

Statistical Design for Recycling Kaolin Processing Waste in the Manufacturing of Mullite-Based Ceramics

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Mineral extraction and processing industries have been cited as sources of environmental contamination and pollution. However, waste recycling represents an alternative recovery option, which is interesting from an environmental and economic standpoint. In this work, recycling of kaolin processing waste in the manufacture of mullite-based ceramics was investigated based on the statistical design of mixture experiments methodology. Ten formulations using kaolin processing waste, alumina and ball clay were used in the experiment design. Test specimens were fired and characterized to determine their water absorption and modulus of rupture. Regression models were calculated, relating the properties with the composition. The significance and validity of the models were confirmed through statistical analysis and verification experiments. The regression models were used to analyze the influence of waste content on the properties of the fired bodies. The results indicated that the statistical design of mixture experiments methodology can be successfully used to optimize formulations containing large amount of wastes.

Keywords: *recycling, waste materials, design of mixture experiments, mullite*

1. Introduction

Natural raw materials are becoming scarce, while around the world, millions of tons of inorganic wastes are produced everyday in mining, mineral processing and industrial activities, whose disposal is subject to ever stricter environmental legislation. However, some wastes are similar in composition to the natural raw materials used in the fabrication of ceramics and often contain materials that are also beneficial in the fabrication process. Thus, upgrading wastes to alternative raw materials is of technological, economic and environmental interest¹⁻³.

Mining and mineral processing wastes have traditionally been discarded in landfills and often dumped directly into ecosystems without adequate treatment. However, possible reuse or recycling alternatives should be investigated and implemented³⁻⁵. Today, the reuse and recycling of wastes after their potentialities have been detected is considered an activity that can contribute to reduce production costs, provide alternative raw materials for a variety of industrial sectors, conserve nonrenewable resources, save energy, and improve public health⁶⁻⁸.

Kaolin is an important raw material in various industrial sectors. However the kaolin mining and processing industry generates large amounts of waste. The kaolin industry, which processes primary kaolin, produces two types of wastes. The first type derives from the first processing step (separation of sand from ore). The second type of waste results from the second processing step, which consists of wet sieving to separate the finer fraction and purify the kaolin.

Previous studies⁹ have indicated the viability of using kaolin processing waste for the production of ceramic bricks. However, these studies have proved to be economically unviable. Thus, there is a need to find solutions enabling kaolin processing waste to be incorporated into products of higher added value. In this respect, incorporation of wastes in mullite-based ceramics is being sought and is of high commercial interest¹⁰⁻¹³.

Mullite ($3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$), is the only stable compound of the SiO_2 - Al_2O_3 binary system under atmospheric pressure, is widely used in conventional and advanced ceramics because of its high melting point, low coefficient of thermal expansion, excellent creep resistance, good chemical stability and high strength at high temperature^{11,13,14}.

In the development and manufacture of ceramics using waste materials, the properties of fired bodies are basically determined by the combination of raw materials and process parameters. When the processing conditions are kept constant, a number of properties of dried and fired bodies are basically determined by the combination (or mixture) of raw materials¹⁵. This is the basic assumption in the statistical design of mixture experiments to obtain a response surface using mathematical and statistical techniques^{16,17}. To this end, it is necessary first to select the appropriate mixtures from which the response surface might be calculated. Then, from the calculated response surface, the property value of any mixture can be predicted based on the changes in the proportions of its components^{18,19}.

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This methodology has found important applications in various areas, and is becoming popular in the field of glasses and ceramics^{15,20-24}.

Current optimization procedures for developing ceramic compositions using waste materials are based mainly on experiments rather than on a comprehensive approach. In general, the approach consists of selecting and testing a first trial batch, evaluating the results, and then adjusting the mixture proportions and testing further mixtures until the required properties are achieved. The conventional method of optimization is time consuming and does not allow for detection of the global optimum, especially due to the interactions among the factors. In contrast, statistical design methods are rigorous techniques not only for achieving desired properties but also for establishing an optimized mixture for a given constraint while minimizing the number of trials^{25,26}.

Statistical experimental design methodology is an established and proven methodology^{16,17}, but no researchers have reported using this technique in the research of recycling of mining and mineral wastes for the production of ceramic materials. Thus, this work aims to study the recycling of kaolin processing waste in the manufacture of mullite-based ceramics using the statistical design of mixture experiments methodology.

2. Materials and Methods

The waste investigated here was obtained from the second step of primary kaolin processing. The waste was dried at 110 °C, dry milled in a ball mill and sieved through a 150 µm mesh. The other raw materials used in this research were ball clay (Arnil Minerios, Brazil – D₁₀ of about 0.8 µm, D₅₀ of about 2.0 µm and D₉₀ of about 5.0 µm) and alumina (A1000SG, Alcoa Industrial, Chemicals Division – D₁₀ of about 0.3 µm, D₅₀ of about 0.6 µm and D₉₀ of about 1.9 µm). These commercial materials were used in the as-received condition. Table 1 presents the chemical composition of the raw materials, determined by wet process.

Physical and chemical characterizations of kaolin processing waste are described elsewhere^{27,28}. According to those reports, kaolin waste is composed of kaolinite (Al₂Si₂O₅(OH)₄), mica (KAl₂(Si₃Al)O₁₀(OH,F)₂) and quartz (SiO₂) and has a particle size distribution with a mean value of 54 µm and a D₅₀ of 58 µm, a D₁₀ of about 5 µm and a D₉₀ of about 135 µm.

