were carried out using scanning electron microscopy coupled with energy dispersive spectrometry (SEM-EDS) and X-ray powder diffraction (XRD) technique. Brinell hardness and electrical conductivity of a selected number of alloy samples with compositions along three vertical sections (Cu-In0.5Ni0.5, In-Cu0.8Ni0.2, and $x(\text{In}) = 0.4$) of the studied Cu-In-Ni system were experimentally determined. Based on the obtained experimental results and by using appropriate mathematical models values of hardness and electrical conductivity for the whole ternary system were predicted. A close agreement between calculations and experimental results was obtained both in case of thermodynamic, electrical conductivity and hardness predictions.

Keywords: *The Cu-In-Ni ternary system, isothermal section at 300 °C, microstructural analysis, Brinell hardness, electrical conductivity.*

1. Introduction

Nickel and nickel-based alloys are widely used in different industries such as chemical, automotive, marine etc. for making vessels, pipes, heat exchangers, pumps, impellers, valves, and other type of equipment¹. Furthermore, nickel with copper forms high-quality alloys with a variety of applications²⁻⁴. Especially Cu-Ni and Cu-Ni-based alloys are used for making parts in the electronics industry⁵⁻⁸ e.g. for alkaline batteries, gas engines and turbines⁹, optical mirrors^{10,11}, equipment for food, chemical and petrochemical industries, as well as for galvanic coating of steel objects. The most commonly used Ni-Cu alloy is Monel¹²⁻¹⁴, which is primarily composed of nickel (up to 67%) and copper, with small amounts of iron, manganese, carbon, and silicon.

On the other hand, it is well known that copper is a widely used material because of its high electrical and thermal conductivity. By adding a nickel to copper, it is possible to improve the mechanical properties and corrosion resistance

of copper, while adding indium lowers its melting point. To the extent of our knowledge, up to now, ternary Cu-In-Ni alloys have not been investigated from the point of view of mechanical and electrical properties. Furthermore, it can be expected that some of these ternary alloys may be excellent candidates for some of the aforementioned applications.

The Cu-In-Ni ternary system has been previously experimentally and thermodynamically assessed by Minić et al.¹⁵. In their study, Minić et al.¹⁵ reported the liquidus surface, three vertical sections and isothermal sections at 400 °C and 500 °C.

In the current study, microstructures, electrical and mechanical properties of selected alloy samples from the isothermal sections at 300 °C of the Cu-In-Ni ternary system are presented. Additionally, chemical and phase compositions of the studied alloys determined by SEM-EDS and XRD analyses are presented as well. The applied research procedure is similar to that given in¹⁶⁻¹⁸ and it is aimed at providing better insight into properties of alloys which should contribute to further expansion of their application possibilities.

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2. Experimental Procedure

Nineteen ternary and three binary alloy samples (marked as a B1, B2, and B3) were prepared from copper, indium, and nickel (99.999 at. %) from Alfa Aesar (Germany) in an induction furnace under high-purity argon atmosphere. In general, the average loss of mass during melting of samples was about 2 mass pct. Then prepared alloy samples were placed in evacuated quartz tubes and sealed. Then alloy samples were annealed at 300 °C for 4 weeks at high-temperature furnace (GSL1700X, Hefei Kejing Materials Technology Co., Ltd., Hefei, China) with estimated error of the temperature ± 1 °C. After annealing samples were quenched into a water and ice mixture in order to retain reached phase equilibrium. Annealed samples were divided into two part. One part of the sample is subjected to microstructural analysis, hardness and electroconductivity measurements. This part of the sample were prepared by the conventional metallographic procedure without etching. Prepared sample was oval and polished with parallel sides. Polished side of the sample were first subjected to EDS elemental mapping to check compositional homogeneity and possible segregation. Further, overall compositions and compositions of coexisting phases were determined using EDS point and area analysis. This test was carried out on TESCAN VEGA3 scanning electron microscope with energy dispersive spectroscopy (EDS) (Oxford Instruments X-act). Further same sample at the same polished part was subjected to the microhardness test. For this test was used Vickers microhardness tester Sinowon, model Vexus ZHV-1000V. After this test electrical conductivity measurements were carried out by using Foerster SIGMATEST 2.069 instrument. At last step on same samples, the hardness of the samples was determined by using a Brinell hardness tester INNOVATEST, model Nexus 3001.

The second part of the sample was grinded and examined by using X-ray diffraction. XRD patterns of the studied samples were recorded on a D2 PHASER powder diffractometer equipped with a dynamic scintillation detector and ceramic X-ray Cu tube (KFLCu-2K) in a 2θ range of 5 to 75 deg with a step size of 0.02 deg. The patterns were analyzed using Topas 4.2 software and ICDD databases PDF2(2013).

3. Results and Discussion

The isothermal section at 300 °C of the Cu-In-Ni ternary system has been thermodynamically predicted using optimized thermodynamic parameters for the constitutive binary systems from literature¹⁹⁻²¹. The parameters for the binary Cu-In a system were taken from Liu et al.¹⁹, for the In-Ni system from Waldner and Ipser²⁰, and for the Cu-Ni binary system from Mey²¹ (supplementary information). Calculations were performed using PANDAT software²².

The list of phases from constitutive binary subsystems considered for thermodynamic binary-based prediction together with their corresponding Pearson symbols is given in Table 1.

The calculated isothermal section of the Cu-In-Ni ternary system at 300 °C is presented in Fig. 1. The alloy samples selected for experimental investigation are also marked in Fig. 1.

Compositions of the selected alloy samples lie along three vertical sections red squares Cu-In0.5Ni0.5, violet squares In-Cu0.8Ni0.2 and blue squares $x(\text{In}) = 0.4$ of the studied ternary system. The all selected samples marked in Fig. 1 were investigated using the same experimental techniques.

Out of all predicted regions from the isothermal section at 300 °C, seven regions were selected and investigated. Six of the investigated regions are three-phase regions and the remaining one is a two-phase region.

