

## Classification of Polymers Insulators Hydrophobicity based on Digital Image Processing

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Although the hydrophobicity is usually an arduous parameter to be determined in the field, it has been pointed out as a good option to monitor aging of polymeric outdoor insulators. Concerning this purpose, digital image processing of photos taken from wet insulators has been the main technique nowadays. However, important challenges on this technique still remain to be overcome, such as; images from non-controlled illumination conditions can interfere on analyses and no existence of standard surfaces with different levels of hydrophobicity. In this paper, the photo image samples were digitally filtered to reduce the illumination influence, and hydrophobic surface samples were prepared from wetting silicon surfaces with solution of water-alcohol. Furthermore, previous studies trying to quantify and relate these properties in a mathematical function were found, that could be used in the field by the electrical companies. Based on such considerations, high quality images of countless hydrophobic surfaces were obtained and three different image processing methodologies, the fractal dimension and two Haralick textures descriptors, entropy and homogeneity, associated with several digital filters, were compared. The entropy parameter Haralick's descriptors filtered with the White Top-Hat filter presented the best result to classify the hydrophobicity.

**Keywords:** *image processing, insulators, image texture analysis*

### 1. Introduction

Continuous improvements on polymeric materials have contributed to replace the traditional glass and ceramic high voltage outdoor insulators for polymeric insulators in different situations on electrical power transmission and distribution systems<sup>1</sup>. In fact, due to the lightweight, lower susceptibility to breakage and excellent hydrophobic surface of polymeric insulators, they have been used with success, on high pollution environments and on transmission system with compact towers.

The hydrophobicity is a physical-chemical property used in various areas of knowledge as chemistry, medicine and pharmacology. It is an important indicator applied to the transport and permeability of membranes, interactions with biological receptors and enzymes, toxicity and biological potential<sup>2,3</sup>. The hydrophobic effect is not an attractive force between nonpolar molecules nor a repulsive force between such molecules and water. Rather, it is an entropic effect originating from the disruption of highly dynamic hydrogen bonds between molecules of liquid water by the nonpolar solute<sup>4</sup>.

The hydrophobic behavior of a material is directly related to the surface energy that acts as a driving force between the phases. The surface energy is defined as the free energy increased in a system on creating a unit area of new surface at constant temperature, pressure and composition. The force required to extend a liquid surface per unit

length is the surface tension and is numerically equal to the surface energy. In a system with a number of phases, the equilibrium distribution is determined by the condition that interface energy is a minimum. This requirement fixes the contact angle for a liquid-solid-vapor system with suitable limitations<sup>5</sup>.

The hydrophobicity surface of polymeric insulators is widely desired because it prevents the formation of a water path for electric current, preventing flashover and discharges on the insulation, causing electric breakdown<sup>6</sup>. However, some outdoor conditions such as, ultraviolet radiations, snow or salt can accelerate their aging process as well as reduce the hydrophobicity of polymers<sup>7-9</sup>. Fact that requires improvements in maintenance processes of electrical systems that use these insulators. In this context, the monitoring of the hydrophobicity of insulator surfaces directly in the field has become an important issue in power electric utilities.

Some methodologies to determine the surface hydrophobicity of electrical insulators come from STRI Guide<sup>10</sup> or from IEC TS 62073<sup>11</sup>. The first technique basically consists of wetting the surface of the insulator with water and then taking pictures. By comparing them with standard photos taken on laboratory conditions it is possible to identify modifications on the surface hydrophobicity. The second method is based on the measurement of the contact angle of droplets on the surface; which is more difficult to

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be performed in the field since the surface must be placed horizontally. Therefore the STRI method is generally used for monitoring outdoor insulators, although it has a rough hydrophobicity classification (HC), since it compares subjective images, taken on poor illumination conditions, with seven pattern images, which are defined from HC01 to HC07 (from fully hydrophobic to fully hydrophilic texture)<sup>10</sup>.

