

## Numerical analysis of collapse modes in optimized design of alveolar Steel-concrete composite beams via genetic algorithms

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### Abstract

The objective of this study is to present the formulation and applications of the optimization problem of steel-concrete composite alveolar beams. In addition to presenting the formulation, a comparative analysis of the predominant collapse modes is performed numerically via the finite element method. The optimization program was developed with the GUI platform available in Matlab 2016. Since this is a discrete problem, a Genetic Algorithm (GA) was used to solve the optimization model, implemented with the Matlab optimization toolbox. Numerical examples using finite elements model are presented to validate the solution and analyze its effectiveness, along with an assessment of the predominant collapse modes for a group of 12 beams. The results show that more efficient designs are obtained when optimization tools are applied.

**Keywords:** alveolar beams; composite beam; genetic algorithm; collapse modes.

### 1. Introduction

Steel beams with uniformly distributed web openings, also referred to as alveolar or castellated beams, have several constructive advantages. These include larger spans, lower overall cost of the structure and lower weight, if compared to beams of the same height with full webs. In fact, the increase in height is one of the main advantages of converting conventional beams into their alveolar counterparts, especially if the beam is structurally joined with a concrete slab, forming a steel-concrete composite floor system. This configuration allows an increase in the resistance of the structural system by taking advantage of certain mechanical characteristics of each material, which in this case are the compressive and tensile strengths of concrete and steel, respectively.

Some recent studies on steel alveolar beams, such as Cimadevila, Gutierrez

and Rodrigues (2000), Silveira (2011), Veríssimo *et al.* (2012) and Badke Neto, Calenzani and Ferreira (2015), show advances in the numerical analysis of the aforementioned structural system.

Cimadevila, Gutierrez and Rodrigues (2000) developed a theoretical approach for determining resistant forces and deformations of steel alveolar beams, establishing consistent equations for the structural design of these elements.

Silveira (2011) performed a numerical analysis to evaluate the behavior of steel alveolar beams with emphasis on modes of collapse induced by plasticization. The author developed numerical models to represent alveolar beam sections normally used in the Brazilian market, focusing on the assessment of collapse modes and ultimate load.

Veríssimo *et al.* (2012) presented a generalized analytical-numerical study

aimed at reevaluating the behavior of alveolar beams with various geometries, including laminated I-profiles produced in Brazil as early as 2002, with the objective of proposing a design procedure.

A recent study published by Sonck and Belis (2015) evaluates the behavior of cellular steel structures subjected to lateral torsional buckling. This methodology however, has yet to be evaluated for use in steel profiles manufactured in Brazil. Alternatively, Lubke, Alves and Azevedo (2017) introduced a formulation for optimization of cellular beams and performed a comparative analysis between different optimization methods. Alves and Lubke (2019) presented the optimization problem and an analysis of the predominant collapse modes for castellated steel-concrete composite beams and their different failure patterns.

The Genetic Algorithm (GA) method was conceived by Holland (1992) based on principles of the theory of evolution proposed by Charles Darwin. Over the last decades, the method has been used to solve optimization problems with discrete variables in various areas of application. Recent noteworthy researches on the use of this method for structural optimization are listed below.

Cho, Min and Lee (2001) used genetic algorithms to conduct an optimization study on the life cycle cost of bridges with orthotropic steel deck systems consisting of steel slabs with ribbed formwork. In this life cycle analysis, building and maintenance costs were considered, with adjustments in structural resistance, deflection and fatigue of the structure. The study concludes that the optimization analyses lead to a more rational, economical and safer design when compared to conventional methods.

Liu, Hammad and Itoh (1997) conducted an optimization study for bridge recovery using GA, forming a model with multiple objective functions and combining the various results with Pareto's approach. The objective was to reduce the cost of bridge recovery and the degree of deterioration. The authors show that the GA presents excellent results even in a model containing mul-

multiple objectives, and with relatively short computational time.

Kripakaran and Gupta (2011) developed, also in 2011, a decision support system based on GA applied to steel frames, with various connection types. The study highlights the advantages of using discrete variables with GA. This feature is explored in the software presented later herein.