A {3,2} centroid simplex-lattice design, augmented with interior points, was used to define the mixtures of raw materials

to be investigated. Mixtures with the selected compositions were processed as follows: wet mixing/milling (using ball mill), drying (24 hours), de-agglomerated (by gently grinding in a mortar), moisturizing (6.5 wt. (%), dry basis) and granulation. Test specimens (50 x 20 x 5 mm) were obtained by uniaxial pressing under 35 MPa, and were sintered in a laboratory furnace at 1300 and 1400 °C for 2 hours in air, at a heating rate of 5 °C/min, followed by natural cooling. Three independent batches (replications) of each composition were prepared and processed.

The water absorption (WA) was determined using the Archimedes liquid displacement method by immersion in water for 24 hours. The fire modulus of rupture (MR) was determined in a three-point-bending test, with a 0.5 mm/min cross-head using the test specimens (50 x 20 x 5 mm).

The results of the three replications were used to calculate the coefficients of the regression equations iteratively until statistically relevant models and response surfaces were obtained, relating the WA and MR with the proportions of waste and commercial raw materials used in the formulations. The calculations were carried out with Statistica 6.0 (StatSoft Inc., 2001) software.

The resulting statistical analysis involves fitting of mathematical equations to the experimental results (i.e., water absorption and modulus of rupture) to get the entire response surface, and validation of the model through an analysis of variance.

X ray diffraction patterns of the fired bodies were obtained in an X ray diffractometer (Shimadzu, XRD 7000) using Cu K_α radiation. Diffraction patterns were recorded for the 2θ range 10-70°.

3. Results and Discussion

Table 2 list the compositions of the 10 mixtures (M_i, i = 1, 2, ..., 10), while Table 3 presents the measured values of water absorption (WA) and modulus of rupture (MR) of the fired test specimens.

Based on the data obtained (Table 3), regression equations were designed for the properties analyzed at 1300 and 1400 °C, with a 5% level of significance. Equation (1) to (4) describe the behavior of the properties in response to the proportions of raw materials. Statistically these equations were found to be the most adequate (5% significance level).

$$WA_{1300^{\circ}C} = 9.57A + 5.79B + 2.03K + 9.37AB + 4.42BK + 85.30ABK - 23.03 AK(A - K) \quad (1)$$

Table 1. Chemical composition^a (wt. (%)) of the wastes and commercial raw materials used.

Material	SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	K ₂ O	TiO ₂	CaO	Na ₂ O	LOI ^b
Kaolin waste	52.68	33.57	0.93	5.72	0.12	-	0.08	6.75
Ball clay	56.29	27.10	1.60	0.18	0.70	-	0.09	14.02
Alumina	00.03	99.80	0.02	-	-	0.02	0.03	-

a) Determined by wet chemical analysis; and b) Loss on Ignition.

Table 2. Compositions of the design mixtures created by the augmented {3,2} simplex.

Raw Material (wt. (%))	Design Mixture									
	M ₁	M ₂	M ₃	M ₄	M ₅	M ₆	M ₇	M ₈	M ₉	M ₁₀
Alumina	100.0	000.0	000.0	50.0	50.0	00.0	33.3	66.6	16.6	16.6
Ball Clay	000.0	100.0	000.0	50.0	00.0	50.0	33.3	16.6	66.6	16.6
Kaolin waste	000.0	000.0	100.0	00.0	50.0	50.0	33.3	16.6	16.6	66.6

Table 3. Measured values of water absorption and modulus of rupture obtained for the 10 simplex mixtures.

	Temperature 1300 °C		Temperature 1400 °C	
	WA ^a (%)	MR ^b (MPa)	WA ^a (%)	MR ^b (MPa)
Replication 1				
M ₁	9.58	47.50	5.66	89.51
M ₂	5.13	19.85	7.72	18.14
M ₃	1.73	16.56	1.65	13.38
M ₄	9.91	36.00	8.21	46.97
M ₅	6.44	33.21	4.09	34.32
M ₆	5.22	19.08	0.90	20.57
M ₇	9.38	22.56	6.12	25.21
M ₈	9.20	43.98	8.65	43.84
M ₉	10.56	20.88	4.39	28.99
M ₁₀	8.37	16.09	2.97	28.45
Replication 2				
M ₁	9.47	57.21	5.26	82.26
M ₂	5.59	15.67	8.18	18.78
M ₃	1.94	15.35	1.04	12.21
M ₄	9.66	39.93	7.26	37.00
M ₅	5.08	34.97	3.98	40.82
M ₆	4.86	20.67	1.36	23.78
M ₇	9.08	25.03	6.46	30.07
M ₈	9.45	43.08	9.09	50.37
M ₉	9.83	18.54	5.68	21.81
M ₁₀	8.35	21.54	3.86	29.95
Replication 3				
M ₁	9.31	52.39	5.49	93.26
M ₂	5.12	18.05	7.89	19.77
M ₃	2.07	15.14	1.66	12.36
M ₄	9.97	40.10	7.86	38.86
M ₅	5.38	37.00	4.02	34.76
M ₆	4.59	16.86	0.78	29.33
M ₇	9.18	24.47	7.30	26.51
M ₈	9.54	43.49	8.94	38.84
M ₉	9.62	22.00	5.70	25.04
M ₁₀	8.64	19.55	3.82	24.92
Replication 4				
M ₁	9.42	53.50	5.33	78.32
M ₂	6.81	20.32	7.42	22.88
M ₃	1.86	13.92	1.55	10.40
M ₄	9.52	35.73	7.99	44.61
M ₅	4.70	35.47	4.30	38.56
M ₆	4.35	22.01	1.13	16.82
M ₇	9.32	24.56	6.80	27.30
M ₈	9.72	38.70	9.33	39.00
M ₉	10.38	20.24	5.45	23.07
M ₁₀	7.68	23.20	3.32	28.20

a) Water absorption, and b) Modulus of rupture.