In order to improve the STRI method to monitor outdoor insulators some digital images processing techniques has been proposed by many researches, such as, circular factor<sup>12</sup>, goniometric measurement using Hough transformation<sup>13</sup>, segmentation<sup>14</sup>, scaled entropy and histogram analyses<sup>15,16</sup>, surface energy<sup>17</sup>, and online hydrophobicity measurement methodology<sup>18,19</sup>, which use the spray method and inspection of the surface insulators in the field by photos and processing image methodologies.

The use of digital image processing has become a technique to identify patterns and shapes in a fast and accurate way<sup>20</sup>, being suitable to this study. In this paper, three digital image processing methodologies, fractal dimension and two Haralick's textures descriptors, entropy and homogeneity, which have not yet been applied to the investigation of hydrophobicity are combined with digital filters to reduce the influence of illumination conditions. A comparison between these three methods allowed us to obtain a better technique to determine the hydrophobicity of polymeric surfaces. The processing methods were chosen due to their abilities to identify similar textures<sup>21,22</sup> and the photos were taken from samples obtained from the experimental procedure to prepare hydrophobic surfaces, described in<sup>21</sup>.

## 2. Experimental Procedure

Experimental procedure consists of preparing physical polymeric samples with different hydrophobic levels; taking photos of them on different illumination conditions; classifying them according to the STRI Guide, so they can correspond to the HC level, and also measure the contact angle of droplets on the surface as recommended in STRI Guide.

### 2.1. Samples preparation

Ten specimens of silicon rubber with  $10 \times 10 \text{ cm}^2$  and 5 mm thickness were sprayed with a solution of water and isopropyl alcohol (WIA) at different concentrations (from 0 to 100%)<sup>19,21</sup>. These solutions were identified as percentage of alcohol (%WIA). The parameters of the process to obtain the silicon rubber in industry are very well defined, and it is known that this material recovers the hydrophobicity behavior after some shelf time<sup>16</sup>. In this way, images from each WIA solution were taken from each specimen to prevent surface modification and to guarantee the reliability of the measurements. This solution was adopted due to the excellent results from previous works<sup>19,21</sup>, which showed high chemical stability of the materials employed and reproducibility of the results due to the low dispersion.

As discussed in previous work<sup>21</sup>, the alcohol reduces the surface tension of the water without any modification on the

surface of silicon rubber. In this way, images with different contact angles, due to the different %WIA solutions, and textures from the insulator surfaces could be produced. The modification between contact angle and %WIA is shown in Figure 1.

### 2.2. Sample image preparation

Photo images, named (OR), were taken under natural illumination condition from each sample wetted with different percentages of WIA, with a 7.2 megapixel Sony W120 digital camera. This procedure provided ten VGA images grayscale, which were classified according to the STRI guide. Four of these images are presented in Figure 2. Images from the droplets were also taken in order to measure the contact angle with ImageJ software<sup>23</sup>. The computational procedure was performed in MatLab<sup>®</sup> v7.12 and Image Processing Toolbox v7.2 for Mac. The hardware used was an iMac with Intel i3 3.2 GHz and 12 Gb of RAM.

In order to avoid the influence of natural conditions of illumination, histogram equalization (EQU)<sup>24</sup>, which promotes the balance in the grayscale distribution and/or the White Top-Hat filter (WTH)<sup>24</sup>, which gives an enhancement of the image edges were used. Combinations of both these processes were also implemented. These light adjustments were used according to previous studies<sup>25</sup>, which show lower deviation and higher correlation in the results observed for these analyses.

## 3. Theoretical Considerations of Image Processing Methods

There are many methods to interpret and identify patterns and texture in digital image<sup>22,24</sup>. Most of them are employed regarding easiness of implementation, short time processing and reliability. For hydrophobicity classification most of the classical methods can be applied to distinguish its textures. However, for field application, as this work proposes, short processing time and on-line evaluation are desired characteristics. Considering this, the fractal dimension method, and the entropy and the homogeneity Haralick's descriptors, were selected for a performance comparison.