Kociecki and Adeli (2015) and Prendes-Gero *et al.* (2018) implemented GA for optimization of different steel structural systems in 2015 and 2018, respectively, and observed gains of around 10% when compared to non-optimized designs. Both studies also highlighted the ability to work with discrete variables when using GA as an important characteristic for obtaining good results. The authors emphasized the high suitability of the method for application in real world scenarios, made possible with the use of discrete variables.

Lima (2011) developed an optimization program with a genetic algorithm for reinforced concrete beams using discrete variables to better represent the reality of structural projects. The authors conclude that the GA provides favorable results, especially in complex problems with discrete variables and constant restrictions. Moreover, results show that in 85% of

the cases, optimized solutions were also optimal solutions.

Souza Jr. (2005) developed a genetic algorithm to assess global mechanical behavior of spatial metallic tubular structures. Steel consumption was analyzed for various geometric configurations in order to minimize the cost of the structure.

Bilbao (2016) conducted an analysis of the optimal design of tuned mass dampers in prefabricated slabs using GA. Results were consistent with available design abacuses.

Ramos and Alves (2018) presented a formulation for the optimization of steel-concrete composite cellular beams, as well as a finite element analysis of predominant collapse modes.

The present article aims to present the formulation and criteria for optimizing the design of steel-concrete composite alveolar beams with the use of genetic algorithms, based on the guidelines provided by Lawson and Hicks (2011), also described in the European design standard SCI Publication P355. A finite element analysis was performed in order to demonstrate the applicability of the formulation, along with a comparative analysis of the governing modes of collapse. A software was developed on Matlab 2016 using the embedded GUI and optimization toolboxes.

## 2. Problem formulation

The optimization model consists of choosing the optimal solution based on an

objective function that will be minimized, in this case, the weight of the beam.

### 2.1 Objective function

The relevant geometric parameters chosen as the problem variables for

a Peiner alveolar beam are presented in Figure 1. The objective function,

called "minimize weight", is shown in Equation (1):

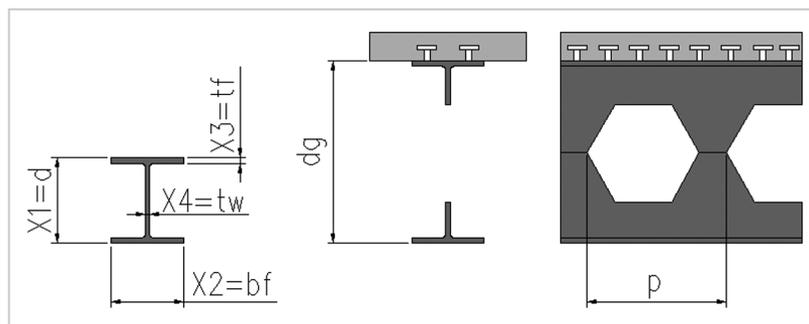


Figure 1 - Geometric parameters for Peiner castellated Beam.

$$\text{Minimize Weigth} = \left\{ \left[ \left( (kx_1 - 2x_3) x_4 \right) + 2x_2x_3 \right] l - \left( \frac{3x_1^2 \sqrt{v}}{2} \right) x_4 n \right\} \rho_a \quad (1)$$

where  $x_1$  is the profile height;  $x_2$  is the flange width;  $x_3$  is the flange thickness;

$x_4$  is the web thickness;  $k$  is the expansion ratio;  $n$  is the number of opening,

$\rho_a$  is the specific weight of steel.

## 2.2 Constraint functions

### 2.2.1 Resistance criteria

The optimization algorithm selects a specific beam as a solution provided that said beam meets the

criteria of ultimate and serviceability limit states prescribed by Lawson and Hicks (2011), adapted to suit Brazilian

standard NBR 8800:2008. Equations to determine design forces are given below.