$$WA_{1400^{\circ}\text{C}} = 5.46A + 7.83B + 1.50K + 4.97AB + 2.69AK - 14.26BK + 30.07AB(A - B) \quad (2)$$

$$MR_{1300^{\circ}\text{C}} = 52.69A + 18.51B + 15.28K - 195.05ABK + 42.10AB(A - B) \quad (3)$$

$$MR_{1400^{\circ}\text{C}} = 85.87A + 19.92B + 12.12K - 43.89AB - 47.25AK + 26.68BK - 139.24AK(A - K) \quad (4)$$

Equations (1) to (4) are referred to the raw materials used; A, B and K are the fractions of alumina, ball clay and kaolin waste, respectively. Table 4 lists the main statistical properties of the regressions obtained with the analysis of variance, using the nomenclature commonly reported in the literature^{16,17}. All the regression models employed (Equations (1) to (4)) were found to be statistically significant at the required level (p valor below the significance level) and to present little variability (high coefficients of multiple determination). The coefficients of multiple determination indicate the percentage of variation in the response, which is explained by the deliberate variation in the factors (raw materials fractions) during the course of the experiment²⁹.

The significance of the derived models can also be evaluated by comparing the F test value to the F value tabulated in Fisher-Snedecor distribution^{16,17}. The regression is considered statistically significant, i.e., the fluctuations due to the independent variables are mainly explained by the model, if the F value is greater than the tabulated value (for the required significance level). All the F values presented in Table 4 are more than fivefold higher than the tabulated values.

To evaluate the adequateness of the regression models also requires analyzing the residuals. Figures 1 and 2 present the plot of properties (WA and MR) raw residuals vs. predicted values and normal probability curves for property residuals after firing at 1300 and 1400 °C. The raw residual is the difference between the experimentally determined value and the calculated estimate²¹. The plots of raw residuals vs. predicted values (Figures 1 and 2) show that the error values can be considered randomly distributed around a mean zero value (i.e. they are uncorrelated), which suggests a common constant variance for all the property values at the two temperatures. Straight lines can be considered to correlate the expected normal values with the raw residuals, indicating that the distribution of residuals is normal. Thus, Table 4 and Figures 1 and 2 suggest that the regression model equations are adequate to predict the behavior of the properties of the fired ceramic bodies to a very high degree of confidence.

To counter-check the statistical models, test specimens of the compositions M₁₁ (40.0 wt. (%) ball clay, 60.0 wt. (%) kaolin waste), M₁₂ (40 wt. (%) alumina, 60 wt. (%) kaolin waste), M₁₃ (34.0 wt. (%) alumina, 6 wt. (%) ball clay, 60 wt. (%) kaolin waste) and M₁₄ (60 wt. (%) alumina, 40 wt. (%) kaolin waste) were prepared (as described in the Experimental Procedure) and their WA and MR were predicted based on the models and were measured experimentally. Table 5 shows the results obtained, indicating that the errors of the predicted values are low, thus confirming the validation of the calculated models.

Figure 3 depicts the X ray diffraction patterns of the test specimens of the compositions M₁₁, M₁₂, M₁₃ and M₁₄ after firing at 1300 and 1400 °C. The bodies presented mullite (3Al₂O₃·2SiO₂), quartz (SiO₂) and/or alumina (Al₂O₃) as crystalline phases after firing at 1300 °C and 1400 °C. The XRD patterns show that mullite and alumina are the main crystalline phases presented in compositions M₁₂, M₁₃ and M₁₄ after firing at 1400 °C.

The mathematical Equations (1) to (4), which describe the change and evolution of the properties as a function of composition (wastes content) are expressed in their canonical form as low degree polynomials in the form of full cubic models. However, statistically, the

Table 4. Analysis of variance for significance of regression models^a.

Property	Temperature (°C)	Regression model	SSR	DF	MSR	SSE	DF	MSE	F test	p value	R ² (%)
WA ^b	1300	Full Cubic	15.2287	2	7.6144	19.8067	31	0.6390	11.9175	0.0001	93.04
WA ^b	1400	Full Cubic	19.7784	2	9.8892	4.8567	31	0.1567	63.1221	<0.0001	98.18
MR ^c	1300	Full Cubic	48.720	2	24.360	161.0971	31	5.1967	4.6876	0.0166	97.23
MR ^c	1400	Full Cubic	412.70	2	206.350	480.422	31	15.4975	13.3151	0.0001	96.95

a) SSR: regression sum of squares; DF: degrees of freedom; MSR: regression mean squares; SSE: error sum of squares; MSE: error mean squares; R²: coefficient of multiple determination; b) Water Absorption; and c) Modulus of rupture.

Table 5. Composition of checkpoint mixtures and corresponding measured and predicted values of water absorption and modulus of rupture.