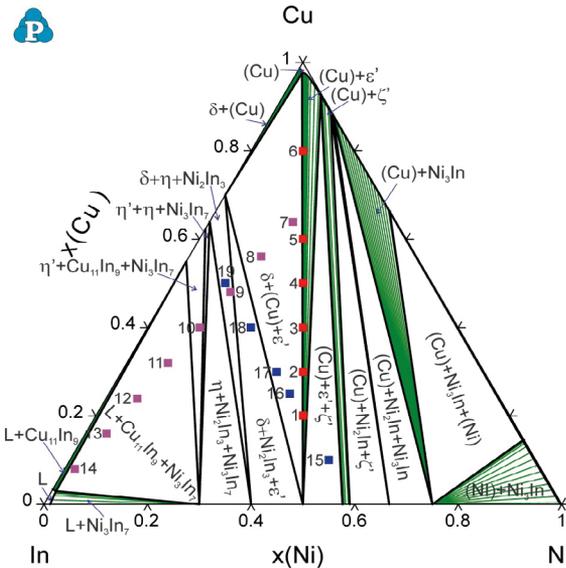
In Table 2 are given the experimental results of EDS and XRD analyses.

According to the thermodynamic calculations, (see Fig. 1) samples from number 1 to 6 belong to the two-phase region (Cu)+ ϵ' (NiIn). The obtained experimental results of these six alloy samples confirm the existence of this two-phase region. In all cases, the solubility of copper in intermetallic phase ϵ' (NiIn) was found to be less than 1 at. % and thus it was negligible. Also in the case of the solid solution (Cu), the detected solubility of In was negligible. The other obtained results related to the identified phases were found to be the same as predicted so the existence of all predicted regions was confirmed. Moreover, the subsequent XRD analysis has also confirmed the presence of the same phases as were predicted by thermodynamic calculations and determined by EDS analysis. Figure 2 shows microstructures of the six alloy samples selected out of nineteen studied alloys. Sample 6 belongs to the two-phase region while the rest samples 8, 9, 10, 11 and 12 are from three-phase regions. The phases identified using the results of energy dispersive spectrometry (EDS) are marked on the presented microstructures.

In microstructure of sample 6, two phases are visible, solid solution (Cu) which is a dominant phase and binary intermetallic compound ϵ' (NiIn). Three phase region $\delta(\text{Cu}_7\text{In}_3)+(\text{Cu})+\epsilon'(\text{NiIn})$ is visible at the microstructure of sample 8. The alloy samples 9 and 10 (Fig.2c and Fig.2d) also belong to three-phase regions. As can be seen from Fig.2c the δ phase is the most dominant phase within the microstructure of sample 9 whereas Ni_2In_3 intermetallic compound appears as light phase situated at its grain boundaries. The alloy sample 10 (Fig.2d) seems to have more fine-grained microstructure compared to the rest of the studied alloy samples. In its microstructure (Fig.2d) η' phase can be observed as a small, black and round phase evenly distributed throughout the microstructure of the alloy. The samples 11 and 12 belong to the three-phase region in which liquid phase L is present ($\text{L}+\text{Ni}_3\text{In}_7+\text{Cu}_{11}\text{In}_9$). It can

Table 1. Considered phases in Cu-In-Ni ternary system and their crystal structures

Phase name	Common name	Space group	Strukturbericht designation	Pearson symbol
LIQUID	Liquid		-	-
TETRAG_A6	(In)	$I4/mmm$	A6	$tI2$
FCC_A1	(Cu,Ni)	$Fm\bar{3}m$	A1	$cF4$
BCC_A2	β (Cu ₄ In)	$Im\bar{3}m$	A2	$cI2$
CUIN_DELTA	δ (Cu ₇ In ₃)	$P\bar{1}$...	$aP40$
CUIN_ETAP	η (Cu ₂ In)	$P6_3/mmc$	$B8_2$	$hP6$
CUIN_ETA	η' (CuIn)	$P6_3/mmc$	$B8_1$	$hP4$
CUIN_THETA	Cu ₁₁ In ₉	$C2/m$...	$mC20$
CUIN_GAMMA	γ (Cu ₉ In ₄)	$P\bar{4}_2m$...	$cP52$
NI3IN7	Ni ₂₈ In ₇₂	$Im\bar{3}m$...	$cI40$
NI2IN3	Ni ₂ In ₃	$P\bar{3}m1$	$D5_{13}$	$hP5$
INNI_DELTA	δ (NiIn)	$Pm\bar{3}m$	B2	$cP2$
NIIN	ϵ' (NiIn)	$P6/mmm$	B35	$hP6$
INNI_CHI_PRIME	ζ' (Ni ₁₃ In ₉)	$C2/m$...	$mC44$
INNI_CHI	ζ	
NI2IN	Ni ₂ In	$P6_3/mmc$	$B8_2$	$hP6$
NI3IN	Ni ₃ In	$P6_3/mmc$	$D0_{19}$	$hP6$


Figure 1. Predicted isothermal section of the ternary Cu-In-Ni system at 300 °C with marked compositions of the studied samples

be observed in Fig.2e and Fig.2f as the dark phase trapped between intermetallic compounds. The intermetallic compound Cu₁₁In₉ appears as the darkest phase in the microstructures of the alloy samples 11 and 12 while the Ni₃In₇ intermetallic compound is the most abundant phase.

Lattice parameters of the detected phases were compared with lattice parameters from literature²³⁻³⁰. Two XRD patterns with identified phases, one for the sample 1 and the other for the sample 15 are shown in Figure 3, as an illustration.

From Table 2 it can be seen that the experimentally determined values of lattice parameters for a solid solution (Cu) slightly vary for different alloy samples between 3.5885(1) Å and 3.6023(7) Å. This discrepancy can be explained by taking into account high solubility of nickel in solid solution (Cu) e.g. determined value of a lattice parameter for (Cu) phase in sample 15 is shifted towards the lower value and considering that lattice parameter for (Ni) phase are $a=b=c=3.499$ Å³¹ it can be assumed that the obtained results may be related to the solubility of nickel.

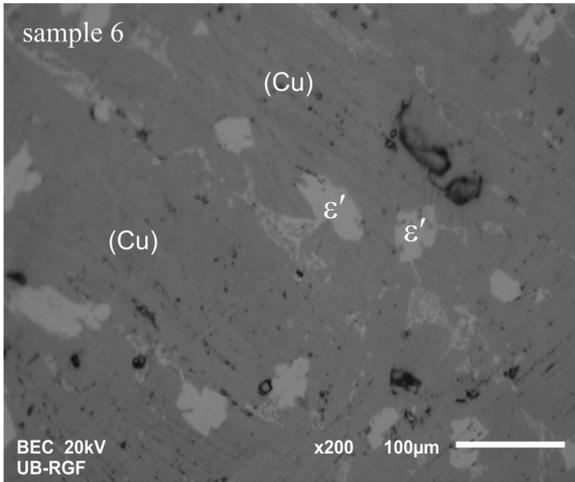
The hardness of the alloys of the Cu-In-Ni ternary system was determined using Brinell method. Measured values of the Brinell hardness of the studied alloy samples are given in Table 3 along with experimentally obtained values of the hardness of three binary alloys (B1, B2, and B3) and literature values for pure elements³².

