

## A conservation law for self-hydrolysis process of aqueous sodium borohydride

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### ABSTRACT

A conservation law is obtained for self-hydrolysis process of aqueous sodium borohydride, which gives an explicit relationship between the concentrations of NaBH<sub>4</sub> and hydrogen ions during the global reaction.

**Keywords:** Sodium borohydride, Self-hydrolysis, Analytical model, Hydrogen storage.

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### 1. INTRODUCTION

Excellent catalytic performance of CoO nanocrystals on the catalytic hydrolysis of alkaline NaBH<sub>4</sub> solutions was observed experimentally, hydrogen generation from the hydrolysis of sodium borohydride (NaBH<sub>4</sub>) solution has drawn much attention recently, due to its high theoretical hydrogen storage capacity and potentially safe operation [1]. However, hydrolysis of NaBH<sub>4</sub> for hydrogen generation is a complex process [1-3], and it is highly needed to have an explicit formulation to reveal concentration change in the reaction process.

The hydrolysis of NaBH<sub>4</sub> is an exothermic reaction that yields hydrogen (H<sub>2</sub>) gas and water-soluble sodium metaborate (NaBO<sub>2</sub>). The global reaction of H<sub>2</sub>O and NaBH<sub>4</sub> is given in the form [2].



The rate of hydrolysis is a complicated reaction that is strongly dependent on solution temperature, NaBH<sub>4</sub> concentration, the molar concentration of dissolved hydrogen ions, H<sup>+</sup> [2]:

$$\frac{dx}{dt} = Ax^{\alpha_1}y^{\beta_1} \quad (2)$$

$$\frac{dy}{dt} = B \exp\left(\frac{\alpha_2(x_0 - x)}{x_0}\right)y^{\beta_2} \quad (3)$$

where  $x$  is NaBH<sub>4</sub> concentration,  $y$  is  $\text{H}^+$  concentration,  $x_0$  the initial concentration of NaBH<sub>4</sub>,  $A$  and  $B$  are constants depending upon temperature,  $\alpha_1$  and  $\beta_1$  represent the order of reaction for [NaBH<sub>4</sub>] and [H<sup>+</sup>], respectively.  $\alpha_2$  and  $\beta_2$  are the exponential constant and the order of reaction for [H<sup>+</sup>], respectively.

The system, Eqs. (2) and (3), can be effectively solved by some an analytical method, such as the variation iteration method, the homotopy perturbation method, and the parameter-expansion method [4,5]. This paper aims to searching for a conservation law for self-hydrolysis process of aqueous sodium borohydride (NaBH<sub>4</sub>) for hydrogen generation purpose.

## 2. CONSERVATION LAW

From Eqs. (2) and (3), we have

$$\frac{dx}{dy} = \frac{Ax^{a_1}y^{b_1}}{B \exp\left(\frac{a_2(x_0 - x)}{x_0}\right)y^{b_2}}$$

(4)

or

$$B \exp a_2 x^{-a_1} \exp(-a_3 x) dx = A y^{b_1 - b_2} dy$$

(5)

where  $\alpha_3 = \alpha_2 / x_0$ .

Integrating Eq. (5) results in

$$y^{b_1 - b_2 + 1} = \frac{B(b_1 - b_2 + 1) \exp a_2}{A} \int x^{-a_1} \exp(-a_3 x) dx$$

(6)

Eq. (6) is the conservation law for the self-hydrolysis process, which implies whatever the process continues, the concentrations of NaBH<sub>4</sub> and hydrogen ions must follow Eq. (6).

## 3. CONCLUSIONS

This work focuses on concentration changes of NaBH<sub>4</sub> and H<sup>+</sup> of the self-hydrolysis of sodium borohydride, the conservation law, Eq.(6), reveals the relationship between concentrations of NaBH<sub>4</sub> and H<sup>+</sup> in the global reaction process. The integration constant involving in Eq.(6) can be determined by the initial concentrations, and the conservation law can be used to predict the reaction process by the pH value of the solution, which is a measure of the molar concentration of dissolved hydrogen ions.

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