#### 2.2.1.1 Design vertical shear resistance of perforated steel section ( $V_{pl,Rd}$ )

The design shear resistance of the perforated section is given by Equation (2).

$$V_{pl,Rd} = \frac{0.6A_w f_y}{\gamma_{a1}} \quad (2)$$

where  $A_w$  is the sum of the shear area of the upper and lower tee sections;  $f_y$

is the yield strength of profile steel;  $\gamma_{a1}$  is the resistance factor equal to 1.1

#### 2.2.2.2 Design bending resistance of the opening ( $M_{0,Rd}$ )

The plastic resistant bending moment can assume two values depending

on the position of the neutral axis of the cross-section. If the axis crosses the con-

crete slab, the design bending moment is given by Equation (3).

$$M_{0,Rd} = N_{bT,Rd} \left( h_{ef} + z_T + h_t - \frac{1}{2} z_c \right) \quad (3)$$

Alternatively, if the neutral axis passes through the upper flange,

the bending resistance is given by Equation (4)

$$M_{0,Rd} = N_{bT,Rd} h_{ef} + N_{c,Rd} \left( z_T + h_t - \frac{1}{2} z_c \right) \quad (4)$$

where  $N_{bT,Rd}$  is the resistant axial tensile force of the steel beam;  $h_{ef}$  is the effective beam height, measured from the centers

of gravity of the tees;  $h_t$  is the thickness of concrete slab;  $z_T$  is the distance between the end of the flange and the center of gravity

of upper tee;  $z_c$  is the height of concrete under compression;  $N_{c,Rd}$  is the resistant axial compressive force of the concrete slab.

#### 2.2.2.3 Verification of the vierendeel mechanism

Vierendeel bending resistance is given by the sum of the resistant local bending moments of the four corners of the opening and the local

resistant bending moment due to the interaction of the upper tee with the concrete slab. Vierendeel's resistant bending moment should be greater

than the difference between internal bending moments to the left and right of the opening, in accordance with Equation (5):

$$M_{V,Rd} = 2M_{b,NV,Rd} + 2M_{t,NV,Rd} + M_{vc,Rd} \geq V_{Sd} l_e \quad (5)$$

where  $M_{b,NV,Rd}$  is the reduced bending resistance of the lower tee due to coexisting shear and axial stresses;  $M_{t,NV,Rd}$  is the reduced bending resistance of the upper tee

due to coexisting shear and axial stresses;  $M_{vc,Rd}$  is the local composite bending resistance due to the interaction of the superior tee with the concrete slab;  $V_{Sd}$  is the design

shear force at the end of the opening with the lowest internal moment;  $l_e$  is the effective length of the opening, equal to 45% of its diameter.

#### 2.2.2.4 Design longitudinal shear resistance of the web-post ( $V_{wp,Rd}$ )

The value of the design longitudinal shear force of the web-post is given by Equation (6).

$$V_{wp,Rd} = \frac{0.6s_0 t_w f_y}{\gamma_{a1}} \quad (6)$$

where  $s_0$  is the width of the web-post;  $t_w$  is the thickness of the web.

#### 2.2.2.5 Design bending resistance of the web-post ( $M_{wp,Rd}$ )

The resistant bending moment of the web-post can be obtained by Equation (7).

$$M_{wp,Rd} = \frac{s_0^2 t_w f_y}{6\gamma_{a1}} \quad (7)$$

### 2.2.2.6 Resistance to buckling of the web-post ( $N_{wp,Rd}$ )

The buckling resistance of the web-post relies on the reduction coefficient established in the compres-

sive strength curve of ABNT NBR 8800:2008, which depends on the longitudinal slenderness of the ele-

ment. According to Lawson and Hicks (2011), this coefficient is given by Equation (8).

$$\lambda_0 = \frac{\sqrt{12} I_{ww} t}{\lambda_1} \quad (8)$$

### 2.2.2.7 Verification of displacements on the beam

The maximum deflection resulting from a uniformly distributed load on

the beam is determined according to Equation (9):

$$f = \frac{5ql^4}{348EI} \quad (9)$$

where  $q$  is the magnitude of uniformly distributed loading;  $l$  is the length of the

beam;  $I$  is the equivalent moment of inertia of the perforated composite section.