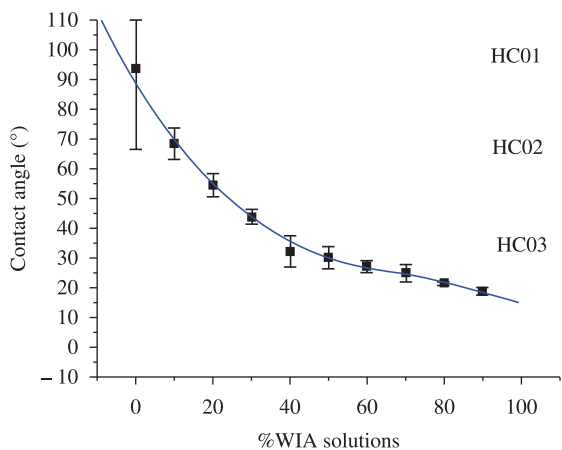
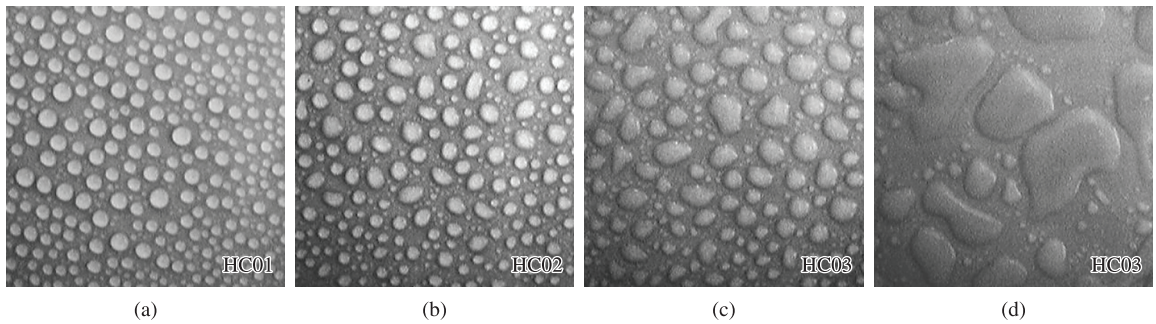


Figure 1. %WIA solution vs contact angle.



**Figure 2.** Original images from surfaces sprayed with water-alcohol solutions of a) 0% WIA and HC01; b) 20% WIA, HC02; c) 40% WIA, HC 03; and d) 60% WIA with HC03.

### 3.1. Fractal dimension

Literature provides some ways to calculate de Fractal Dimension of an object or image, and most of them are based on Hausdorff Dimension<sup>26</sup>. For a compact and uniform object in an image, it results in an integer value equal to the topological dimension, but to a fractal, it gives a fractionary number. In this way, an irregular shape gives a higher Fractal Dimension value, which is helpful to compare two fractals shapes. The Box-Counting is one of the best known and employed methods to estimate the Fractal Dimension, due to its simplicity and easiness of implementation. It consists of overlapping square grids and counting the number of squares necessary to cover the shape<sup>27</sup>.

The fractal dimension calculations have been performed by the box-count method in the grayscale images<sup>28</sup>, with the box-size ranging from 3 to 11. The fractal dimension based on the box-count method can be defined by:

$$D_n = \frac{\log(N_n)}{\log 2^n} \quad (1)$$

where the fractal dimension ( $df$ ) is the linear fitting of  $D_n$  for many  $n$  values present in an image divided  $n$  times and  $N_n$  is the number of boxes crossing the image.

The  $N_n$  calculation can be obtained based on grayscale values from pixels grid ( $i,j$ ) as follows:

$$N_n = \sum n_n(i,j) \quad (2)$$

The  $n_n$  values are obtained from the Equation 3, where:

$$n_n(i,j) = \text{int} \left( \frac{\text{Gray}_{\max}(i,j) - \text{Gray}_{\min}(i,j)}{S} \right) + 1 \quad (3)$$

where  $\text{Gray}_{\max}(i,j)$  and  $\text{Gray}_{\min}(i,j)$  are the maximum and minimum grayscale image values in the grid ( $i,j$ ) and  $S'$  is the size of the box.