Temperature (°C)	Composition (wt. (%))			Predicted values		Measured values ± SD ^c	
	Alumina	Ball clay	Kaolin waste	WA ^a	MR ^b	WA ^a	MR ^b
1400	00.0	40.0	60.0	0.61	21.65	0.77 ± 0.04	21.70 ± 0.87
1300	40.0	00.0	60.0	6.16	30.24	5.68 ± 0.28	28.31 ± 1.70
1400	40.0	00.0	60.0	3.73	36.96	4.18 ± 0.21	33.75 ± 1.35
1300	34.0	06.0	60.0	7.43	26.04	6.17 ± 0.41	27.96 ± 1.68
1400	34.0	06.0	60.0	4.44	35.47	4.38 ± 0.22	34.60 ± 1.38
1300	60.0	00.0	40.0	5.46	37.72	3.83 ± 0.39	36.66 ± 2.20
1400	60.0	00.0	40.0	4.52	38.35	3.55 ± 0.28	40.08 ± 1.60

a) Water Absorption; b) Modulus of rupture; and c) Standard Deviation.

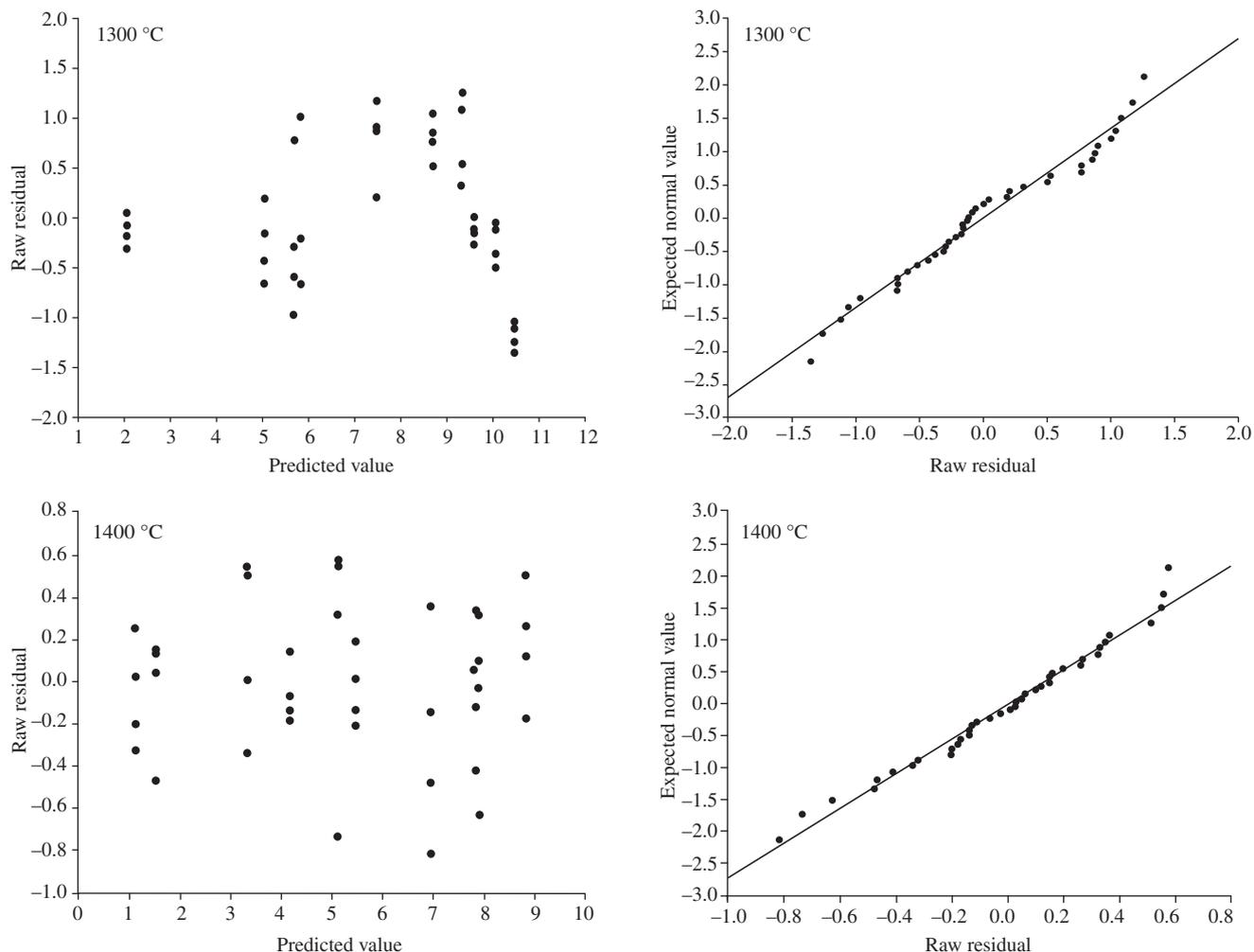


Figure 1. Water absorption raw residuals vs. predicted values and normal probability curve for water absorption residuals at 1300 °C and 1400 °C.