## 2.3 Resistance constraint equations

As presented in the previous items, this set of equations represent

the constraints that the optimized solution must meet. These functions can be

written in standard form according to Equations (10) through (19).

$$1 - \frac{P_{rd}}{P_{Sd}} \leq 0 \quad (10)$$

$$1 - \frac{V_{rd}}{V_{Sd}} \leq 0 \quad (11)$$

$$1 - \frac{M_{0,rd}}{M_{Sd}} \leq 0 \quad (12)$$

$$1 - \frac{M_{Vrd}}{V_{Sd} l_e} \leq 0 \quad (13)$$

$$1 - \frac{V_{wpSd}}{V_{wpRd}} \leq 0 \quad (14)$$

$$1 - \frac{M_{wp,Rd}}{M_{wp,Sd}} \leq 0 \quad (15)$$

$$1 - \frac{N_{wp,Rd}}{N_{wp,Sd}} \leq 0 \quad (16)$$

$$1 - \frac{V_{Rd1}}{V_{Sd}} \leq 0 \quad (17)$$

$$1 - \frac{V_{Rd2}}{V_{Sd}} \leq 0 \quad (18)$$

$$1 - \frac{f_{LIM}}{f_T} \leq 0 \quad (19)$$

The variables included in Equations (10) to (19) are described in the

### 3. The Computational program

The program was developed in Matlab with the use of the GUI tool. Optimal design is obtained using Genetic Algorithms considering input parameters pre-

#### 3.1 Applicability of the formulation

The demonstration of the applicability of the model proposed herein is performed by solving two examples of alveolar composite beams found in

##### 3.1.1 Example A1

The first example is presented by Brinkhus (2015). The author developed an excel spreadsheet to verify alveolar mixed beams of steel and concrete. For this example she used a profile W 150x18 kg/m, manufactured by Gerdau Açominas (table of profile Gerdau); this profile

previous sections. The optimal solution will be chosen from a steel profile

viously defined by the user. The program displays a summary of software checks, resistant and internal forces, as well as optimal design. The genetic algorithm chosen

literature. The first and second examples consist of a comparative analysis between the solution proposed here and castellated composite beams presented by Brinkhus

was expanded to become a castellated beam. The purpose of this example is, through the proposed formulation, to choose a profile, from the Gerdau profile table, that supports the same loads and geometric conditions (length of the span, effective width of concrete flange) used by

catalogue, provided by ArcelorMittal (2016).

is an optimization model for discrete variables, suitable for the proposed problem, since the optimal solution is extracted from a table of commercially available profiles.

(2015). The objective is to demonstrate that the proposed formulation is able to improve results regarding the weight of the profile.

Brinkhus and, after this choice compare the results. Input data for the first example presented by Brinkhus (2015) is shown in Table 1. Results are compared with those obtained by Brinkhus (2015) in Table 2 and Table 3, after the application of the optimization formulation.

Table 1 - Input data Brinkus(2015).

Item	Parameters	Values
Beam	Length of the span	4.2 m
	Profile	W 150 x 18
Materials	Effective width of concrete flange	1 m
	Yield strength - steel	345 MPa
	Compressive strength - concrete fck	30 MPa
Actions	Beam weight	18 kg/m
	Live load	7 kN/m

Table 2 - Comparison of results - general data.

Item	Brinkhus (2015)	Authors
Alveolus height	15.3 cm	15.3 cm
Concrete thickness	20.0 cm	20.0 cm
Interaction type	full	full

Table 3 - Comparison of results - forces.

	$M_{sd}$ (kNm)	$V_{sd}$ (kN)	$V_{Rd}$ (kN)	$N_{wpRd}$ (kN)	$M_{0Rd}$ (kNm)
Brinkhus (2015)	29.33	22.57	86.82	95.5	63.8
Authors	16.10	15.3	63.4	71.6	59.3

The optimization program indicated the profile W 150x13 kg/m as the optimal solution, also from Gerdau Açominas. The resistant forces obtained by Brinkhus (2015) are greater than those found by the optimization program, since the cross-sectional area of the profile chosen by

the author is larger than the one chosen by the program. All the resistant forces obtained with the program are greater than the internal forces induced by the loading. As such, the profile meets all the structural safety criteria and is 28% lighter than the optimal solution indicated

by Brinkhus (2015). The constraint that governed the optimization process was the web amount buckling ( $N_{wpRd}$ ). The Table 8 shows other results for the beam chosen in the optimization process, with respect to resistant forces, as well as the relationship between these and acting forces.