In this way,  $N_n$  is taken for different values of  $n$ , that is, from different sizes of grids. This counting method leads to a better approximation of the boxes that intercept the surface of the grayscale levels in the image. The  $df$  is obtained from the average value of  $D_n$ , or the angular coefficient of the linear fit from  $n$  vs  $D_n$  dilog plot.

### 3.2. Entropy

According to the classical definition of Entropy<sup>29,30</sup> it is defined as the probability of occurrence of an event in a set. Equation 4 presents how this value is obtained.

$$S = - \sum_{\lambda \in \Omega} p(\lambda) \times \log[p(\lambda)] \quad (4)$$

In digital image processing,  $\lambda$  is the set represented by the Gray Level Co-Occurrence Matrix (GLCM), as proposed by Haralick<sup>22</sup>, and  $p(\lambda)$  is the probability of occurrence of this event in the set.

The entropy value is one of the texture descriptors, which can characterize an image, it can be used as a form of discrimination of texture images<sup>31</sup>.

Regarding image processing, Haralick described the entropy as the smoothness of the texture of the image, which can be calculated as

$$S = - \sum_i \sum_j p(i,j) \times \log[p(i,j)] \quad (5)$$

where  $p(i,j)$  is the GLCM obtained by two vectors defined as (1,0) and (0,1), after normalization described by Gonzalez<sup>24</sup>. Thus, the Entropy value was obtained from the average Entropy values from those GLCM.

### 3.3. Homogeneity

The Homogeneity<sup>22</sup> shows the distribution of the elements of a GLCM with its diagonal. Its value is between zero and one, and its one when the diagonal of the GLCM has the same values. The homogeneity is calculated as follows:

$$H = \sum_i \sum_j \frac{p(i,j)}{1 + |i - j|} \quad (6)$$

As the same procedure for Entropy, the Homogeneity was performed from the average values calculated from two GLCM with vectors (1,0) and (0,1).

## 4. Results and Discussions

### 4.1. Images classification and illumination adjustments

Initially the images presented in Figure 2 were compared with the STRI classification through the measurements

of the contact angles as a function of the %WIA solution (Figure 1). According to the STRI Guide, for an HC level, the value must be defined using not only the contact angle, but also the amount of the wetted surface and the shape of the drops, which cannot be observed in the contact angle measurements. Classifying the hydrophobicity based on contact angle of %WIA solutions could make the analyses incoherent, as observed in Figure 1, HC values higher than 4 were not present in those measurements, but they can be noted by superficial analyses<sup>21</sup>. Because of that, the contact angle was not considered in these analyses.

Standard surfaces were naturally illuminated and the pictures for each percentage of WIA solution were taken. Images received digital illumination adjustments as presented in Figure 3, where the original image followed by the illumination adjustments from EQU, WTH, EQU+WTH and EQU+WTH+EQU can be seen.

Variations on the opening size mask of the WTH filter were performed in the range from  $[3 \times 3]$  to  $[121 \times 121]$  pixels, to define the best mask size (B). And it was found that the convergence was reached when B was equal to  $[41 \times 41]$ , as it is presented in Figure 3c), which also shows that the variation in the illumination was significantly reduced.

#### 4.2. Fractal dimension

The fractal dimension of these images was calculated based on Equation 1 and the results are plotted in Figure 4. The plot reveals some dispersion in the results, in general

around 3% and that all the curves tend to converge. As the texture of images became less complex with the addition of the alcohol in WIA solutions, the complexity of the shapes decreased, reducing the fractal dimension values.

As the main goal of this study is to predict the behavior of the hydrophobicity in polymeric surfaces, an injective function was sought in order to provide a reliable mathematical identity.