Figure 4 shows a graphical representation of the obtained experimental results given in Table 3.

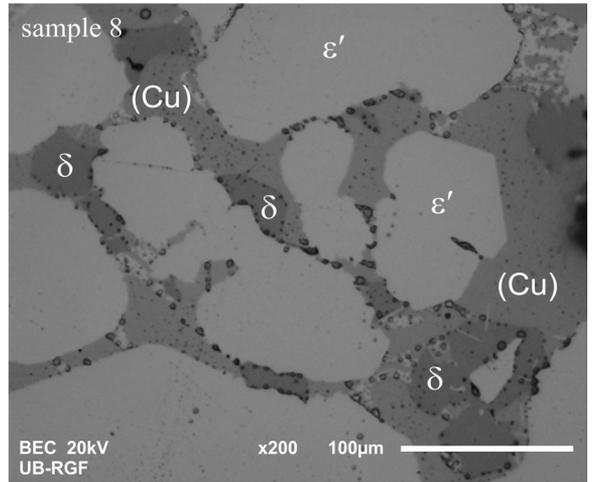
The experimentally obtained results clearly point out that Cu rich ternary alloys have a higher value of hardness. From all ternary alloys, alloy Cu₈₀In₁₀Ni₁₀ have the highest hardness. Experimentally determined value is 423.4 MN/m². The ternary alloy Cu₈₀In₁₀Ni₁₀ consists of the two-phase solid solution (Cu) and intermetallic compound ϵ' (NiIn). Since the solid solution (Cu) is in majority and hardest phase in this system it is expected that this will influence on hardness which is experimentally determined and results that alloys rich with (Cu) phase have the highest hardness.

Table 2. Experimentally determined phase compositions and lattice parameters of phases in the ternary Cu–In–Ni system at 300 °C