Table 4 – Acting forces X Resistant forces – W 150 x 13 kg/m

Authors	$M_{V_{ISd}}$ (kNm)	$M_{V_{IRd}}$ (kNm)	$M_{V_{ISd}}/M_{V_{IRd}}$	$V_{wpSd}$ (kN)	$V_{wpRd}$ (kN)	$V_{wpSd}/V_{wpRd}$
	0.8	5.8	0.14	15.3	32.0	0.48
	$\delta_{Sd}$ (mm)	$\delta_{Rd}$ (mm)	$\delta_{Sd}/\delta_{Rd}$	$N_{wpSd}$ (kN)	$N_{wpRd}$ (kN)	$N_{wpSd}/N_{wpRd}$
	6.2	12.0	0.52	43.5	71.6	0.61

### 3.1.2 Example A2

The second example follows the same pattern as the first example. The input data taken from Brinkhus (2015) is shown in

Table 4. In example A2 of Brinkhus (2015), a W 250x22.3 kg/m profile of Gerdau Açominas was analyzed, subjected to the

loads shown in Table 5. The results are compared with those obtained with the program, in Table 6 e Table 7.

Table 5 - Input data.

Item	Parameters	Values
Beam	Length of the span	10 m
	Profile	W 250 x 22.3
	Effective width of concrete flange	1 m
Materials	Yield strength - steel	345 MPa
	Compressive strength – concrete $f_{ck}$	30 MPa
Actions	Beam weight	22.3 kg/m
	Live load	3.6 kN/m

Table 6 – Comparison of results – general data.

Item	Brinkhus (2015)	Authors
Alveolus height	25.4 cm	25.4 cm
Concrete thickness	20.0 cm	20.0 cm
Interaction type	full	full

Table 7 - Comparison of results.

	$M_{Sd}$ (kNm)	$V_{Sd}$ (kN)	$V_{Rd}$ (kN)	$N_{wpRd}$ (kN)	$M_{0Rd}$ (kNm)
Brinkhus (2015)	74.4	29.75	115.2	120.7	119.5
Authors	49,7	19.9	153.9	127.8	152.8

The optimization program indicated the profile W 310x21 kg/m as the optimal solution, also from Gerdau Açominas. The values of shear resistance  $V_{Rd}$ , and bending resistance in the opening region  $M_{0Rd}$ , returned by the program, are greater than those of the profile chosen by Brinkhus

(2015). Alternatively, the axial resistance of the web-post,  $N_{wpRd}$ , is smaller. The profile chosen by the optimization program features a larger height than the profile of example A2 (49 mm larger), however, the optimized profile is 5.83 % lighter than the one indicated in the ref-

erence. The constraint that governed the optimization process was the web amount buckling ( $N_{wpRd}$ ). The Table 8 shows others results for the beam chosen in the optimization process, with respect to resistant forces, as well as the relationship between these and acting forces.

Table 8 – Acting forces X Resistant forces – W 310 x 21 kg/m.

Authors	$M_{V_{ISd}}$ (kNm)	$M_{V_{IRd}}$ (kNm)	$M_{V_{ISd}}/M_{V_{IRd}}$	$V_{wpSd}$ (kN)	$V_{wpRd}$ (kN)	$V_{wpSd}/V_{wpRd}$
	2.2	26.4	0.08	19.9	81.8	0.24
	$\delta_{Sd}$ (mm)	$\delta_{Rd}$ (mm)	$\delta_{Sd}/\delta_{Rd}$	$N_{wpSd}$ (kN)	$N_{wpRd}$ (kN)	$N_{wpSd}/N_{wpRd}$
	18.6	28.6	0.65	91.1	127.8	0.71

### 3.1.3 Example 3 - Evaluation of collapse modes and numerical analysis

#### 3.1.3.1 Evaluation of collapse modes

The collapse modes of the alveolar beams were used as restrictions for the implementation of the optimization routine. In optimal beam design, it is

common for some constraints to govern the entire calculation process. In order to evaluate the predominant collapse modes in the optimization process,

based on the proposed formulation, 13 beams were optimized for the loads show in Table 9. Results are presented in Figure 2.