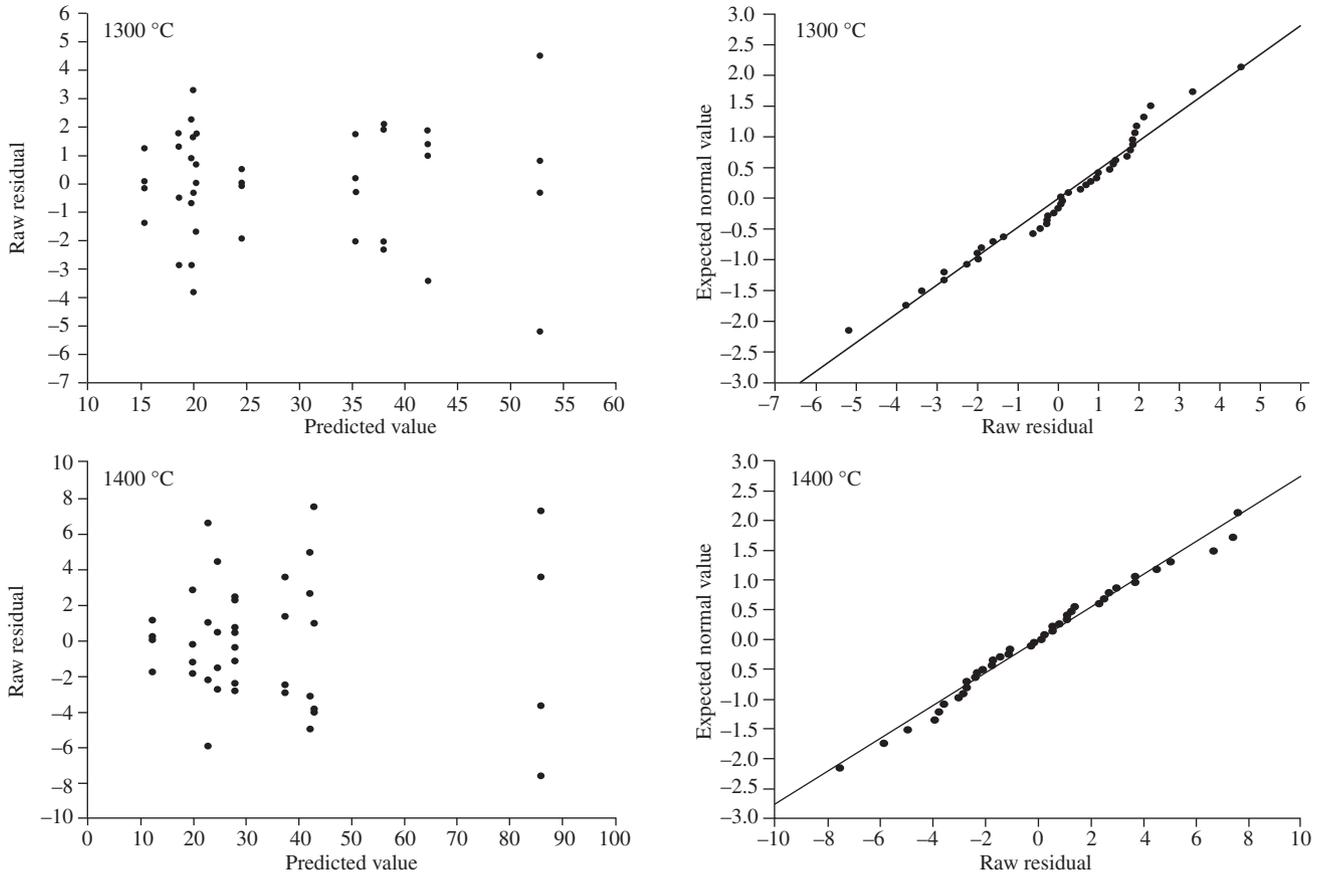


Figure 2. Modulus of rupture raw residuals vs. predicted values and normal probability curve for modulus of rupture residuals at 1300 °C and 1400 °C.

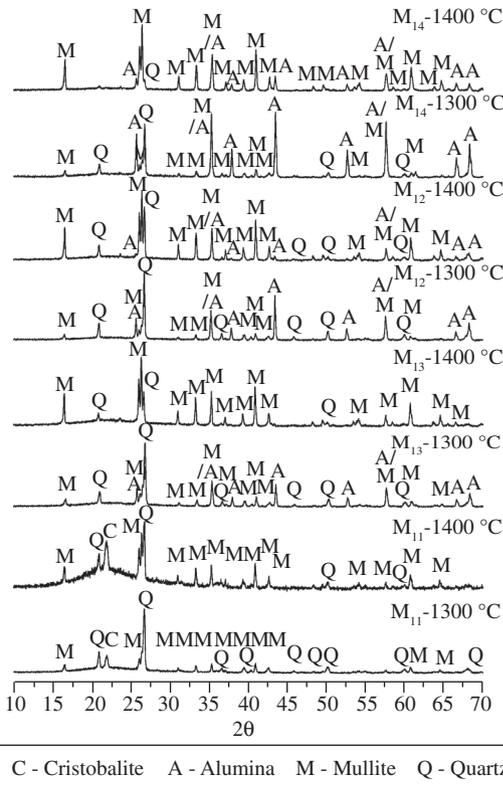


Figure 3. X ray diffraction patterns of the test specimens of the compositions M_{11} , M_{12} , M_{13} and M_{14} after firing at 1300 °C and 1400 °C.