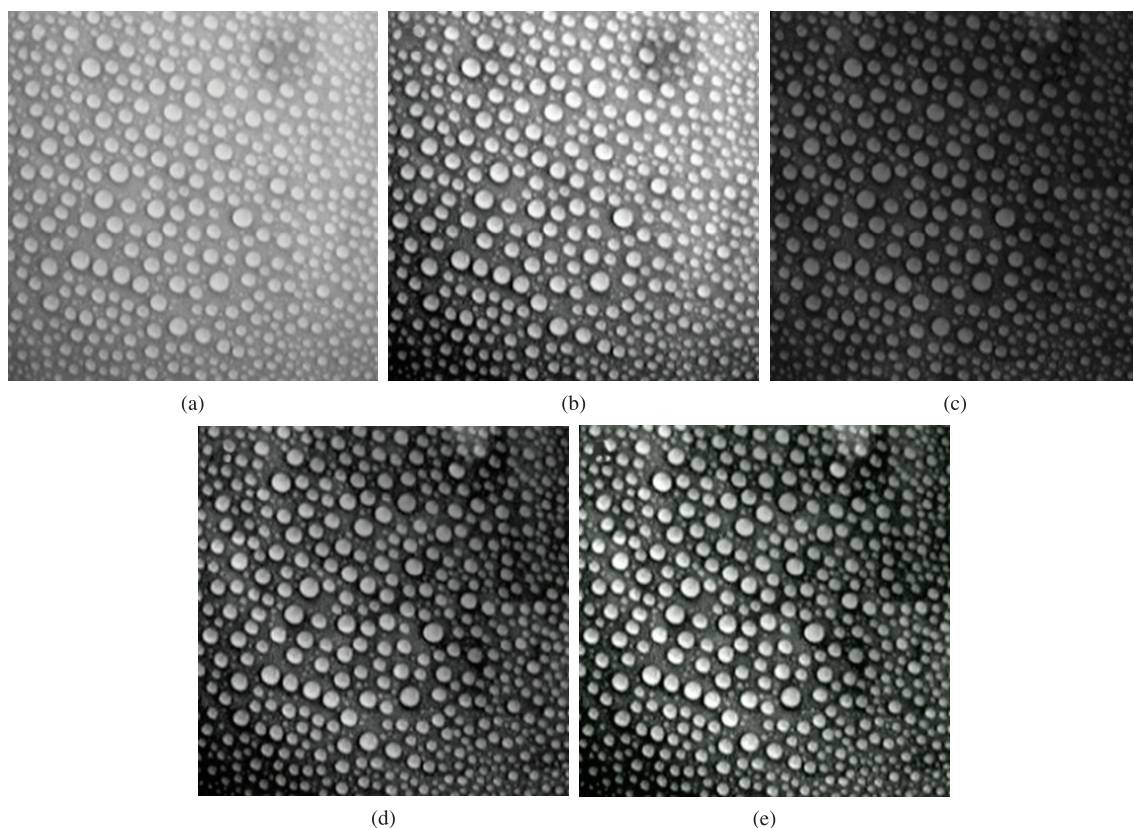
Table 1 shows the values of setting parameters for the mathematical fit of  $df$  values obtained for the images WIA. It is possible to observe that the curve for WTH images presents the best fit of all, which can be confirmed by the highest correlation coefficient shown in Table 1, or:

$$\%WIA = 97.623 \times \exp\left(\frac{2.439 - df}{0.078}\right) \quad (7)$$

Equation 7 relates the image texture from the pattern images based on percentage of %WIA images and its fractal dimension value. In other words, this method provides a direct quantification of the hydrophobicity due to its texture characteristics. Its main advantage is the objective classification promoted by this method, avoiding the subjective analysis of the operator. However, one disadvantage of this method was the long time consumed during calculations, about 1 minute.