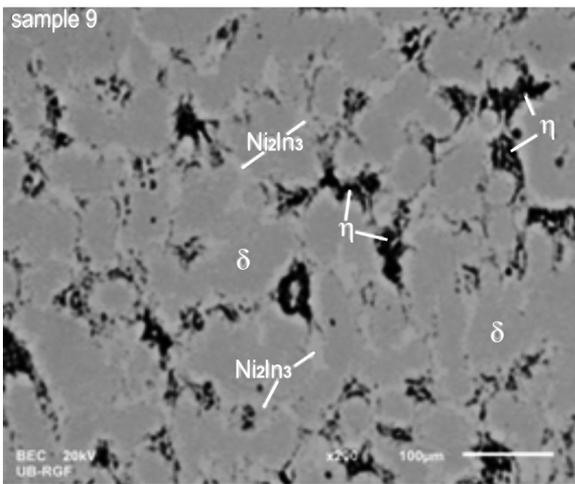
S.	Exp. phases	EDS analysis			XRD analysis		
		Exp. compositions of phases (at.%)			Lattice parameters (Å)		
		Cu	In	Ni	a this work/literature	b this work/literature	c this work/literature
1	(Cu)	94.23±0.2	0.56±0.4	5.21±0.6	3.5993(1)/3.625[30]		4.3569(3)/4.353[23]
	ϵ' (NiIn)	0.67±0.1	50.60±0.3	48.73±0.2	4.5439(7)/4.545[23]		
2	(Cu)	94.53±0.3	0.65±0.7	4.82±0.1	3.5986(3)/3.625[30]		4.3503(5)/4.353[23]
	ϵ' (NiIn)	1.03±0.5	49.87±0.3	49.1±0.4	4.5454(5)/4.545[23]		
3	(Cu)	94.21±0.2	0.57±0.6	5.22±0.3	3.5976(4)/3.625[30]		4.3556(8)/4.353[23]
	ϵ' (NiIn)	0.49±0.4	51.43±0.7	48.08±0.5	4.5465(1)/4.545[23]		
4	(Cu)	96.2±0.2	0.42±0.6	3.38±0.5	3.5976(2)/3.625[30]		4.3505(1)/4.353[23]
	ϵ' (NiIn)	0.81±0.4	50.21±0.2	48.98±0.2	4.5455(2)/4.545[23]		
5	(Cu)	95.1±0.4	0.4±0.4	4.5±0.2	3.5974(4)/3.625[30]		4.3563(3)/4.353[23]
	ϵ' (NiIn)	0.66±0.2	49.65±0.2	49.69±0.1	4.5445(5)/4.545[23]		
6	(Cu)	96.08±0.1	0.63±0.4	3.29±0.4	3.5967(7)/3.625[30]		4.3549(7)/4.353[23]
	ϵ' (NiIn)	0.67±0.4	50.31±0.2	49.02±0.1	4.5449(2)/4.545[23]		
7	δ (Cu ₃ In ₂)	68.98±0.6	29.81±0.5	1.21±0.1	6.7327(1)/6.733[29]	9.1339(1)/9.134[29]	10.0761(8)/10.074[29] 4.3518(7)/4.353[23]
	(Cu)	95.04±0.1	0.3±0.2	4.66±0.6	3.6021(2)/3.625[30]		
	ϵ' (NiIn)	0.87±0.5	48.17±0.6	50.96±0.3	4.5446(1)/4.545[23]		
8	δ (Cu ₃ In ₂)	70.18±0.7	29.15±0.1	0.67±0.3	6.7337(2)/6.733[29]	9.1343(2)/9.134[29]	10.0765(1)/10.074[29] 4.3529(4)/4.353[23]
	(Cu)	94.08±0.3	0.73±0.4	5.19±0.2	3.6009(7)/3.625[30]		
	ϵ' (NiIn)	0.13±0.2	49.03±0.1	50.84±0.5	4.5443(7)/4.545[23]		
9	δ (Cu ₃ In ₂)	68.74±0.2	29.54±0.5	1.72±0.4	6.7378(1)/6.733[29]	9.1354(1)/9.134[29]	10.0737(7)/10.074[29] 5.2928(9)/5.295[23] 5.2387(2)/5.2328[26]
	Ni ₂ In ₃	0.57±0.3	61.06±0.3	38.37±0.1	4.3857(1)/4.387[23]		
	η (Cu ₂ In)	67.32±0.4	32.15±0.3	0.53±0.2	4.2987(1)/4.2943[26]		
10	Cu ₁₁ In ₉	54.32±0.3	44.93±0.2	0.75±0.7	12.8139(7)/12.814[28]	4.3557(2)/4.3543[28]	7.3523(2)/7.353[28] 4.9633(9)/4.965[27]
	Ni ₃ In ₇	0.32±0.2	71.42±0.6	28.26±0.2	9.1799(2)/9.18[24]		
	η (CuIn)	62.28±0.3	37.24±0.2	0.48±0.7	4.2498(1)/4.250[27]		
11	L	2.43±0.3	95.81±0.2	1.76±0.5	-	4.3576(1)/4.3543[28]	7.3522(1)/7.353[28]
	Cu ₁₁ In ₉	56.93±0.2	43.05±0.2	0.02±0.3	12.8187(7)/12.814[28]		
	Ni ₃ In ₇	0.73±0.1	69.64±0.3	29.63±0.8	9.1803(5)/9.18[24]		
12	L	3.48±0.5	95.98±0.5	0.54±0.1	-	4.3522(5)/4.3543[28]	7.3545(7)/7.353[28]
	Cu ₁₁ In ₉	55.54±0.7	43.56±0.7	0.90±0.4	12.8112(4)/12.814[28]		
	Ni ₃ In ₇	1.15±0.3	70.89±0.1	27.96±0.2	9.1798(4)/9.18[24]		
13	L	2.7±0.6	96.34±0.1	0.96±0.7	-	4.3587(4)/4.3543[28]	7.3521(2)/7.353[28]
	Cu ₁₁ In ₉	54.69±0.5	44.83±0.4	0.48±0.2	12.8156(6)/12.814[28]		
	Ni ₃ In ₇	1.66±0.3	68.13±0.2	30.21±0.1	9.1799(1)/9.18[24]		
14	L	2.68±0.3	96.23±0.2	1.09±0.7	-	4.3527(1)/4.3543[28]	7.3555(7)/7.353[28]
	Cu ₁₁ In ₉	54.10±0.4	45.83±0.3	0.07±0.5	12.8144(2)/12.814[28]		
	Ni ₃ In ₇	0.80±0.1	70.54±0.3	28.66±0.3	9.1801(5)/9.18[24]		
15	(Cu)	92.35±0.4	0.46±0.7	7.19±0.1	3.5885(1)/3.625[30]	8.3273(6)/8.329[25]	4.3518(9)/4.353[23] 8.9763(1)/8.977[25]
	ϵ' (NiIn)	0.18±0.3	48.94±0.2	50.88±0.6	4.5473(2)/4.545[23]		
	ζ (Ni ₃ In ₃)	0.43±0.3	40.04±0.1	59.53±0.3	14.6433(7)/14.646[25]		
16	δ (Cu ₃ In ₂)	69.58±0.2	30.01±0.1	0.41±0.2	6.7343(1)/6.733[29]	9.1365(1)/9.134[29]	10.0712(3)/10.074[29] 4.3518(8)/4.353[23]
	(Cu)	97.26±0.1	1.41±0.7	1.33±0.7	3.6018(1)/3.625[30]		
	ϵ' (NiIn)	0.77±0.1	49.74±0.5	49.49±0.7	4.5433(6)/4.545[23]		
17	δ (Cu ₃ In ₂)	70.04±0.2	28.45±0.6	1.51±0.3	6.7329(8)/6.733[29]	9.1339(2)/9.134[29]	10.0733(3)/10.074[29] 4.3545(1)/4.353[23]
	(Cu)	97.12±0.1	1.23±0.4	1.65±0.2	3.6023(7)/3.625[30]		
	ϵ' (NiIn)	0.14±0.3	49.33±0.2	50.53±0.3	4.5423(2)/4.545[23]		
18	δ (Cu ₃ In ₂)	69.13±0.1	28.93±0.3	1.94±0.5	6.7334(9)/6.733[29]	9.1355(1)/9.134[29]	10.0765(3)/10.074[29] 5.2977(6)/5.295[23] 4.3565(4)/4.353[23]
	Ni ₃ In ₇	0.17±0.1	30.25±0.4	69.58±0.4	4.3844(6)/4.387[23]		
	ϵ' (NiIn)	0.13±0.5	51.31±0.5	48.56±0.4	4.5439(4)/4.545[23]		
19	δ (Cu ₃ In ₂)	68.65±0.4	29.98±0.3	1.37±0.2	6.7387(8)/6.733[29]	9.1323(8)/9.134[29]	10.0757(7)/10.074[29] 5.2944(6)/5.295[23] 5.2338(4)/5.2328[26]
	Ni ₃ In ₇	0.61±0.3	31.75±0.3	67.64±0.3	4.3854(4)/4.387[23]		
	η (Cu ₂ In)	67.32±0.3	32.12±0.2	0.56±0.3	4.2932(1)/4.2943[26]		