Table 9 - Input data.

Floor system				Roof system					
	$L_b$ (m)	$Q_{cp}$ (kN/m)	$Q_{sc}$ (kN/m)	Optimum Profile		$L_b$ (m)	$Q_{cp}$ (kN/m)	$Q_{sc}$ (kN/m)	Optimum Profile
Beam 1	5.0	1.0	1.50	W150x13	Beam 7	11	1.0	1.50	W310x21
Beam 2	6.0	2.0	2.50	W250x17.9	Beam 9	12	2.0	2.50	W410x38.8
Beam 3	7.0	3.0	3.50	W250x17.9	Beam 10	13	3.0	3.50	W460x52
Beam 4	8.0	4.0	4.50	W310x28.3	Beam 11	14	4.0	4.50	W530x66
Beam 5	9.0	5.0	5.50	W410x38.8	Beam 12	15	5.0	5.50	W530x85
Beam 6	10.0	6.0	6.50	W410x46.1	Beam 13	16	6.0	6.50	W610x101

a) To obtain the graphs in Figure 2, the two most predominant collapse modes were analyzed for each beam and in each optimization process. The following conclusions are drawn from the graphs: Web-post buckling was the most common collapse mode for ultimate limit state criteria. Both cellular and castellated beams presented the occurrence of this type of failure.

b) Beams with lengths of 8m, 9m and 10m presented flexural failure of the web-post along with buckling of this element. This is due to these modes of collapse being associated with shear forces in adjacent openings.

c) Beams of 6m and 7m presented flexural failure of the open region and incidence of the Vierendeel mechanism.

Both modes of collapses are associated with the presence of bending moment in the opening, as a result of the Vierendeel mechanism.

d) The 16 m beam show the occurrence of the two modes associated with buckling of the web-post: the first due to the normal compressive force,  $N_{wpSd}$ , and the second due to longitudinal shear force  $V_{wpSd}$ .

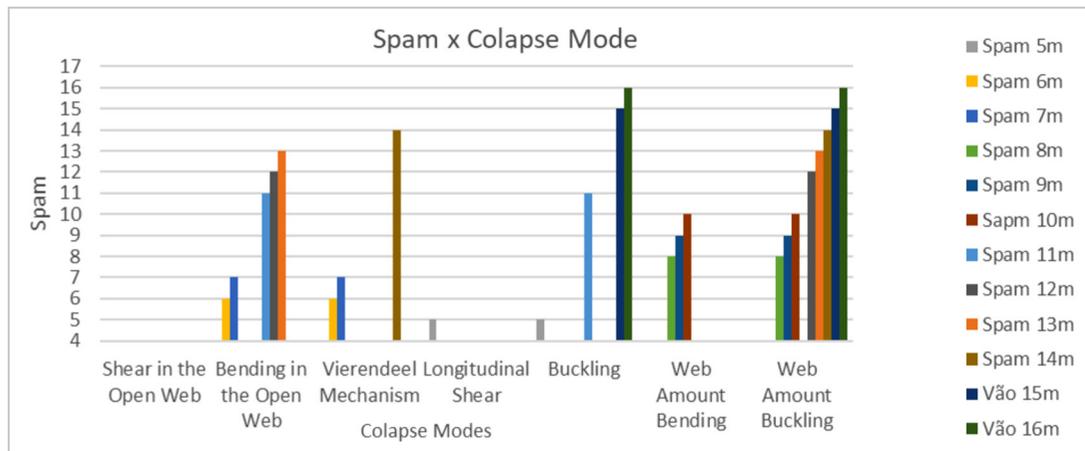


Figure 2 –Analysis of collapse modes.