#### 4.3. Entropy

Figure 5 shows the behavior between the Entropy values and the %WIA images. High linearity and low



**Figure 3.** Images with different illumination adjustments: a) OR; b) EQU; c) WTH; d) EQU+WTH; and e) EQU+WTH+EQU.

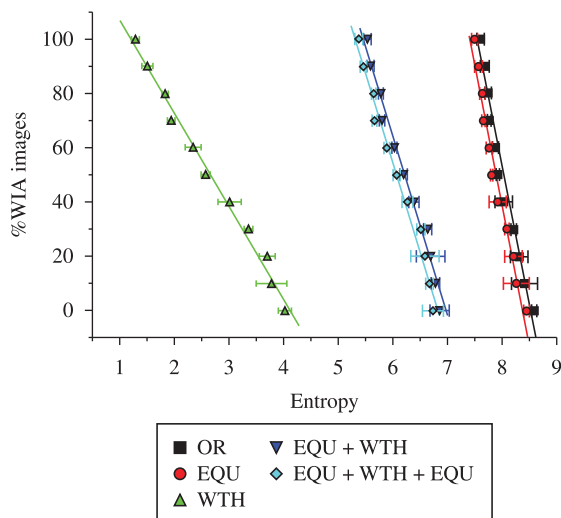
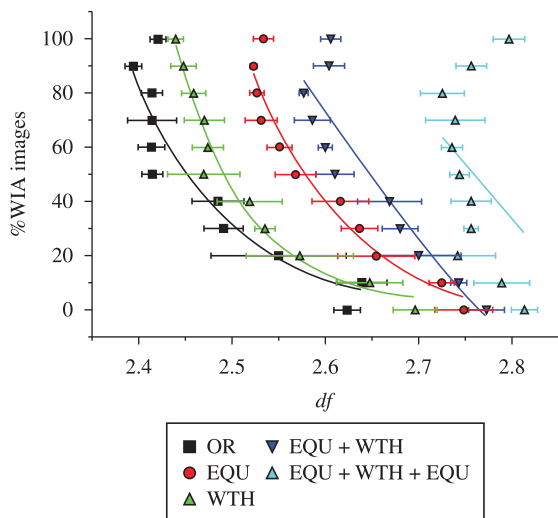


Figure 4. df values of various %WIA images.

Figure 5. Entropy values of various %WIA images.

Table 1. First order exponential parameters to %WIA images and fractal dimension values.

| Image       | $x_0$             | $A_1$               | $t_1$             | Correlation |
|-------------|-------------------|---------------------|-------------------|-------------|
| OR          | $2.394 \pm 0.001$ | $88.485 \pm 8.737$  | $0.101 \pm 0.027$ | 0.788       |
| EQU         | $2.534 \pm 0.001$ | $89.205 \pm 37.444$ | $0.080 \pm 0.068$ | 0.914       |
| WTH         | $2.439 \pm 0.001$ | $97.623 \pm 4.324$  | $0.078 \pm 0.008$ | 0.958       |
| EQU+WTH     | $2.577 \pm 0.001$ | $89.867 \pm 9.983$  | $0.097 \pm 0.026$ | 0.778       |
| EQU+WTH+EQU | $2.725 \pm 0.001$ | $65.857 \pm 19.247$ | $0.113 \pm 0.117$ | -0.104      |

Table 2. Angular, linear and correlation coefficient values to %WIA images and entropy values.

| Image       | Angular              | Linear               | Correlation |
|-------------|----------------------|----------------------|-------------|
| OR          | $-99.548 \pm 6.353$  | $850.515 \pm 51.124$ | -0.982      |
| EQU         | $-104.838 \pm 6.482$ | $880.776 \pm 51.403$ | -0.983      |
| WTH         | $-34.151 \pm 1.119$  | $141.908 \pm 3.182$  | -0.995      |
| EQU+WTH     | $-66.832 \pm 3.100$  | $466.619 \pm 19.378$ | -0.990      |
| EQU+WTH+EQU | $-65.254 \pm 3.080$  | $448.575 \pm 18.873$ | -0.990      |

dispersion between the values for all types of processed images can be seen, when compared to the values presented by fractal dimension analysis. These results indicate that the use of this method is more reliable to this kind of texture analysis.