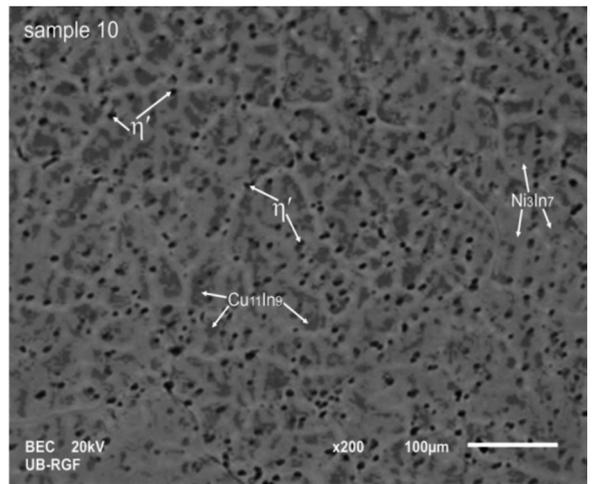
(a) sample 6



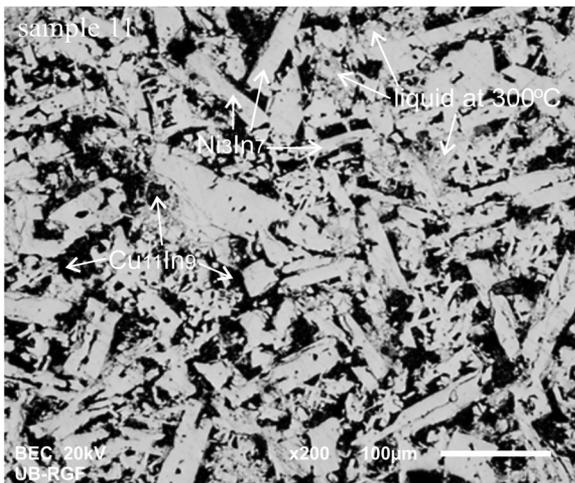
(b) sample 8



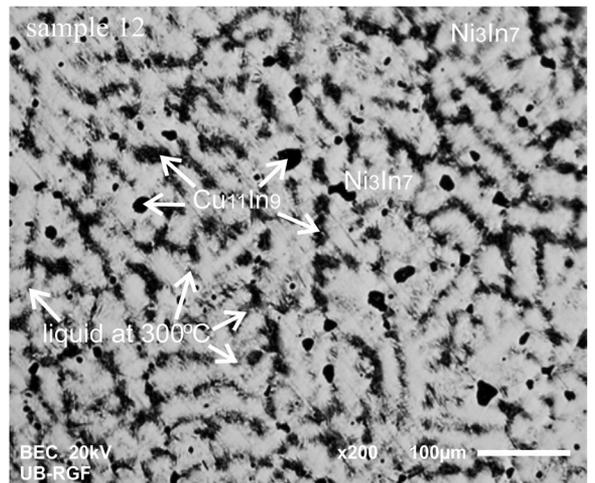
(c) sample 9



(d) sample 10



(e) sample 11



(f) sample 12

Figure 2. Microstructures of the alloys analyzed using SEM-EDS technique: a) sample 6, b) sample 8, c) sample 9, d) sample 10, e) sample 11 and f) sample 12

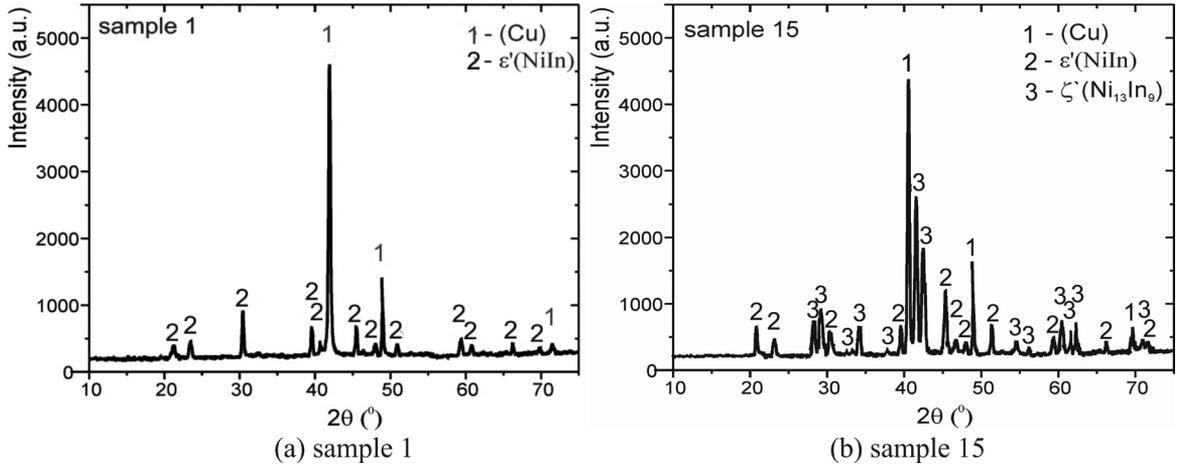


Figure 3. XRD patterns of the studied alloys: a) sample 1 and b) sample 15

Table 3. Brinell hardness of the investigated alloys from the Cu-In-Ni ternary system

Number	Composition of sample (at.%)	Brinell hardness (MN/m ²)			
		Values for different measurements			Mean value
		1	2	3	
B1	In ₅₀ Ni ₅₀	288.4	290.2	290.5	289.7
1	Cu ₂₀ In ₄₀ Ni ₄₀	154.4	154.9	155.8	155.0
2	Cu ₃₀ In ₃₅ Ni ₃₅	185.9	165.9	174.9	175.5
3	Cu ₄₀ In ₃₀ Ni ₃₀	267.8	286.4	283.1	279.1
4	Cu ₅₀ In ₂₅ Ni ₂₅	343.8	340.5	341.2	341.8
5	Cu ₆₀ In ₂₀ Ni ₂₀	351.6	356.6	353.2	353.8
6	Cu ₈₀ In ₁₀ Ni ₁₀	423.8	423.8	422.6	423.4
Ref. ^[32]	Cu				874
B2	Cu ₈₀ Ni ₂₀	532.8	531.5	533.2	532.5
7	Cu ₆₄ In ₂₀ Ni ₁₆	340.2	338.2	337.4	338.6
8	Cu ₅₆ In ₃₀ Ni ₁₄	318.2	319.3	318.6	318.7
9	Cu ₄₈ In ₄₀ Ni ₁₂	217.4	217.5	216.4	217.1
10	Cu ₄₀ In ₅₀ Ni ₁₀	184.4	183.2	184.8	184.1
11	Cu ₃₂ In ₆₀ Ni ₈	52.8	40.9	34.8	42.8
12	Cu ₂₄ In ₇₀ Ni ₆	40.8	42.8	41.2	41.6
13	Cu ₁₆ In ₈₀ Ni ₄	24.1	24.9	23.6	24.2
14	Cu ₈ In ₉₀ Ni ₂	21.6	19.2	18.6	19.8
Ref. ^[32]	In				8.83
B3	Cu ₅₀ In ₅₀	2.75	2.77	2.7	2.74
15	Cu ₁₀ In ₄₀ Ni ₅₀	334.6	325.6	312.2	324.1
16	Cu ₂₅ In ₄₀ Ni ₃₅	245.7	223.8	236.2	235.2
17	Cu ₃₀ In ₄₀ Ni ₃₀	224.6	224.2	222.6	223.8
18	Cu ₄₀ In ₄₀ Ni ₂₀	210.8	212.3	211.7	211.6
19	Cu ₅₀ In ₄₀ Ni ₁₀	177.5	176.4	178.3	177.4
Ref. ^[32]	Ni				700