#### 3.1.3.2 Numerical analysis

In order to further verify the results obtained, a finite element analysis was

conducted. The maximum stress observed in the finite element analysis is compared

with the stress obtained analytically with Equation (20).

$$\sigma = \frac{M_s}{W_x} \tag{20}$$

where  $M_s$  is internal moment induced by loading;  $W_x$  is bending modulus of the composite section.

The numerical model was developed and analyzed with Solidworks Simulation software (2015). A mesh with tetrahedral

solid elements with 25 mm sides and tolerance of 1.25 mm was adopted for the steel beam and the concrete slab. The elements feature 4 nodes, each with 3 degrees of freedom representing translations in the three orthogonal directions. Figure

3 shows the finite element model of the structural system. Results are exhibited in Figure 4.

Table 10 presents a comparative analysis between results from the finite element model and the optimization program.

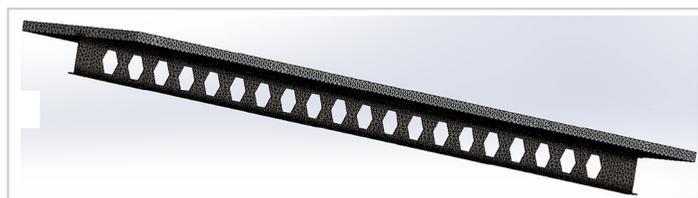


Figure 3 - Finite element model - Alveolar beam.

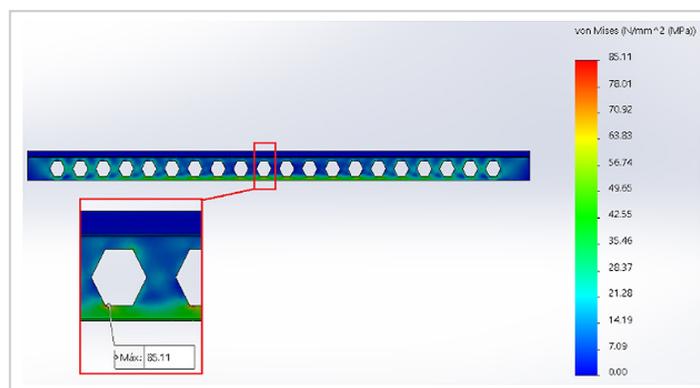


Figure 4 - Maximum stress - alveolar beam.

Table 10 - Stress analysis results.

	Finite Element Analysis (MPa)	Program (MPa)	% Diff.		Finite Element Analysis (MPa)	Program (MPa)	% Diff.
Beam 1	85.11	86.2	1.26	Beam 7	167.5	173.7	3.57
Beam 2	137.2	121.8	11.22	Beam 9	140.0	166.6	15.97
Beam 3	216.2	232.5	7.01	Beam 10	173.5	201.7	13.98
Beam 4	218.8	240.1	8.87	Beam 11	192.2	217.2	11.51
Beam 5	246.1	223.8	9.06	Beam 12	205.7	229.3	10.29
Beam 6	255.7	273.3	6.44	Beam 13	241.7	251.1	3.74

Numerical results corroborate one of the predominant collapse modes, the flexural failure of the composite section.

Overall values were close, with the largest difference being 15.97%. Maximum stresses obtained from numerical and

analytical assessments fall below the yield strength of 345 MPa, adopted as the criterion for material failure.

#### 4. Conclusions

The objective of this study was to present the formulae for design optimization of steel-concrete composite alveolar beams and their applications, as well as the results of a numerical analysis, performed to demonstrate one of the predominant collapse modes in the optimization problem.

The use of genetic algorithms resulted in improvements regarding structural weight when compared to the reference solution. Weight reduction of the optimal profile is observed in all scenarios analyzed, thus demonstrating the effectiveness of the method adopted herein.

An analysis of the collapse modes indicated that lateral buckling of the web-post is the predominant failure pattern. Furthermore, similar results are noticed between the finite element analysis and the analytical approach conducted with the optimization program developed for this research.

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