The curves were linearly fitted, according to Table 2. And in this case, the WTH curve, expressed for (Equation 8), presented the highest angular and correlation coefficient.

$$\%WIA = (141.9 \pm 3.2) + (-34.2 \pm 1.1) \times S \tag{8}$$

In this case, the processing time was shorter than that spent on the Fractal Dimension calculation, about 2 seconds

#### 4.4. Homogeneity

The results from the homogeneity method as a function of the WIA images are presented in Figure 6. Again a linear

behavior of the curves can be observed, suggesting a good agreement with the results presented in Table 3.

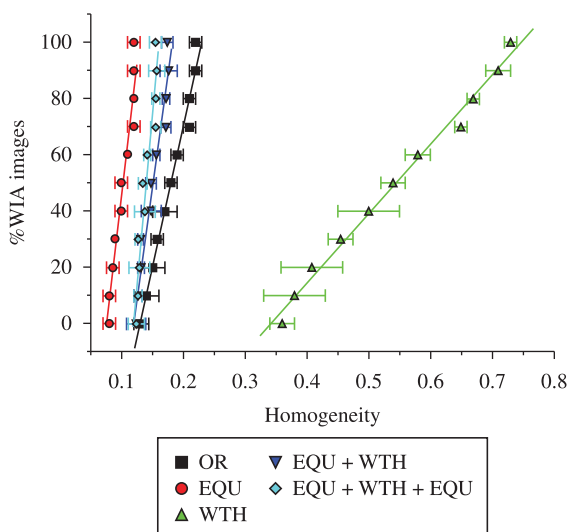
The highest correlation coefficient for these images was obtained for the WTH images, as observed through fractal dimension and entropy analyses. In this case, the relationship obtained was the following:

$$\%WIA = (-83.9 \pm 4.4) + (246.2 \pm 7.8) \times H \tag{9}$$

In comparison to the fractal dimension method, the Haralick texture descriptors presented not only short calculation time (about 2 seconds), but it also resulted in much lower dispersion values and it was mathematically simple to adjust. Comparing the studied methods, the Haralick texture descriptors indicates that the homogeneity or entropy is the best option to make an objective analysis of the classification of hydrophobicity in polymer insulators, since a better correlation was obtained with this method.

**Table 3.** Angular, linear and correlation coefficient values to %WIA images and homogeneity values.

| Image       | Angular            | Linear            | Correlation |
|-------------|--------------------|-------------------|-------------|
| OR          | 1004.548 ± 46.671  | -130.597 ± 8.516  | 0.990       |
| EQU         | 1942.853 ± 162.517 | -148.840 ± 16.829 | 0.970       |
| WTH         | 246.236 ± 7.795    | -83.918 ± 4.355   | 0.996       |
| EQU+WTH     | 1564.065 ± 126.623 | -185.599 ± 19.235 | 0.972       |
| EQU+WTH+EQU | 2360.442 ± 260.701 | -280.947 ± 36.702 | 0.949       |

**Figure 6.** Homogeneity values of various %WIA images.

## 5. Conclusions

To evaluate the hydrophobicity of polymeric outdoor insulator surfaces, which are direct associated with the aging of materials, three digital image processes, the fractal dimension and two Haralick's descriptors, the homogeneity and entropy, were compared using different filters to adjust illumination conditions. For this comparison, samples

of silicon rubber sprayed with alcohol aqueous solutions were prepared. By controlling the alcohol proportion in the solution, it was possible to simulate the transition of a hydrophobic polymer surface to a hydrophilic surface. This methodology has shown to be very convenient to produce standard and reproducible samples with different levels of hydrophobicity and, from them to obtain digital images and contact angles of droplets on their surfaces.

To avoid light influence on the images, digital filters such as: equalization and White Top-Hat filter were used separately or in combination. As a result of the comparison between the methods it was found that the best digital process to classify hydrophobicity was the Haralick's descriptor homogeneity associated with the White Top-Hat filter, which presented the highest accuracy. Further work will be carried out comparing this method with more classical ones using this sample preparation method, in order to determine the best solution. As observed in previous studies, the use of fractal dimension shows a relation between its values and the image textures, but the Haralick's descriptors allowed a best correlation in a shorter time of processing, being more attractive to be applied in mobile devices to be used in the field by electricity companies.

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