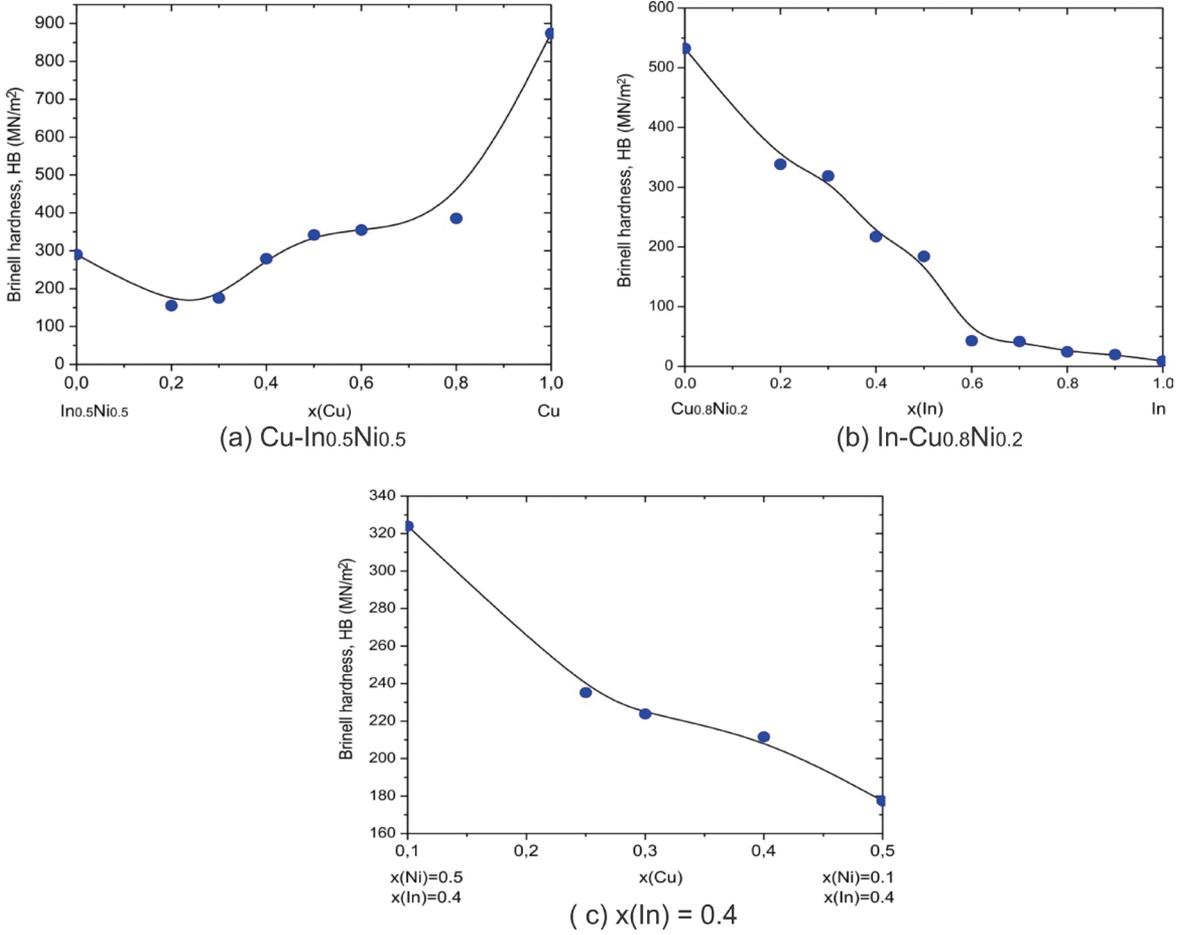


Figure 4. Measured values of Brinell hardness of the alloys from the three studied vertical sections: a) Cu-In_{0.5}Ni_{0.5}, b) In-Cu_{0.8}Ni_{0.2} and c) x(In)=0.4

By using collected experimental results and an appropriate mathematical model it was possible to calculate values of hardness over the whole compositional range.

The mathematical model of Brinell hardness dependence on alloy composition was defined using Design-Expert v.9.0.3.1. software package³³. Based on the preliminary statistical analysis, a Cubic Mixture Model was selected out of possible canonical or Scheffe models³⁴⁻³⁶ that meet the requirements of adequacy:

$$\hat{y} = \sum_{i=1}^q \beta_i x_i + \sum_{i<j}^{q-1} \beta_{ij} x_i x_j + \sum_{i<j}^{q-1} \delta_{ij} x_i x_j (x_i - x_j) + \sum_{i<j<k}^{q-2} \beta_{ijk} x_i x_j x_k \quad (1)$$

Adequacy of the selected model was confirmed by the Analysis of variance (ANOVA). The F-value of the model was found to be 109.94 which implies that the model is significant. In addition, there is only a 0.01% chance that a "Model F-Value" this large could occur due to noise. The final equation of the predictive model in terms of actual components is:

$$\begin{aligned} HB(MN/m^2) = & 785.2466 \cdot x(Cu) \\ & + 22.46841 \cdot x(In) + 700 \cdot x(Ni) \\ & - 1559.52 \cdot x(Cu) \cdot x(In) - 5194.47 \cdot x(Cu) \cdot x(Ni) \\ & - 378.728 \cdot x(In) \cdot x(Ni) + 13997.19 \cdot x(Cu) \cdot z(In) \cdot x(Ni) \quad (2) \\ & - 1711.89 \cdot x(Cu) \cdot x(In) \cdot (x(Cu) - x(In)) \\ & + 6113.256 \cdot x(Cu) \cdot x(Ni) \cdot (x(Cu) - x(Ni)) \\ & - 5129.75 \cdot x(In) \cdot x(Ni) \cdot (x(In) - x(Ni)) \end{aligned}$$

Presented predicted model is just related to the hardness of alloys from the ternary Cu-In-Ni system at 300 °C which is dependent just on the composition.

The resulting iso-lines contour plot for Brinell hardness of alloys defined by Equation 2 is shown in Figure 5.

The succeeding electrical conductivity measurements were carried out on the same alloy samples. The experimentally determined values of electrical conductivity for the selected ternary and three binary alloys (B1, B2, and B3) are presented together with literature values for pure elements³⁷ in Table 4.