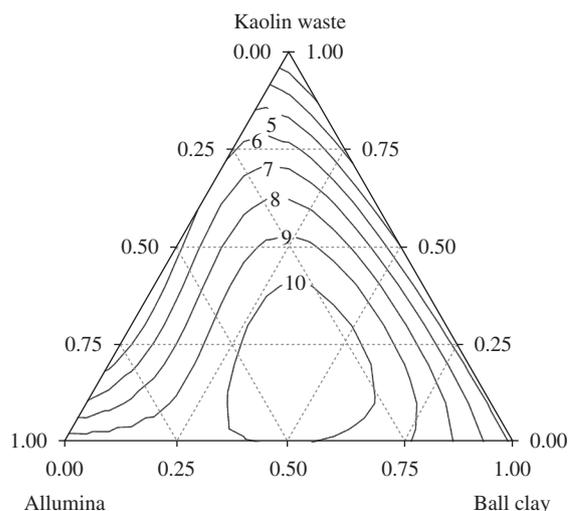
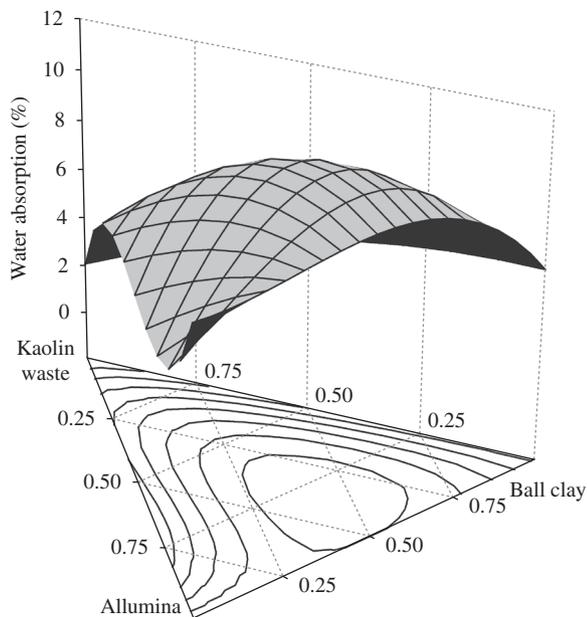
most adequate model can vary according to the analyzed property and the firing temperature, as reported in a previous work³⁰, which expressed the properties of ceramic bricks and tiles using special cubic and quadratic models, according to firing temperature.

Comparing the values and signs of the coefficients of the models in Equations (1) and (2), it may be deduced that the most synergistic interaction after firing at 1300 °C is that manifested between alumina and kaolin waste, while the most synergistic interaction after firing at 1400 °C is associated with ball clay-kaolin waste mixtures. On the other hand, the mixtures of the three components and the interactions between alumina and ball clay are the most antagonistic interactions after firing at 1300 and 1400 °C, respectively.

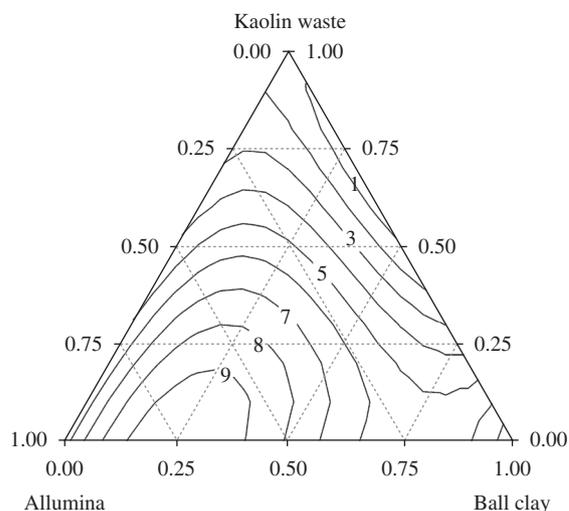
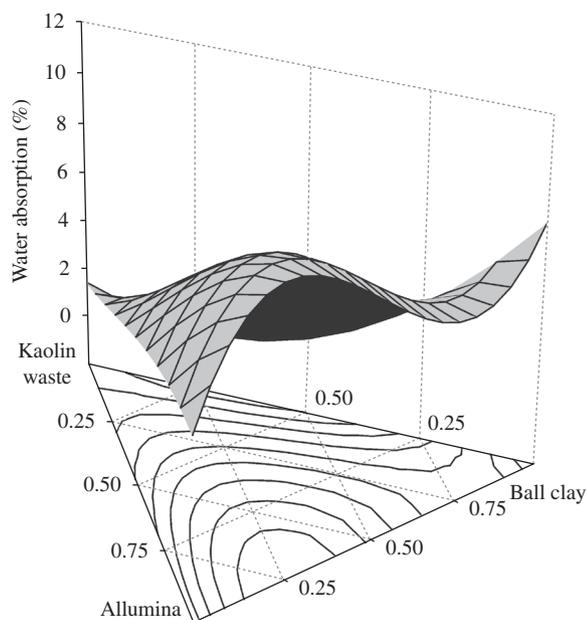
The most synergistic effect on the MR after firing at 1300 and 1400 °C (Equations (3) and (4)) is associated with the alumina content. The mixtures of the three components act in an antagonistic manner after firing at 1300 °C. After 1400 °C, the alumina-ball clay and alumina-kaolin waste mixtures have an antagonistic effect on the MR.

This analysis indicates that the inadequate use of kaolin waste can decrease the properties of mullite-based ceramics and emphasizes that the statistical design methods are the most appropriate for optimizing the mixtures, because they can minimize the deleterious effects of the waste on the properties of the fired bodies rapidly, while optimize the mixtures by conventional methods would be very difficult and time consuming.

Figures 4 and 5 show the calculated response surface plots and their projections onto the composition triangle (as constant properties contours - contour plot) for the WA and MR, respectively. The 3-D surface plot is the graphical representation of Equations (1) to



(a)



(b)

Figure 4. Response surface plots and their projections onto the composition triangle for water absorption at a) 1300 °C; and b) 1400 °C.