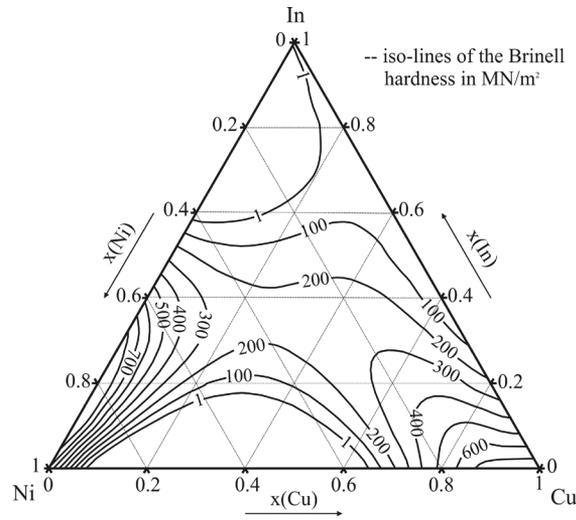


Figure 5. Iso-lines of the Brinell hardness of Cu-In-Ni ternary system.

Table 4. Electrical conductivity of the studied alloys from the Cu-In-Ni ternary system

Number	Composition of sample (at.%)	Electrical conductivity (MS/m)				Mean value
		Values for different measurements				
		1	2	3	4	
B1	In ₅₀ Ni ₅₀	1.0268	1.0321	1.0021	1.0286	1.0224
1	Cu ₂₀ In ₄₀ Ni ₄₀	0.7808	0.7305	0.7996	0.7342	0.7613
2	Cu ₃₀ In ₃₅ Ni ₃₅	0.8316	0.8463	0.8294	0.8613	0.8422
3	Cu ₄₀ In ₃₀ Ni ₃₀	1.715	1.677	1.642	1.723	1.6893
4	Cu ₅₀ In ₂₅ Ni ₂₅	0.4171	0.4185	0.4224	0.4384	0.4241
5	Cu ₆₀ In ₂₀ Ni ₂₀	7.9454	8.0218	8.0253	8.1023	8.0237
6	Cu ₈₀ In ₁₀ Ni ₁₀	8.2265	8.2324	8.2502	8.2421	8.2378
Ref. ^[37]	Cu					59
B2	Cu ₈₀ Ni ₂₀	6.2412	6.2234	6.2556	6.2382	6.2396
7	Cu ₆₄ In ₂₀ Ni ₁₆	0.4721	0.4468	0.4657	0.4722	0.4642
8	Cu ₅₆ In ₃₀ Ni ₁₄	1.6384	1.6227	1.6187	1.6234	1.6258
9	Cu ₄₈ In ₄₀ Ni ₁₂	2.494	2.51	2.535	2.498	2.5093
10	Cu ₄₀ In ₅₀ Ni ₁₀	1.948	1.917	1.883	1.825	1.8933
11	Cu ₃₂ In ₆₀ Ni ₈	4.165	4.078	4.165	4.114	4.1305
12	Cu ₂₄ In ₇₀ Ni ₆	4.531	4.5226	4.5324	4.518	4.526
13	Cu ₁₆ In ₈₀ Ni ₄	5.1864	5.1923	5.2005	5.112	5.1728
14	Cu ₈ In ₉₀ Ni ₂	5.6425	5.5966	5.6228	5.6321	5.6235
Ref. ^[37]	In					12
B3	Cu ₅₀ In ₅₀	3.034	3.062	3.051	3.053	3.05
15	Cu ₁₀ In ₄₀ Ni ₅₀	1.005	1.034	0.9998	1.047	1.0215
16	Cu ₂₅ In ₄₀ Ni ₃₅	0.4683	0.4617	0.4599	0.463	0.4632
17	Cu ₃₀ In ₄₀ Ni ₃₀	1.8226	1.8395	1.9239	1.8168	1.8507
18	Cu ₄₀ In ₄₀ Ni ₂₀	2.3246	2.3168	2.2621	2.3345	2.3095
19	Cu ₅₀ In ₄₀ Ni ₁₀	1.81	1.861	1.779	1.793	1.8108
Ref. ^[37]	Ni					14

Graphical presentation of the correlation between electrical conductivity and mole fraction of components for the all investigated samples is shown in Figure 6.

The presented experimental results (Table 4 and Fig. 6) show that $\text{Cu}_{60}\text{In}_{20}\text{Ni}_{20}$ and $\text{Cu}_{80}\text{In}_{10}\text{Ni}_{10}$ ternary alloys have the highest electrical conductivity of the all studied ternary alloys.

Calculation of electrical conductivity of the alloys from the Cu-In-Ni ternary system was carried out in the same manner as the aforementioned Brinell hardness calculation.

In this case, also the model summary statistics suggested the Cubic Mixture Model. The F-value of the Model determined using analysis of variance (ANOVA) was found to be 49.82 which implies that the model is significant. The final equation of the predictive model in terms of actual components is:

$$\begin{aligned} \sigma(\text{MS/m}) = & 51.12361 \cdot x(\text{Cu}) + 8.553991 \cdot x(\text{In}) \\ & + 14.3 \cdot x(\text{Ni}) - 107.169 \cdot x(\text{Cu}) \cdot x(\text{In}) \\ & - 141.114 \cdot x(\text{Cu}) \cdot x(\text{Ni}) - 48.7082 \cdot x(\text{In}) \cdot x(\text{Ni}) \\ & + 255.0256 \cdot x(\text{Cu}) \cdot x(\text{In}) \cdot x(\text{Ni}) \\ & - 33.2152 \cdot x(\text{Cu}) \cdot x(\text{In}) \cdot (x(\text{Cu}) - x(\text{In})) \\ & - 154.213 \cdot x(\text{Cu}) \cdot x(\text{Ni}) \cdot (x(\text{Cu}) - x(\text{Ni})) \\ & + 86.45382 \cdot x(\text{In}) \cdot x(\text{Ni}) \cdot (x(\text{In}) - x(\text{Ni})) \end{aligned} \quad (3)$$

The presented model is related to the ternary alloys at 300 °C depending on composition. A contour plot is shown in Figure 7 displays iso-lines of electrical conductivity defined by equation 3.

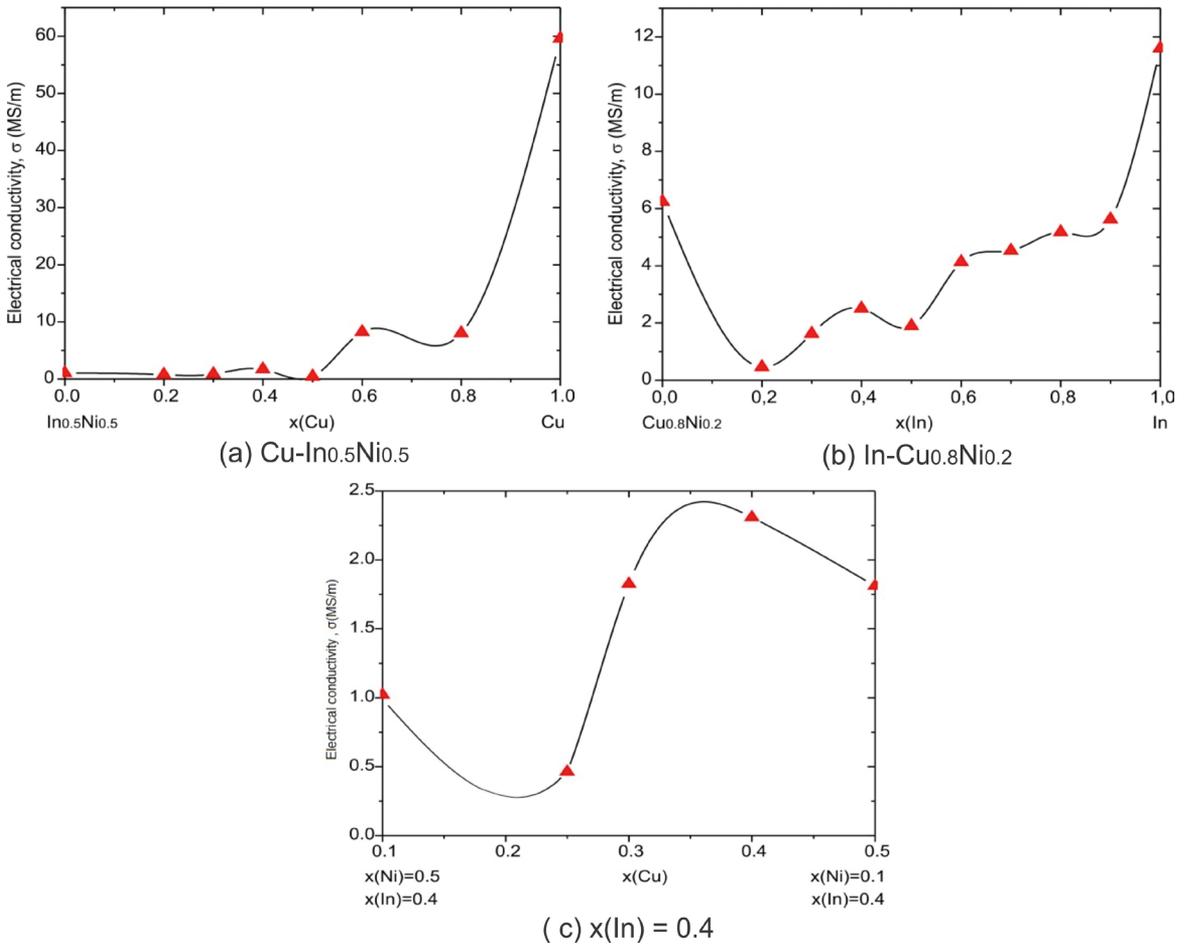


Figure 6. Experimentally determined electrical conductivity of alloys from the three studied vertical sections: a) $\text{Cu-In}_{0.5}\text{Ni}_{0.5}$, b) $\text{In-Cu}_{0.8}\text{Ni}_{0.2}$, c) $x(\text{In})=0.4$

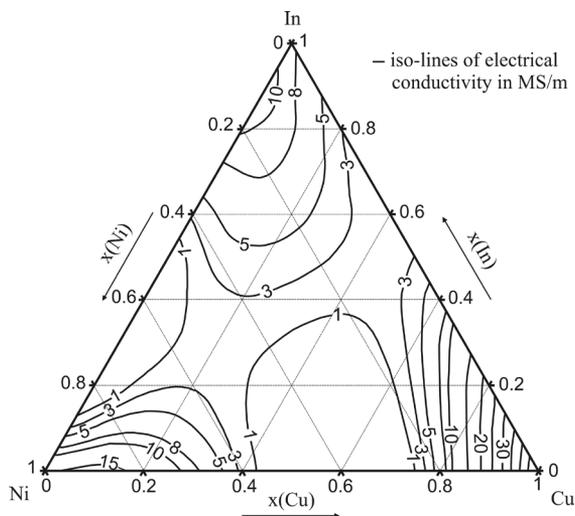


Figure 7. Iso-lines of electrical conductivity of Cu-In-Ni ternary system.

The constructed iso-lines plot (Figure 7) of electrical conductivity for all alloys in ternary Cu-In-Ni clearly shows, as somewhat expected, that all Cu-rich alloys have better electrical conductivity than In or Ni-rich alloys.

4. Conclusion

The isothermal section at 300 °C of a Cu-In-Ni ternary system was investigated using SEM-EDS and XRD analyses. In addition, electrical and mechanical properties of the selected ternary alloys were studied. All experiments were performed on the same alloy samples, which lie along three vertical sections Cu-In_{0.5}Ni_{0.5}, In-Cu_{0.8}Ni_{0.2}, and x(In) = 0.4 of the studied ternary system.

Experimentally investigated microstructures and determined phase compositions of the studied alloy samples equilibrated at 300 °C show close agreement with the results of thermodynamic calculation of isothermal section at 300 °C.

Lattice parameters of the identified phases were determined using XRD analysis and compared with literature data. Determined lattice parameters for all phases are in agreement with literature data and it is determined that lattice parameter of solid solution (Cu) decrease with increasing a solubility of Ni. Since the literature lattice parameters of solid solution (Cu) are $a=b=c=3.625$ Å and for (Ni) are $a=b=c=3.499$ Å it is concludable that lattice parameter of (Cu) solid solution will decrease with increasing the solubility of Ni. Sample 15 has the largest solubility of Ni and lattice parameters for this phase results with the lowest lattice parameters 3.5885(1) Å.

Gathered experimental results of electrical conductivity and Brinell hardness of the selected ternary alloys were used as the basis for calculation of values of electrical conductivity and hardness for an entire compositional range of ternary alloys from the Cu-In-Ni system which are presented in a form of iso-line plots.

The calculated iso-line plot of electrical conductivity shows an increase in values of conductivity towards Cu rich corner while the experimental results show that ternary Cu₈₀In₁₀Ni₁₀ alloy with two-phase microstructure (Cu)+ε'(NiIn) possesses the highest electrical conductivity and hardness of all investigated samples.

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