(4) and allows for easy and rapid predictive estimates over the entire composition range under investigation.

Figure 4 shows that WA increases with the decrease in kaolin waste content at 1300 °C and 1400 °C. However, the alumina-kaolin waste mixtures rich in alumina presented low WA values. As Figure 5 indicates, the highest MR values correspond to compositions with high alumina content (>90 wt. (%)) and that the MR of compositions with high amounts of kaolin waste or ball clay is similar after firing at 1300 °C and 1400 °C.

Another way of visualizing the effect that changes in composition might have on a given property is through the use of response trace plots. The response trace is a plot of the estimated property values as the composition moves away from a reference point, along lines that go through one of the triangle apexes (i.e., it is a vertical section through the property prism in which the fraction of one of the components is changed while the proportion between the other two is kept constant). In this way, the effect of each raw material on those properties can be best visualized^{19,21}. Figure 6 shows the WA and MR

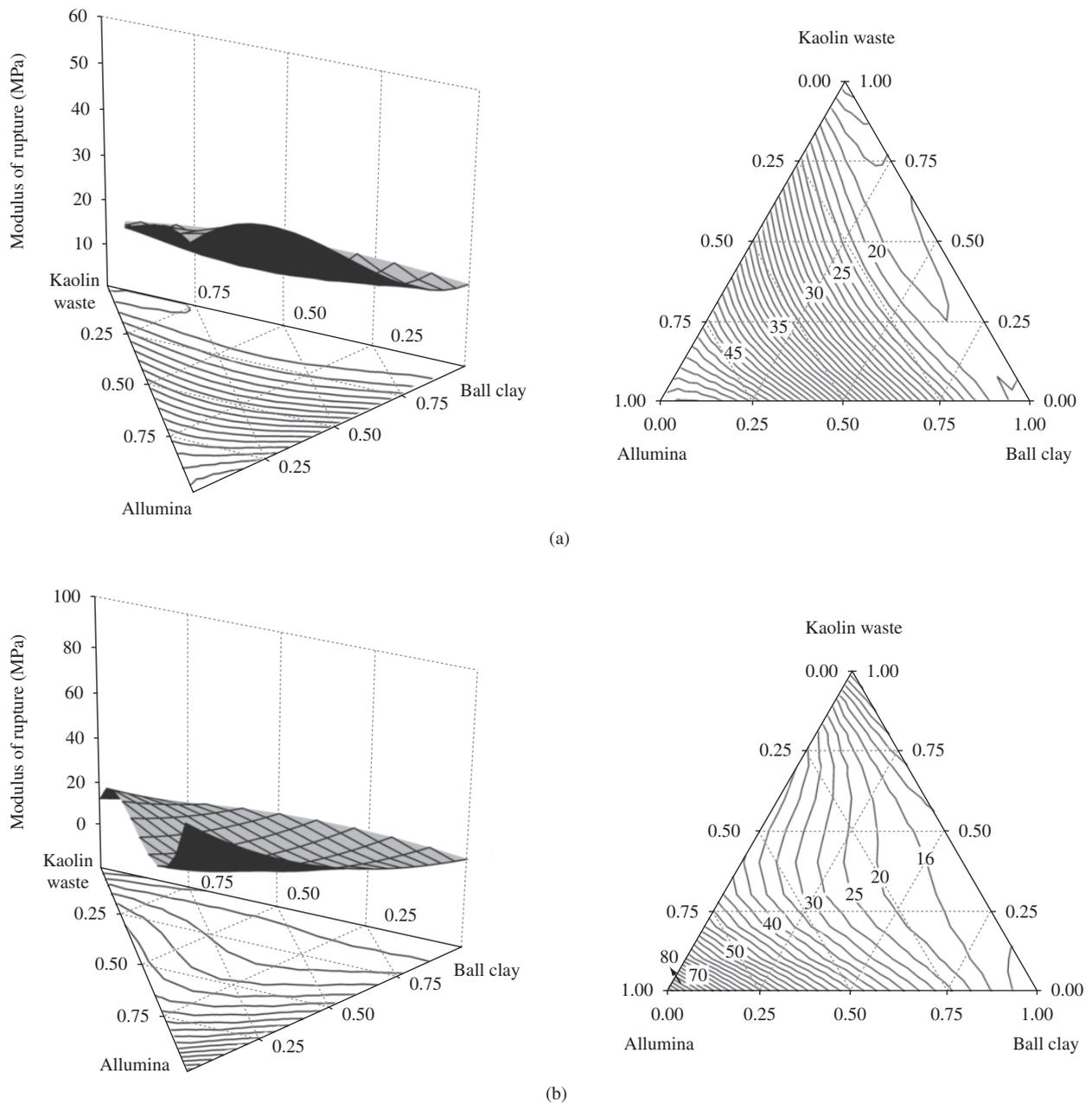


Figure 5. Response surface plots and their projections onto the composition triangle for modulus of rupture at a) 1300 °C; and b) 1400 °C.

trace plots. The reference composition used in the trace plots was the simplex centroid (M_1 in Table 2), which corresponds to 33.3 alumina, 33.3 ball clay, and 33.3 kaolin waste.

Figures 6a and 6b show that increasing the kaolin waste content decreases the WA at 1300 and 1400 °C. The increase in the ball clay and alumina contents increases the WA, but starting from a given amount, the rise in their content, generally causes the WA to decrease.

Figures 6c and 6d indicate that the MR is particularly sensitive to the changes in the alumina content. A sharp decline in the MR can be observed as the alumina content decreases. This behavior is most pronounced at 1400 °C, but is also unmistakable at 1300 °C. The increase in kaolin waste and ball clay contents decreases the MR at

1300 and 1400 °C. But there is a composition range of intermediary-to-high kaolin waste content (35-65 wt. (%)) in which the MR is mildly influenced by the increase in kaolin waste content.

These observations suggest the following: it is interesting use the highest possible proportion of alumina in the formulations; the waste content in the mixtures can be increased in compositions containing more than 35% and up to 65% of waste without severe decreasing the MR; the ball clay content is a detrimental factor for the MR particularly for intermediary-to-high clay contents.

The results indicate that the statistical design of mixture experiments methodology can be used successfully to optimize formulations containing large amounts of wastes. They also suggest the suitability of tailoring waste content to obtain the desired property.

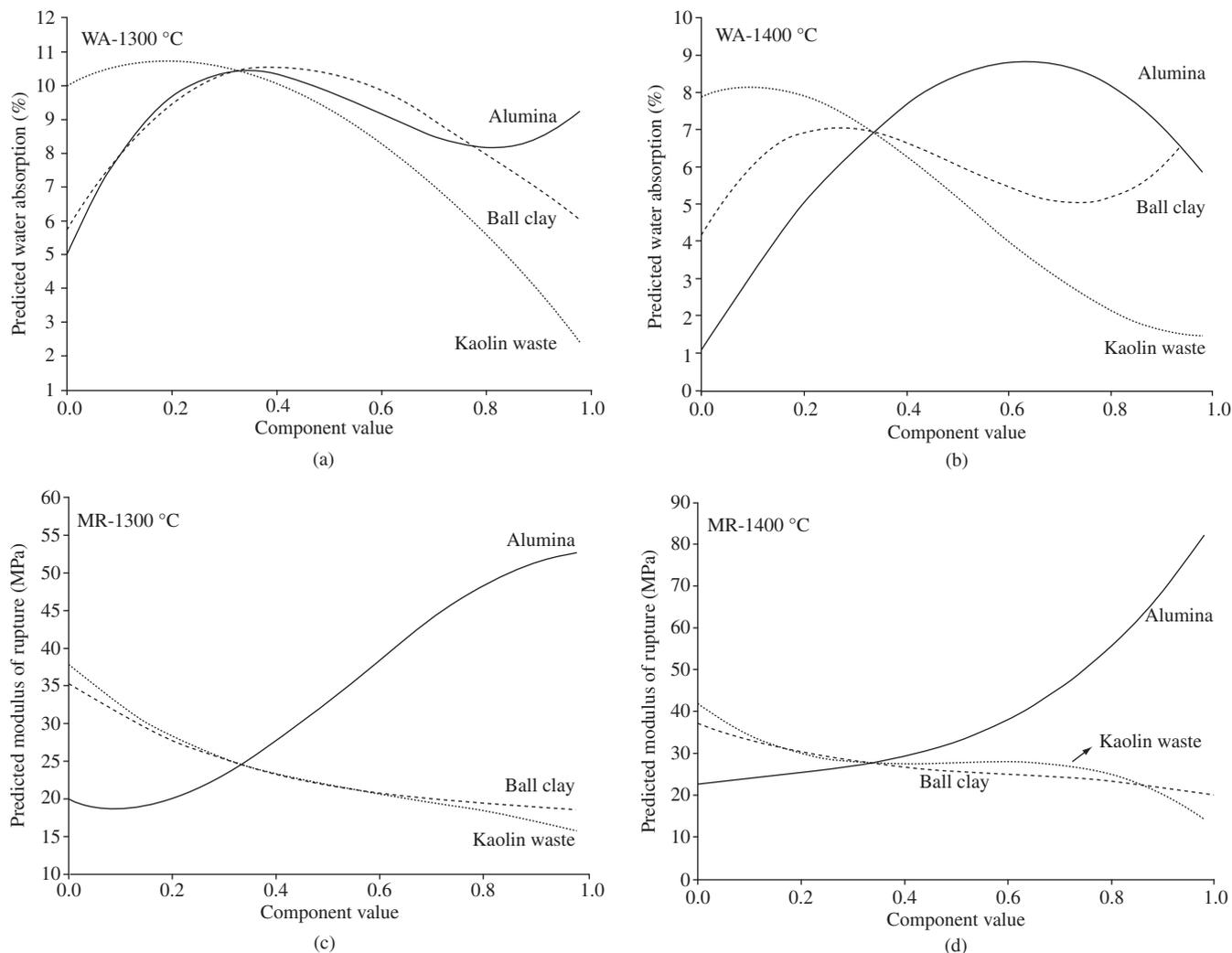


Figure 6. Predicted properties trace plots: a) water absorption at 1300 °C, b) water absorption at 1400 °C, c) modulus of rupture at 1300 °C; and d) modulus of rupture at 1400 °C.

4. Conclusions

The statistical design of mixture experiments and response surface methodologies proved to be powerful tools for planning and analyzing experiments to ascertain the influence of kaolin processing waste content on the technological properties of mullite-based ceramic bodies and to optimize ceramic formulations containing large amount of waste. The calculated regression models were found to be statistically significant at the required level and presented little variability. These regression models, which can be used in the scientific of the optimal waste content to produce mullite-based ceramic bodies with specific properties, offer substantial time savings.

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